



UNIVERSITÉ
DE GENÈVE

From bulk descriptions to emergent interfaces

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University of Geneva
Switzerland

AVALANCHE 2022

Avalanche dynamics and precursors of catastrophic events
August 29th, 2022

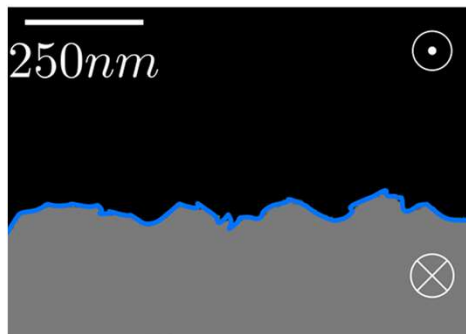
DQMP Department of
Quantum
Matter
Physics



Interfaces

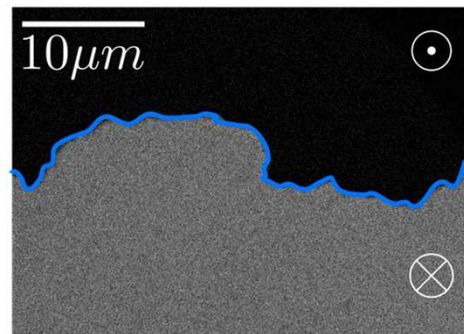
Are ubiquitous in Nature

Ferroelectrics



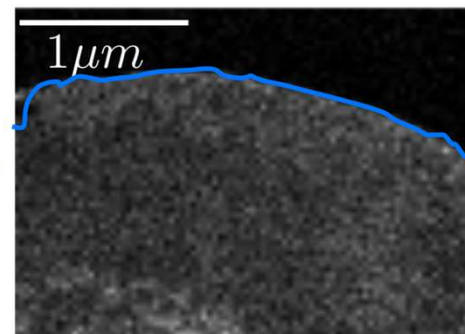
Rapin, Ehrensperger, Blaser, NC, Paruch *et al.* PRB 2017
Obtained in Paruch Lab
UNIGE- Geneva

Ferromagnets



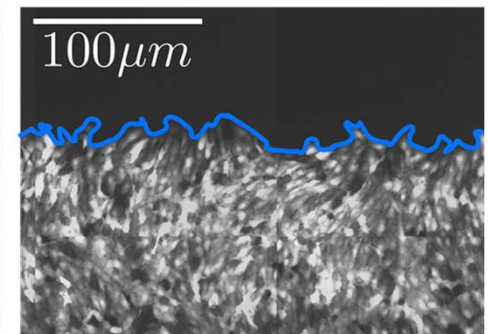
Obtained in Magnetic Resonances Laboratory
Bariloche Atomic Centre- Argentina

Cell membranes



Obtained in Roux Lab in collaboration with Rapin, NC, Sliemers *et al.* 2021.
Biochemistry Department
UNIGE-Geneva

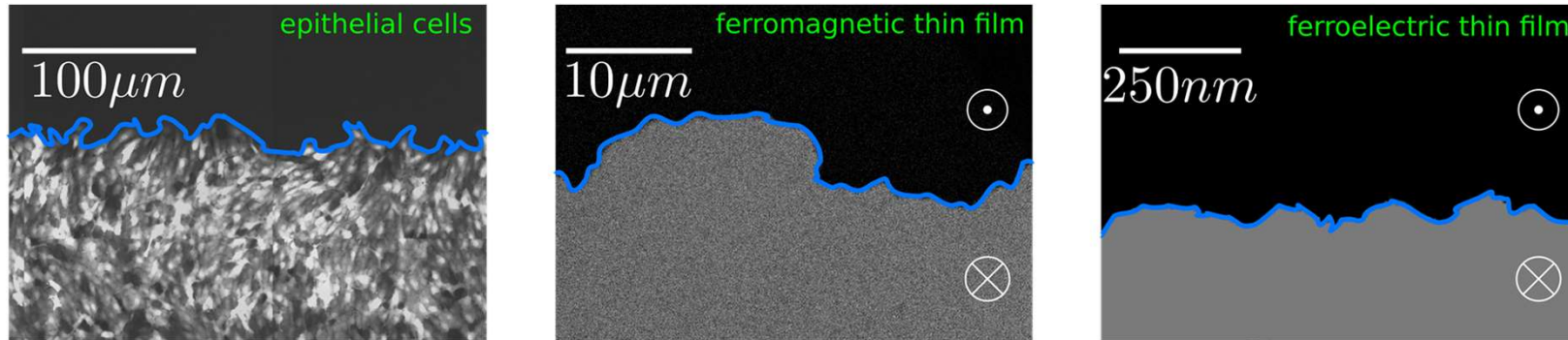
Cell colony



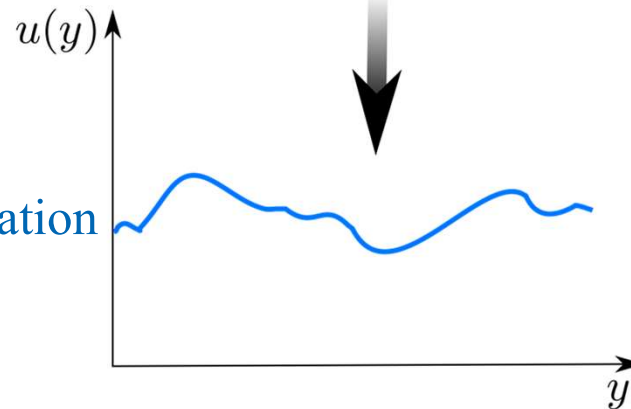
Obtained in Brown's Lab
UZH- Zurich

Tools to study interfaces

Disordered elastic systems framework



Brutal, but effective simplification



$u(y)$ Smooth, univalued

K. Wiese. Theory and experiments for disordered elastic manifolds, depinning, avalanches, and sandpiles, Reports on progress in Physics (2022)

T. Giamarchi, et al. *Dynamics of Disordered Elastic Systems*. Lecture Notes in Physics, vol 688. Springer, Berlin, Heidelberg (2006)

G. Rapin, NC, I. Gaponenko, A. Rawleigh, E. Moriggi, T. Giamarchi, S. A. Brown, P. Paruch, *Roughness and dynamics of proliferating cell fronts as a probe of cell-cell interactions*. Sci Rep. (2021)

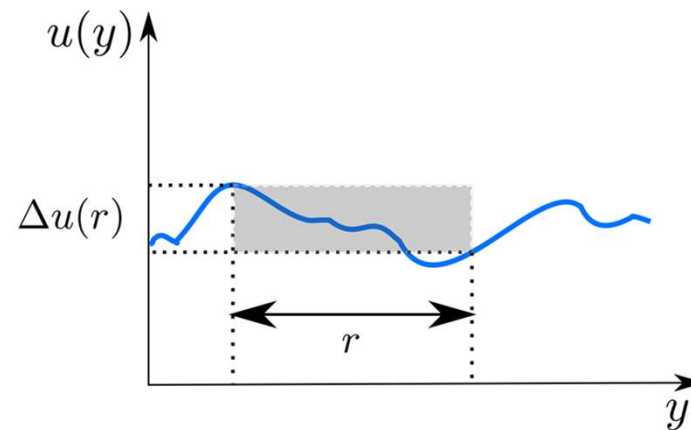
G. Rapin, et al, *Dynamic response and roughening of ferroelectric domain walls driven at electrode edges*. APL (2021)

P. Tuckmantel et al, *Local probe comparison of ferroelectric switching event statistics in the creep and depinning regimes in Pb(Zr_{0.2}Ti_{0.8})O₃ thin films*. PRL (2021)

NC, et al, *Excess velocity of magnetic domain walls close to the depinning field*. PRB (2017)

Tools to study interfaces

Disordered elastic systems framework



$$\tilde{\eta} \partial_t u(y, t) = c \partial_y^2 u(y, t) + F_p(u, y) + F + \sqrt{T} \tilde{\zeta}(y, t)$$

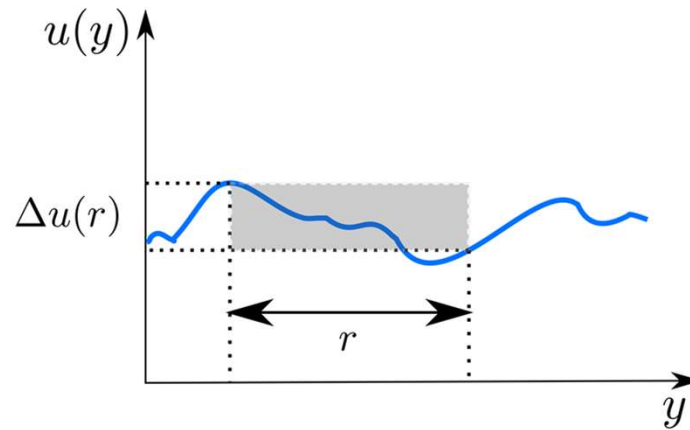


quenched Edwards-Wilkinson equation

the geometrical and dynamical properties of an interface are intrinsically related

Tools to study interfaces

Disordered elastic systems framework



Roughness

$$B(r) = \overline{\langle [u(y+r) - u(y)]^2 \rangle}$$

$$\tilde{\eta} \partial_t u(y, t) = c \partial_y^2 u(y, t) + F_p(u, y) + F + \sqrt{T} \tilde{\zeta}(y, t)$$



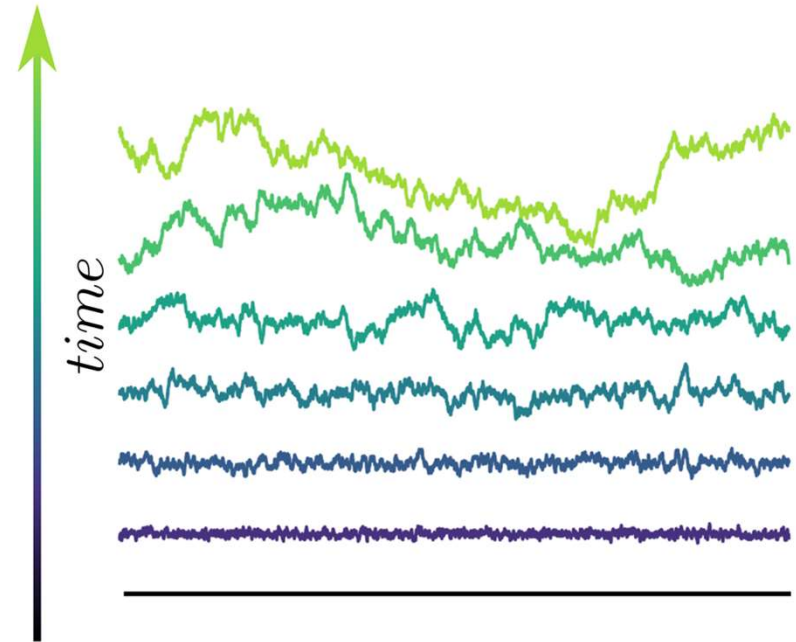
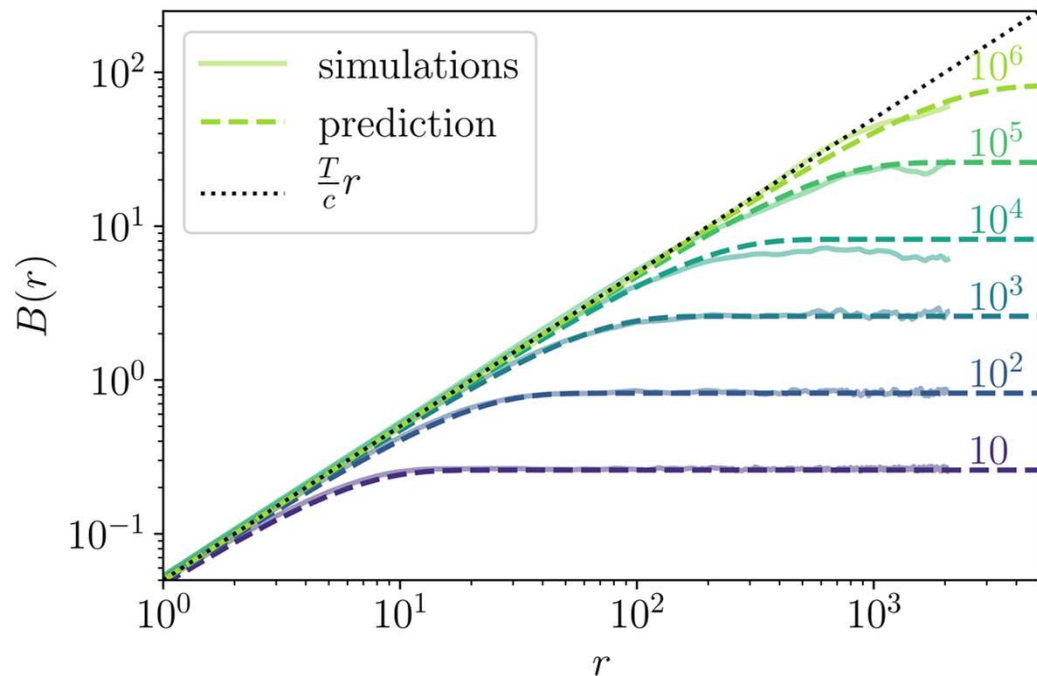
quenched Edwards-Wilkinson equation

the geometrical and dynamical properties of an interface are intrinsically related

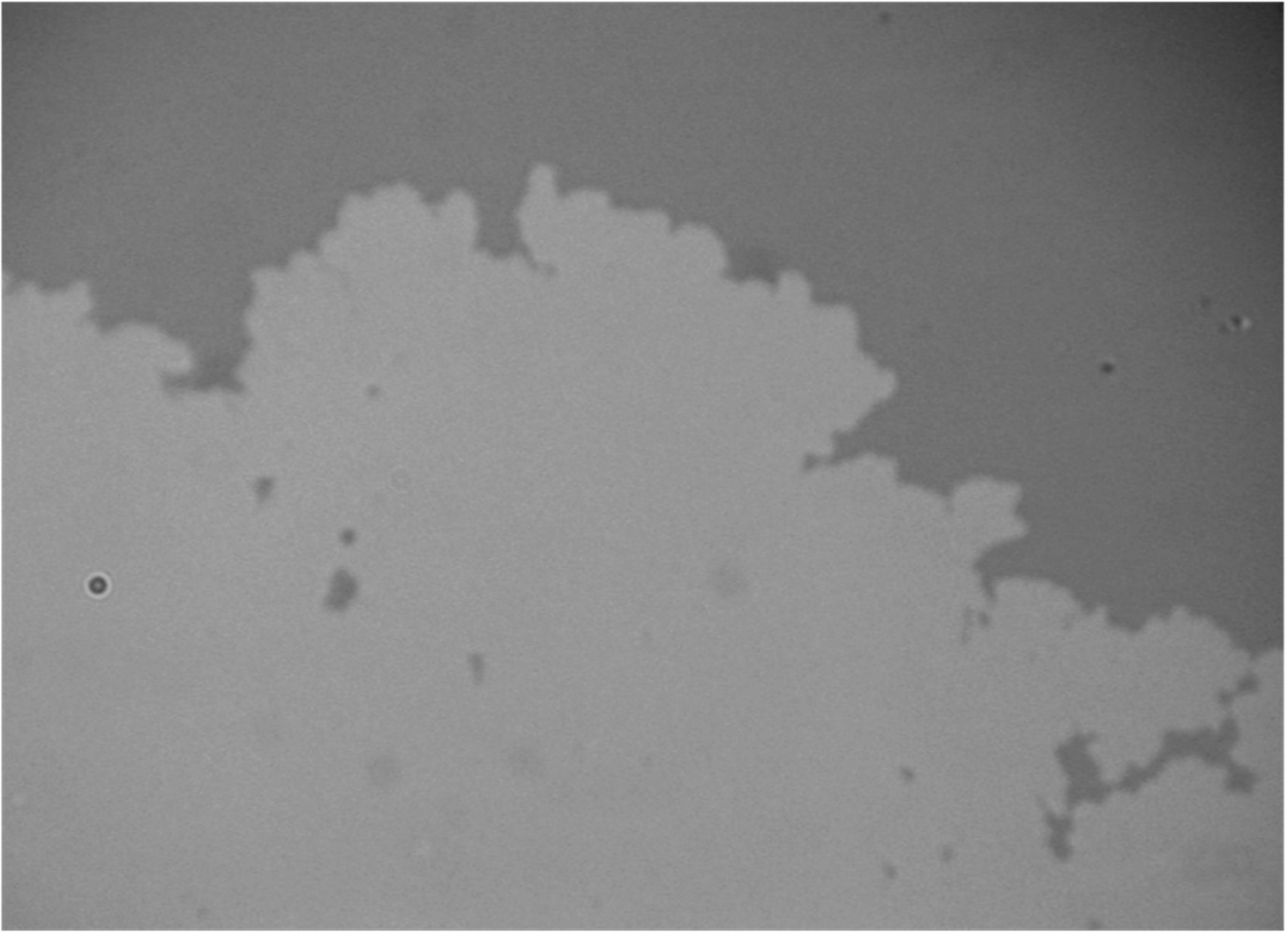
Tools to study interfaces

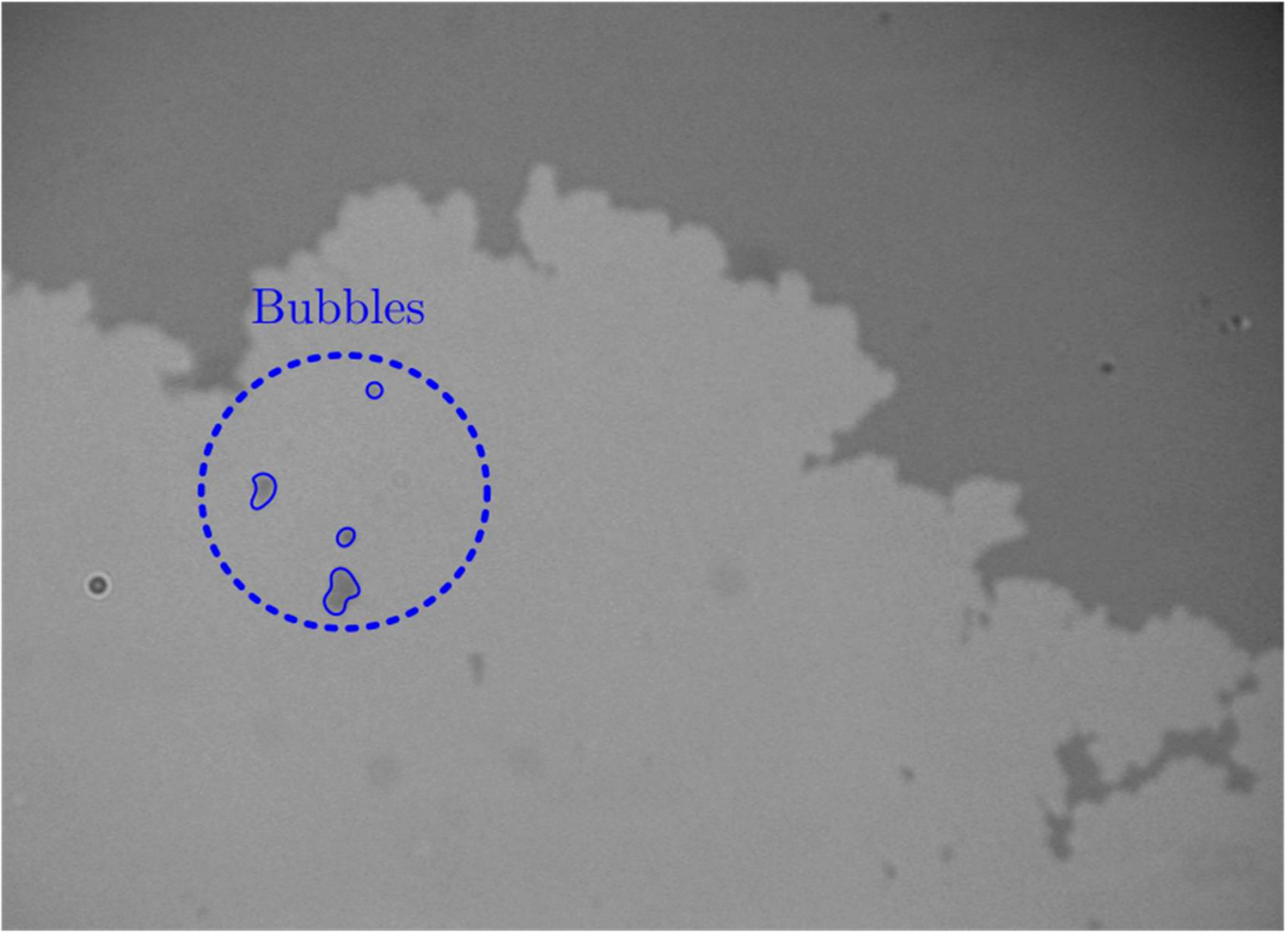
Disordered elastic systems framework

$$B(r, t) = \frac{Tr}{c} \left[1 - \frac{1}{\sqrt{\pi} z r} \left(e^{-z^2 r^2} - 1 \right) - \frac{2}{\sqrt{\pi}} \int_0^{zr} e^{-t^2} dt \right] \quad z = \sqrt{\frac{\tilde{\eta}}{8ct}}$$

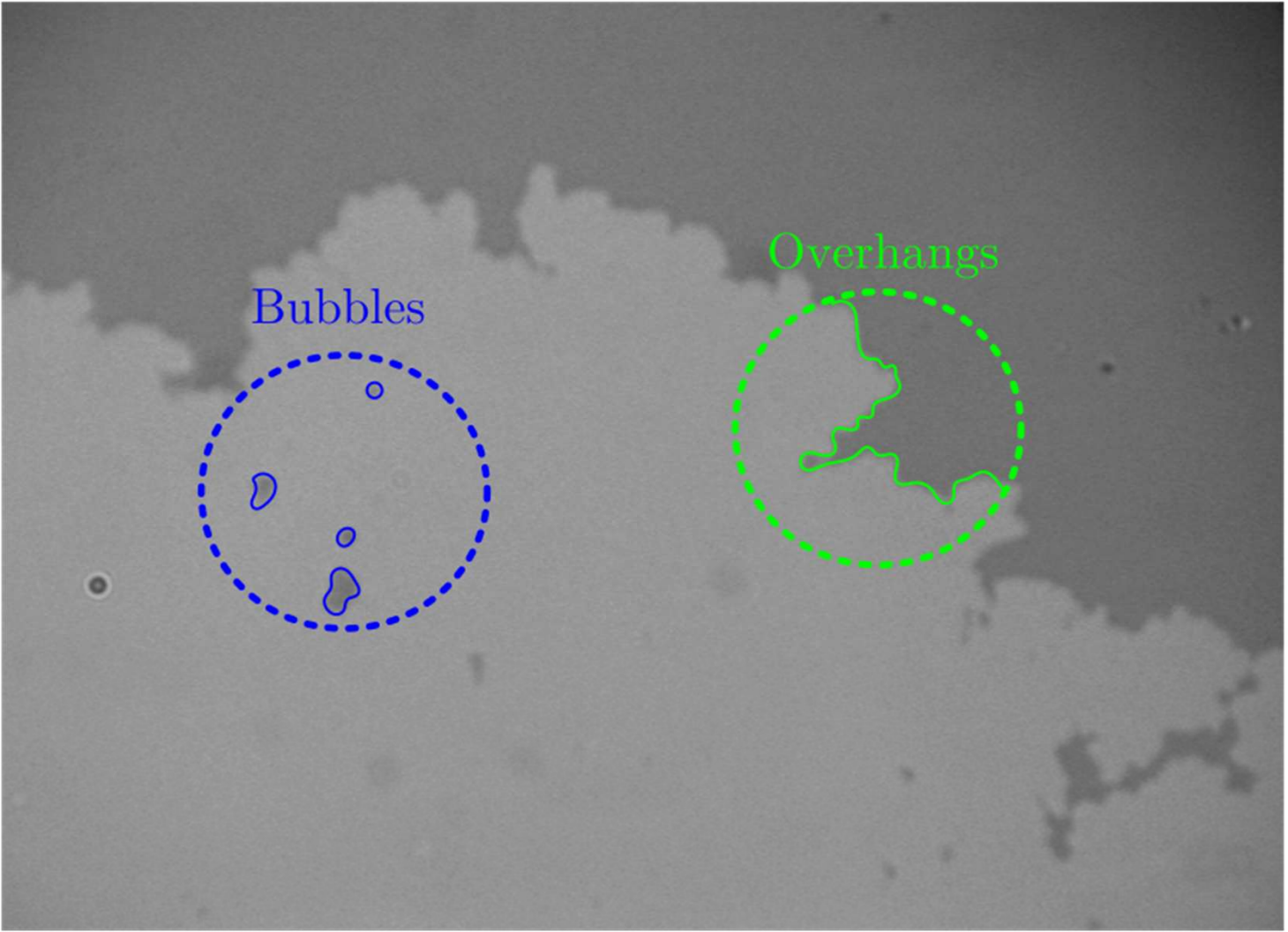


The framework allows us to perform very precise analytical calculations



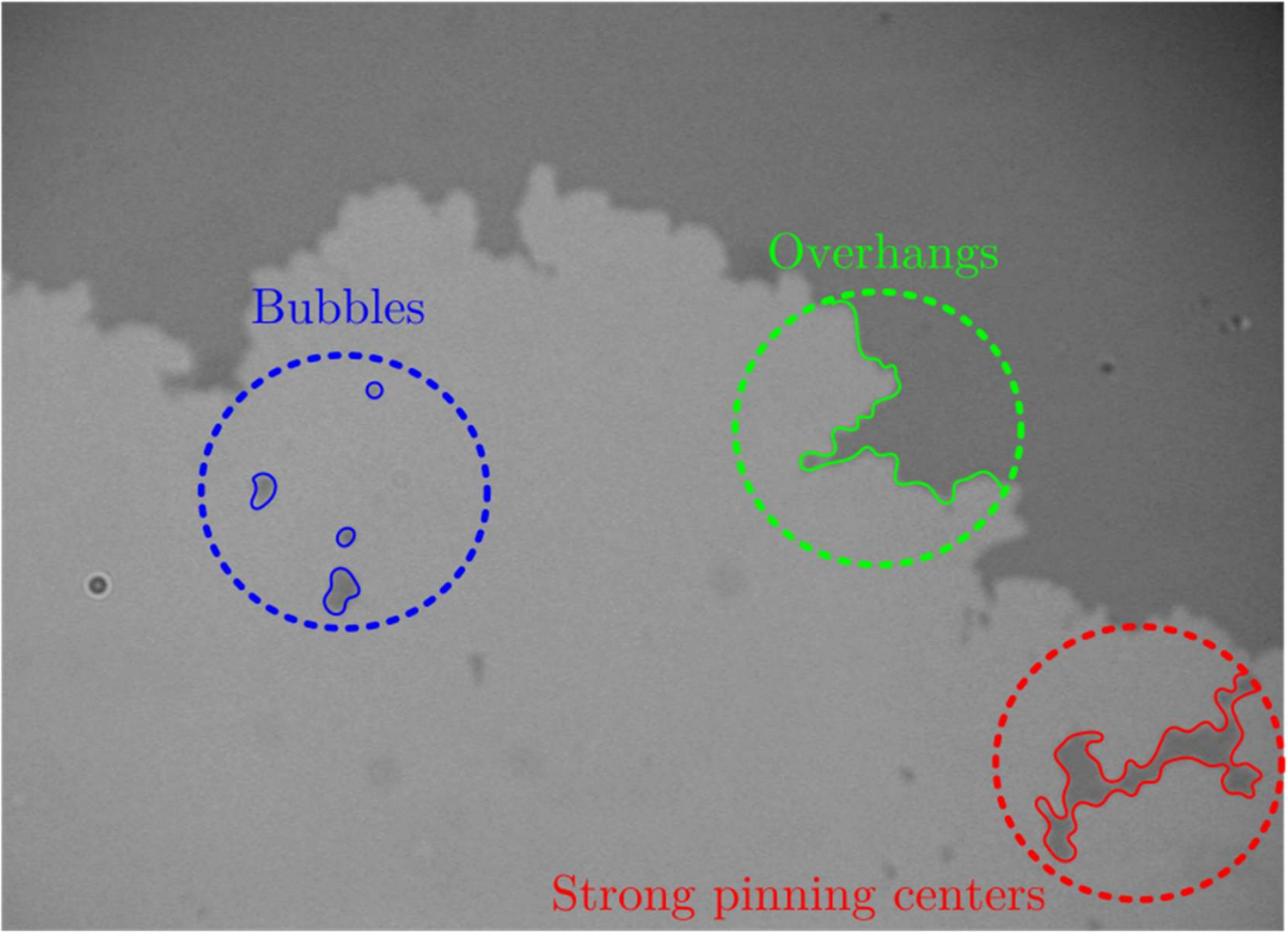


Bubbles



Bubbles

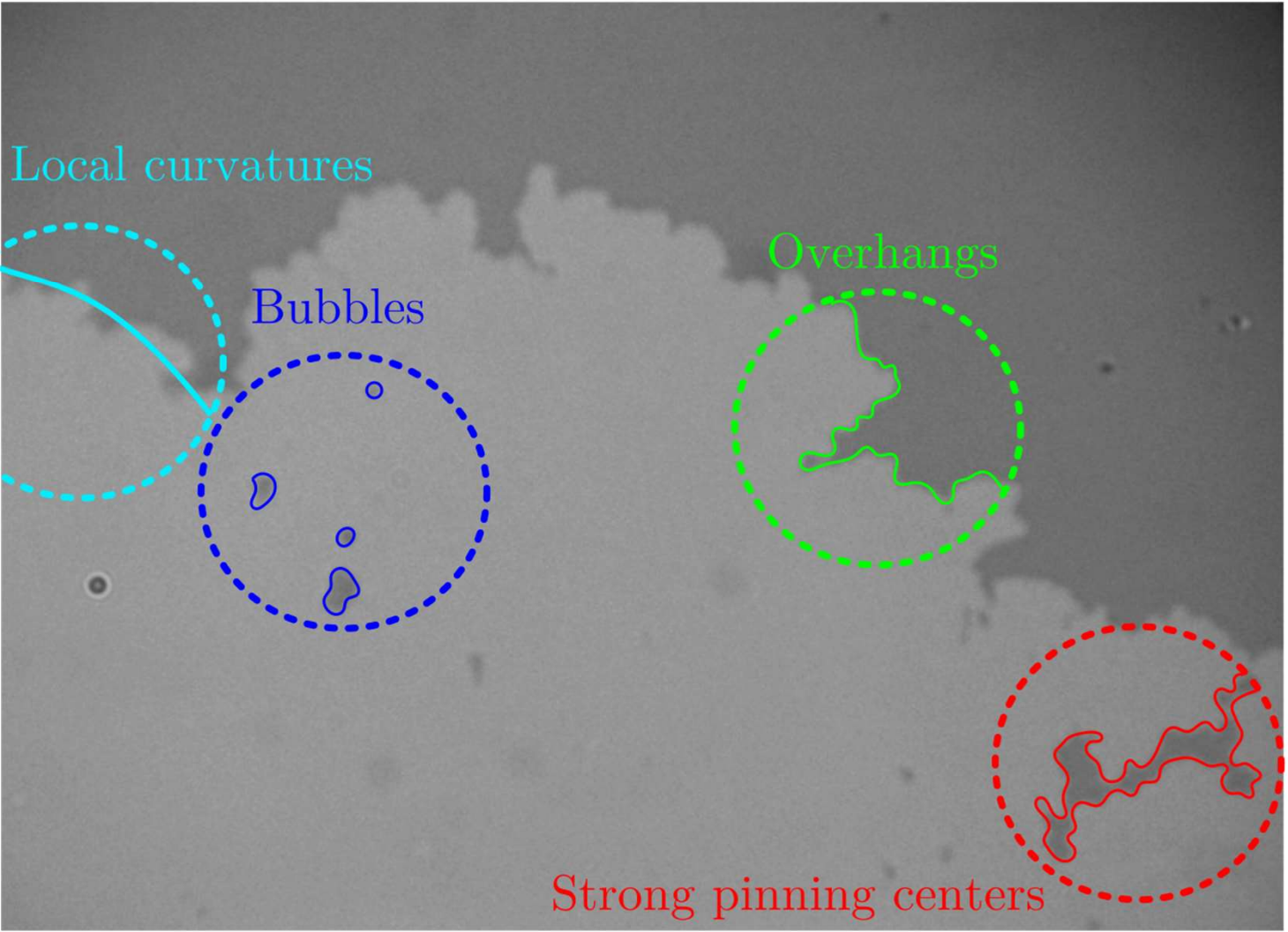
Overhangs



Bubbles

Overhangs

Strong pinning centers



Local curvatures

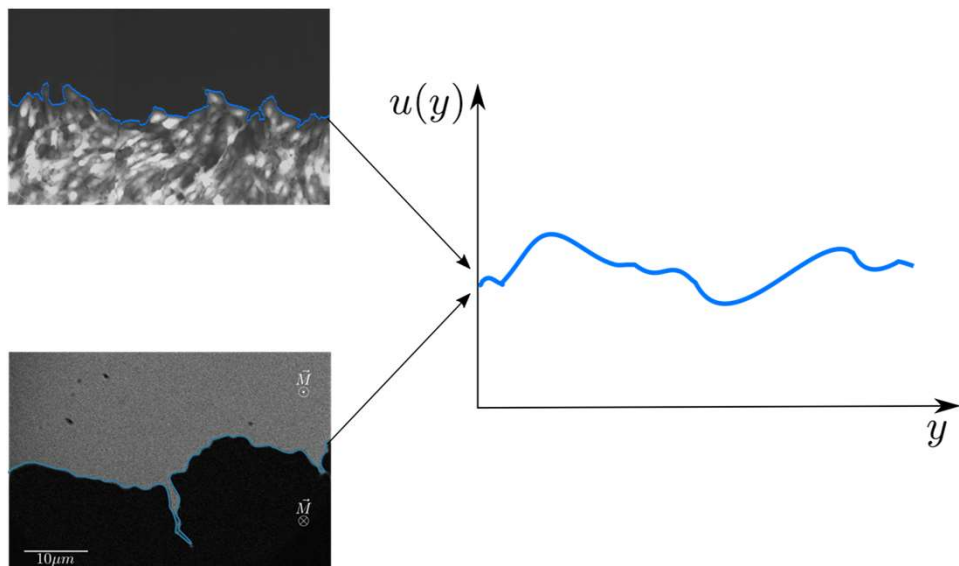
Bubbles

Overhangs

Strong pinning centers

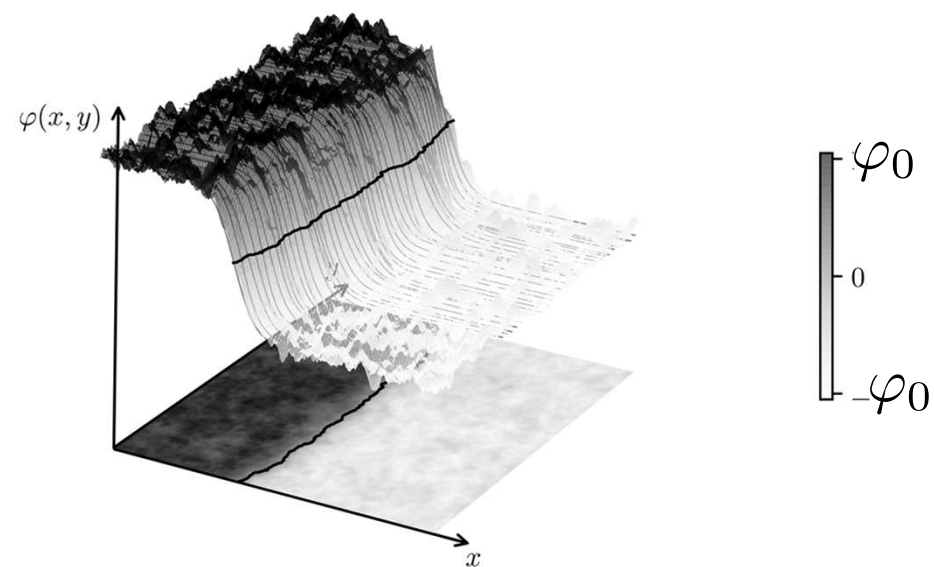
Interface
position

$$u(y)$$



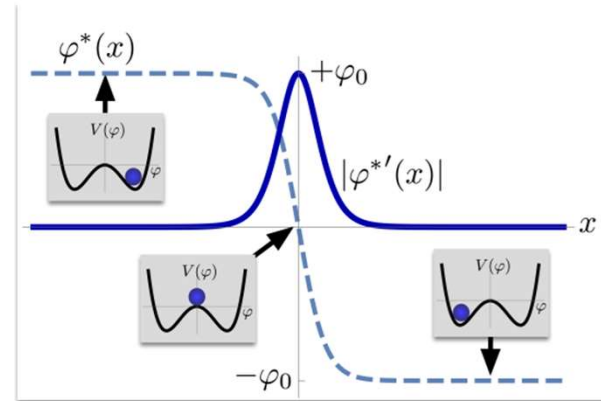
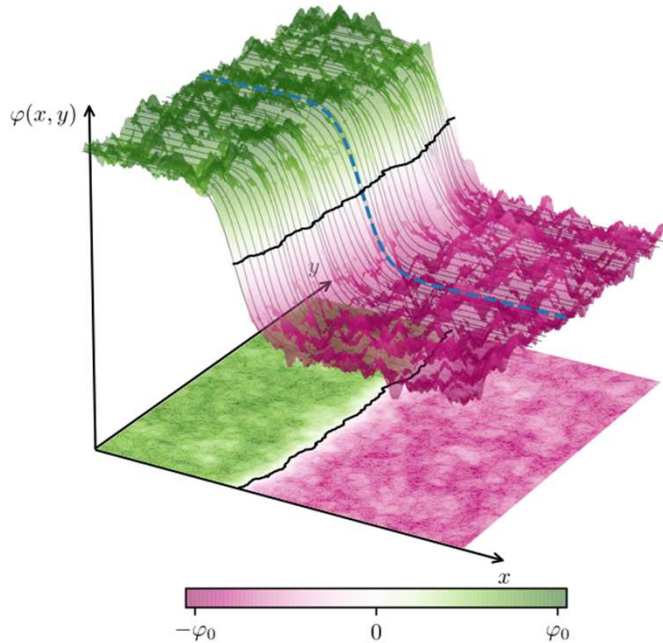
System
state

$$\varphi(x, y)$$



Tools to study interfaces

Ginzburg-Landau approach



$$\mathcal{H}_{\text{GL}}[\varphi] = \int d\vec{r} \frac{\gamma}{2} |\nabla_{\vec{r}} \varphi|^2 + V(\varphi) - h\varphi$$

$$V(\varphi) = -\frac{\alpha}{2} \varphi^2 + \frac{\delta}{4} \varphi^4$$

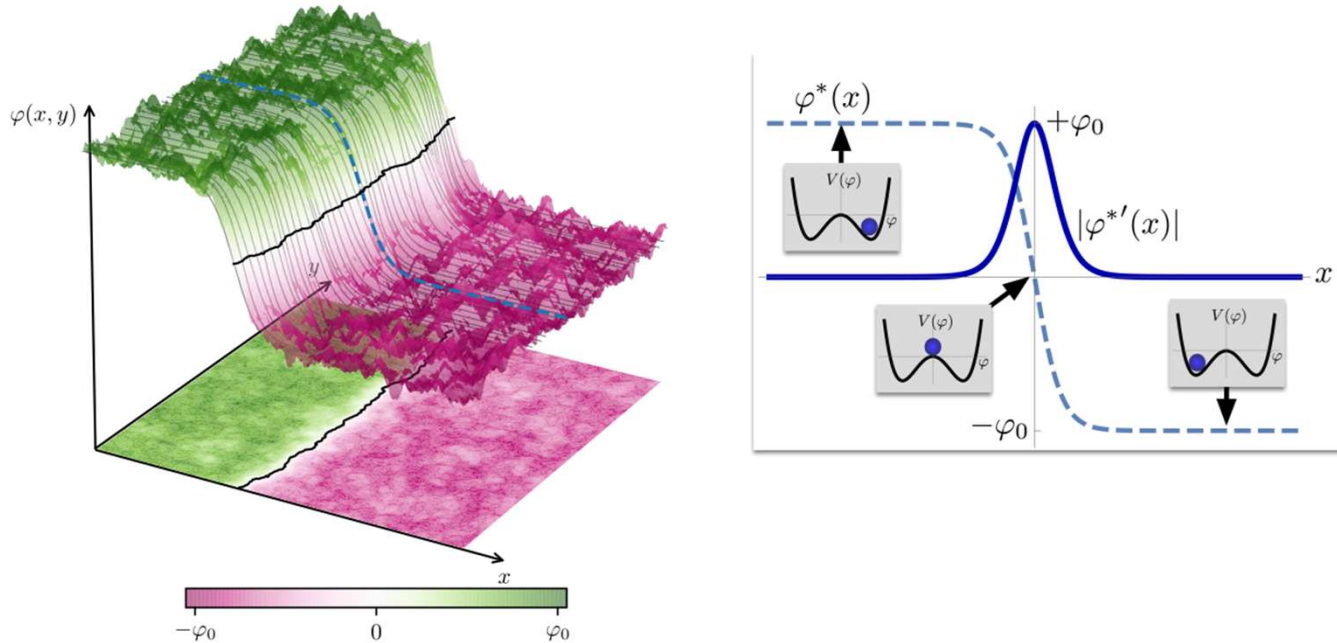
NC, E. Ferrero, A. Kolton, J. Curiale, V. Jeudy, S. Bustingorry, *Magnetic domain wall creep and depinning: A scalar field model approach*. PRE (2018)

NC, E. Agoritsas, V. Lecomte, T. Giamarchi, *From bulk descriptions to emergent interfaces: Connecting the Ginzburg-Landau and elastic-line models*. PRB (2020)

NC. *Degradation of domains with sequential field application*. JSTAT (2021)

Tools to study interfaces

Ginzburg-Landau approach



$$\eta \partial_t \varphi = - \frac{\delta \mathcal{H}_{GL}[\varphi]}{\delta \varphi} + \xi$$

$$\langle \xi(\vec{r}_1, t_1) \xi(\vec{r}_2, t_2) \rangle = 2\eta T \delta^2(\vec{r}_2 - \vec{r}_1) \delta(t_2 - t_1)$$

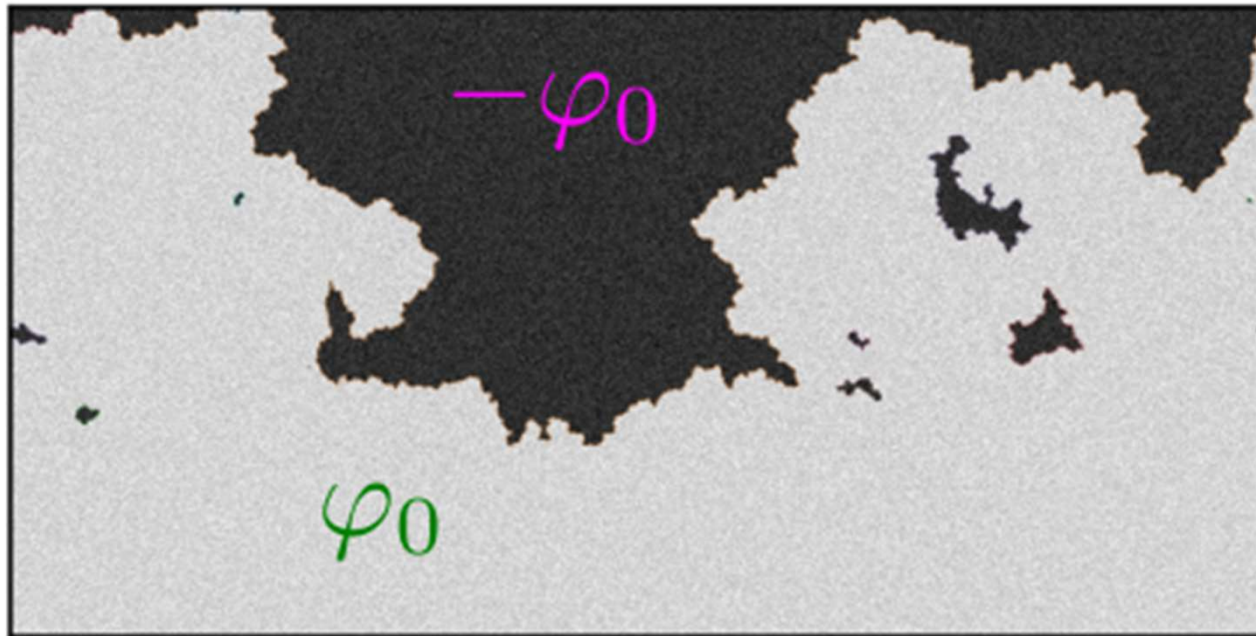
NC, E. Ferrero, A. Kolton, J. Curiale, V. Jeudy, S. Bustingorry, *Magnetic domain wall creep and depinning: A scalar field model approach*. PRE (2018)

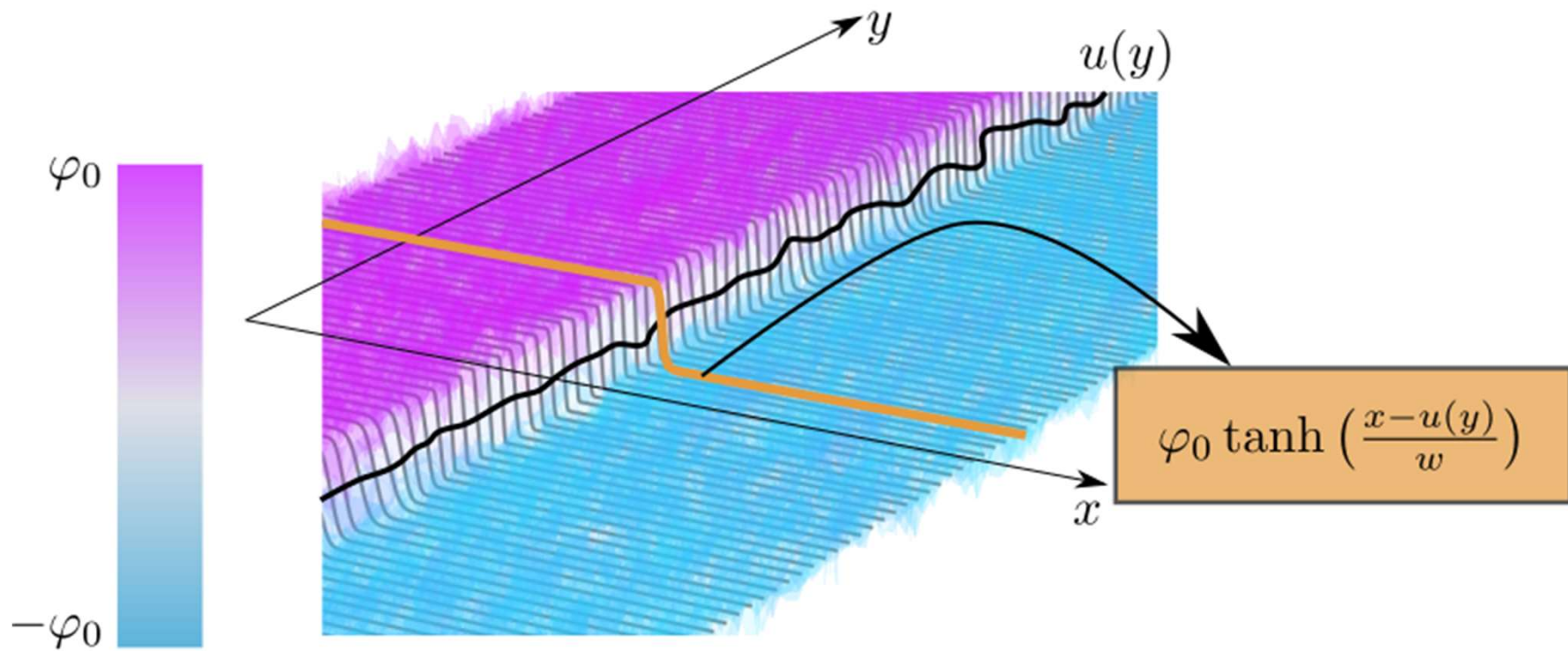
NC, E. Agoritsas, V. Lecomte, T. Giamarchi, *From bulk descriptions to emergent interfaces: Connecting the Ginzburg-Landau and elastic-line models*. PRB (2020)

NC. *Degradation of domains with sequential field application*. JSTAT (2021)

Tools to study interfaces

Domains obtained with a Ginzburg-Landau approach

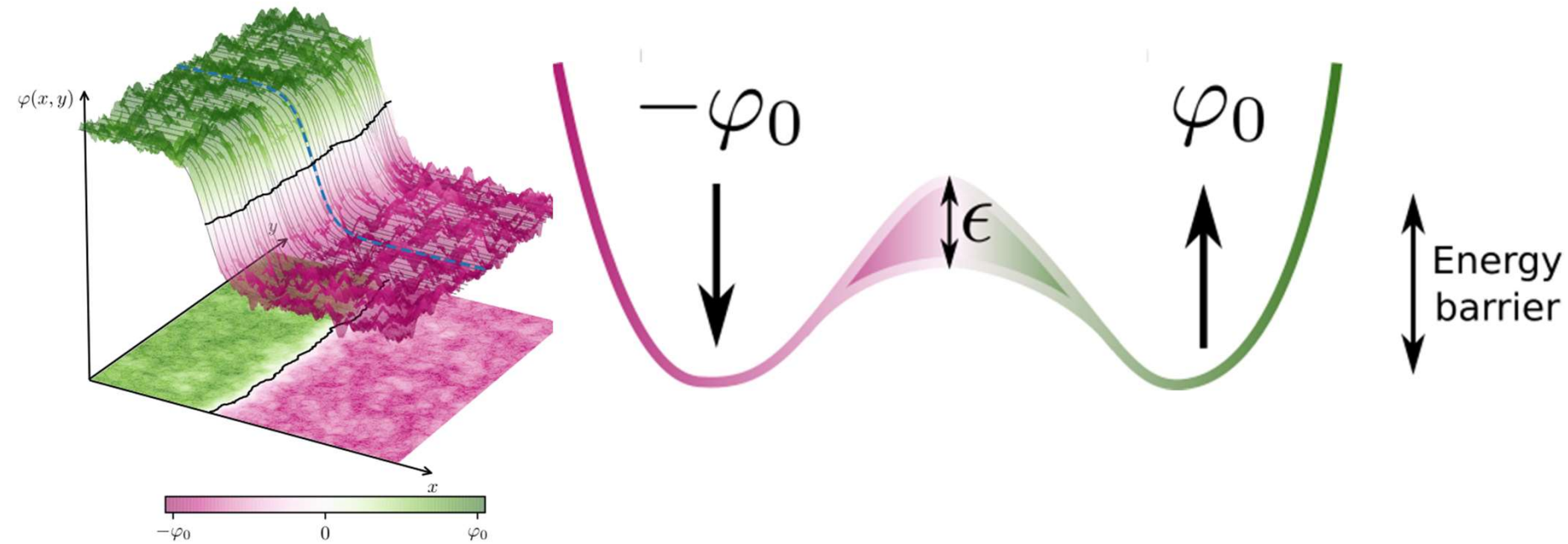




The most probable configuration is the one which minimizes the energy:

$$\frac{\delta \mathcal{H}}{\delta \varphi} = 0 \rightarrow \varphi^* = \varphi_0 \tanh\left(\frac{x - x_0}{w}\right) \quad \varphi_0 = \sqrt{\frac{\alpha}{\delta}} \quad w = \sqrt{\frac{2\gamma}{\alpha}}$$

Disordered Ginzburg-Landau model

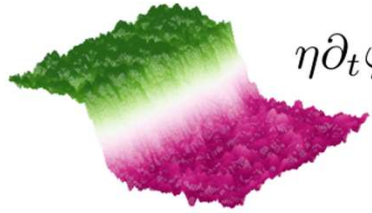


$$V_{\zeta}(\varphi(\vec{r})) = V(\varphi(\vec{r}))(1 + \epsilon\zeta(\vec{r}))$$

$$\langle \zeta(\vec{r}_i)\zeta(\vec{r}_j) \rangle = \delta^2(\vec{r}_i - \vec{r}_j)$$

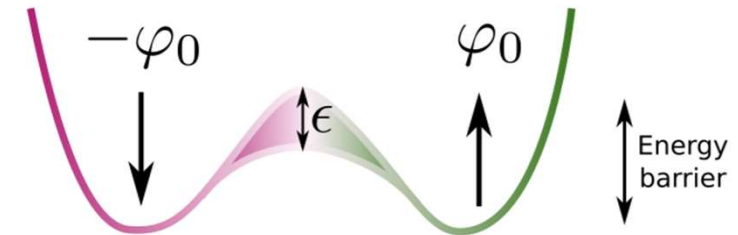
Ginzburg-Landau

State: φ



disorder

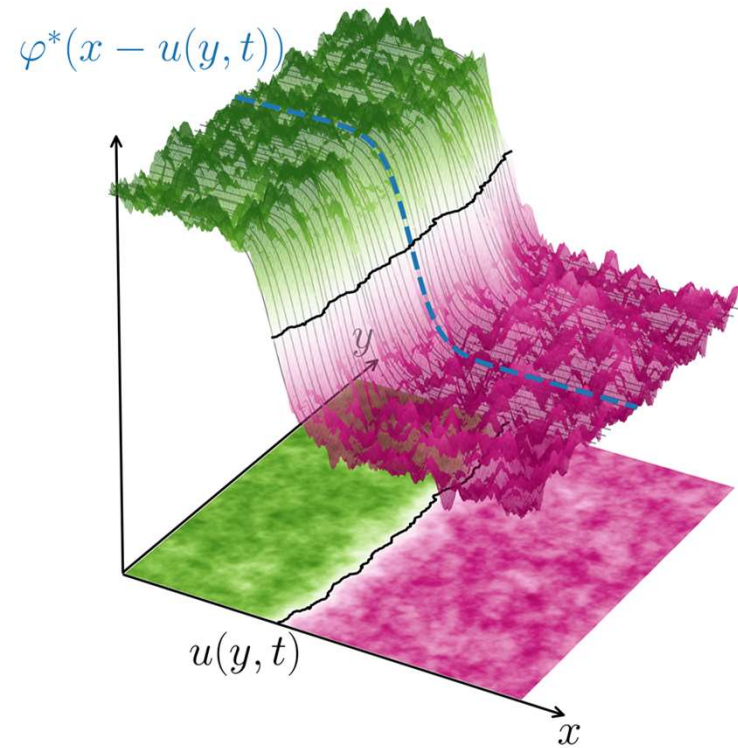
$$\eta \partial_t \varphi = \gamma \nabla^2 \varphi - (1 + \epsilon \zeta(\vec{r})) V'(\varphi) + h + \xi(\vec{r}, t)$$



We use an ansatz

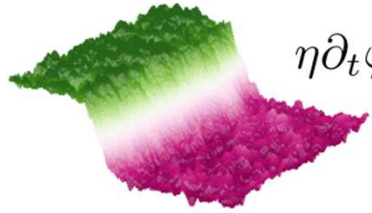
$$\varphi(x, y, t) = \varphi^*(x - u(y, t))$$

$$-\frac{\delta \mathcal{H}_{GL}[\varphi]}{\delta \varphi} \Big|_{\varphi^*} = \gamma \varphi^{*''} - V'(\varphi^*) = 0$$



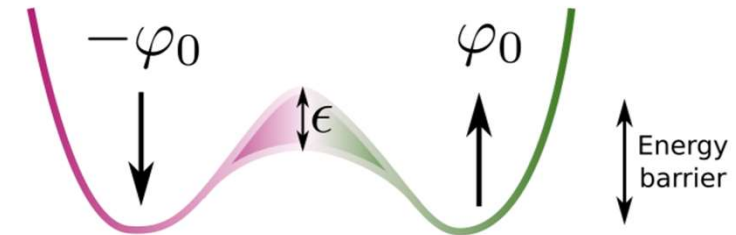
Ginzburg-Landau

State: φ



disorder

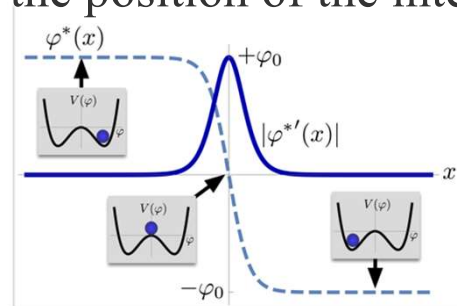
$$\eta \partial_t \varphi = \gamma \nabla^2 \varphi - (1 + \epsilon \zeta(\vec{r})) V'(\varphi) + h + \xi(\vec{r}, t)$$



1) By using our ansatz, the Langevin equation becomes

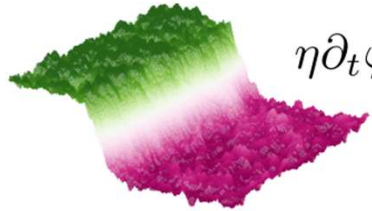
$$-\eta \varphi^{*'} \partial_t u = \gamma \left(\varphi^{*''} (\partial_y u)^2 - \varphi^{*'} \partial_y^2 u \right) - \epsilon \zeta(x, y) V'(\varphi^*) + \xi(x, y, t)$$

2) We “localize” the equation around the position of the interface by multiplying by $\varphi^{*'}$



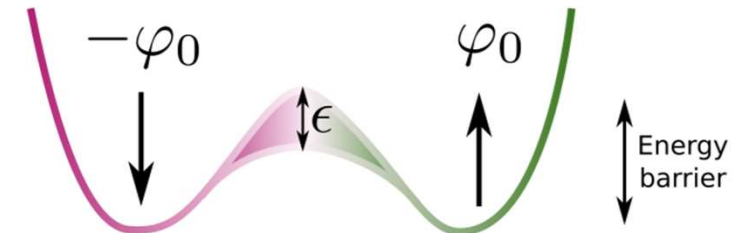
Ginzburg-Landau

State: φ



disorder

$$\eta \partial_t \varphi = \gamma \nabla^2 \varphi - (1 + \epsilon \zeta(\vec{r})) V'(\varphi) + h + \xi(\vec{r}, t)$$



1) By using our ansatz, the Langevin equation becomes

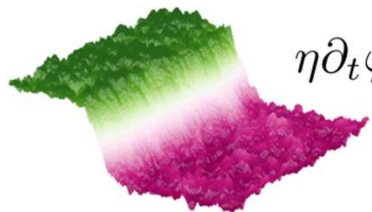
$$-\eta \varphi^{*'} \partial_t u = \gamma \left(\varphi^{*''} (\partial_y u)^2 - \varphi^{*'} \partial_y^2 u \right) - \epsilon \zeta(x, y) V'(\varphi^*) + \xi(x, y, t)$$

2) We “localize” the equation around the position of the interface by multiplying by $\varphi^{*'}$

3) We integrate x over the whole space

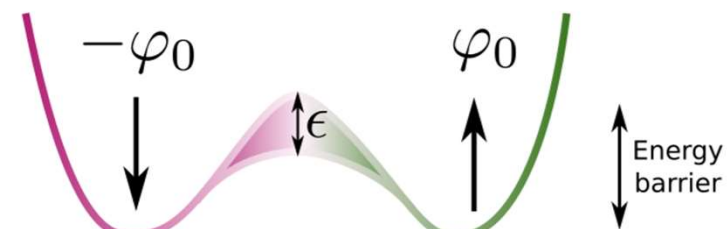
Ginzburg-Landau

State: φ



disorder

$$\eta \partial_t \varphi = \gamma \nabla^2 \varphi - (1 + \epsilon \zeta(\vec{r})) V'(\varphi) + h + \xi(\vec{r}, t)$$



Quantitative system reduction

quenched Edwards-Wilkinson

Interface: u

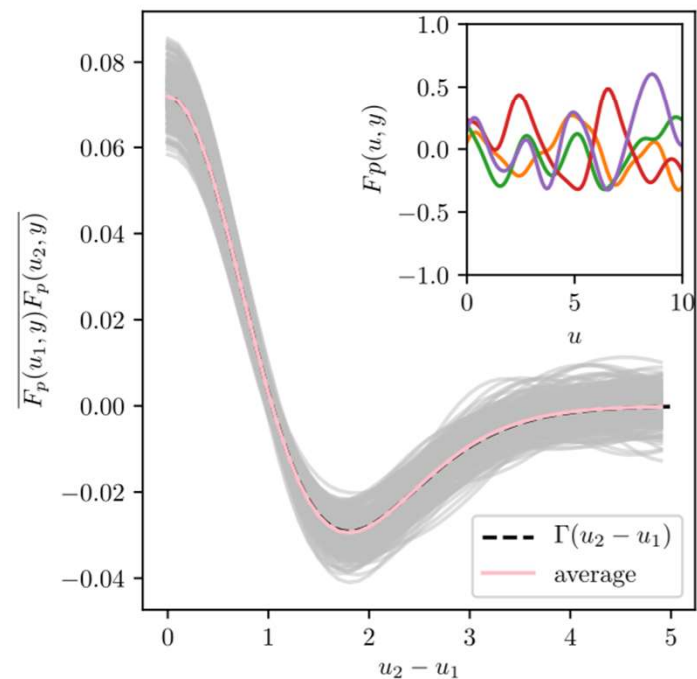


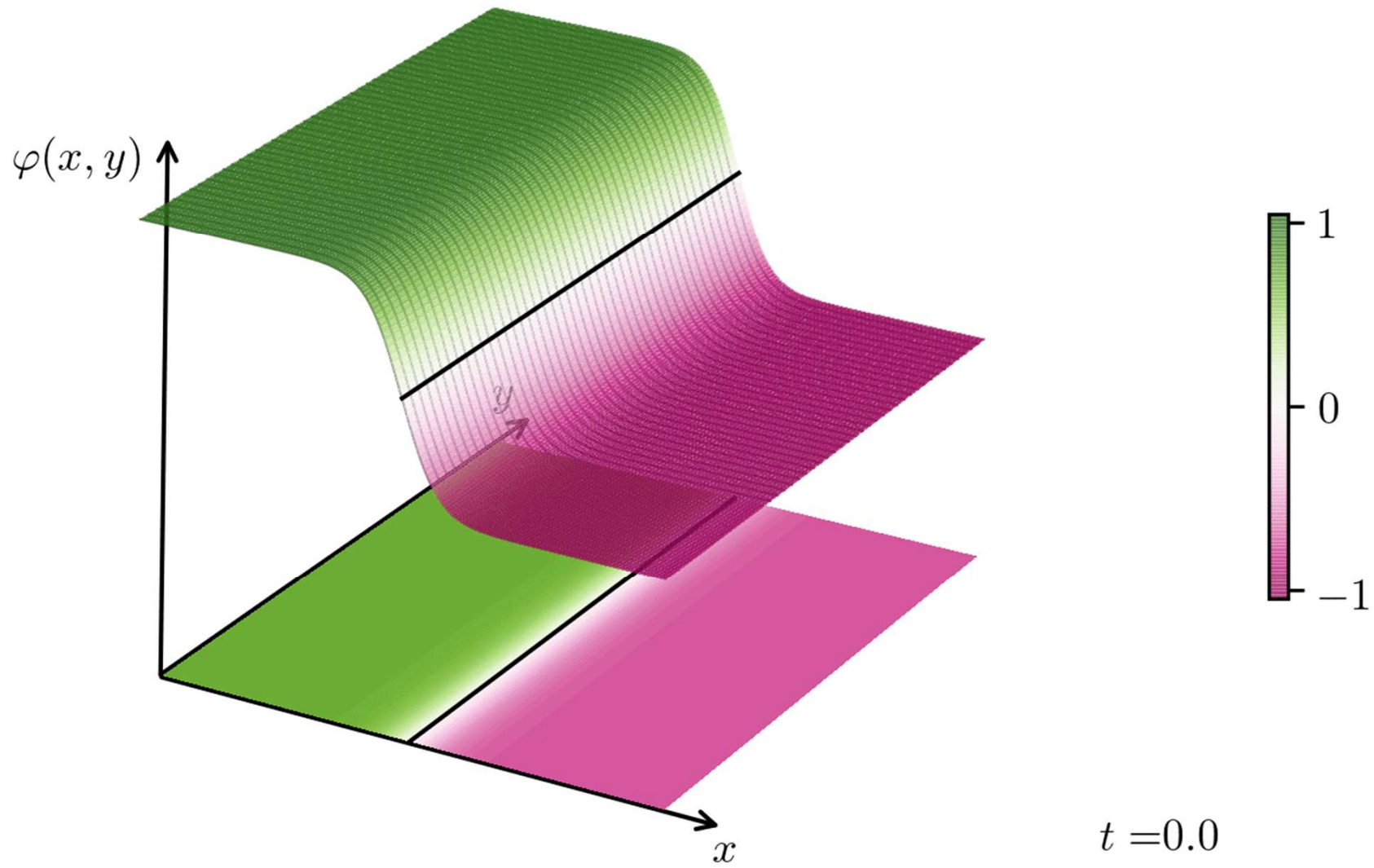
disorder

$$\tilde{\eta} \partial_t u = c \partial_y^2 u + F_p(u(y, t), y) + F + \tilde{\xi}(y, t)$$

$$\overline{F_p(u_1, y_1) F_p(u_2, y_2)} = \epsilon^2 \delta(y_1 - y_2) \Gamma(u_2 - u_1)$$

$$\Gamma(u) = \gamma^2 \int_{-\infty}^{\infty} dx (\varphi^{*'} \varphi^{*''})(x) (\varphi^{*'} \varphi^{*''})(x - u)$$





Evolution from an initially flat configuration with equivalent parameters

Edwards-Wilkinson

One solves for $u(y, t)$

With parameters

$$\tilde{\eta} = \eta \mathcal{N}(\alpha, \delta, \gamma)$$

$$c = \gamma \mathcal{N}(\alpha, \delta, \gamma)$$

$$F_p(\varepsilon, \alpha, \delta, \gamma)$$

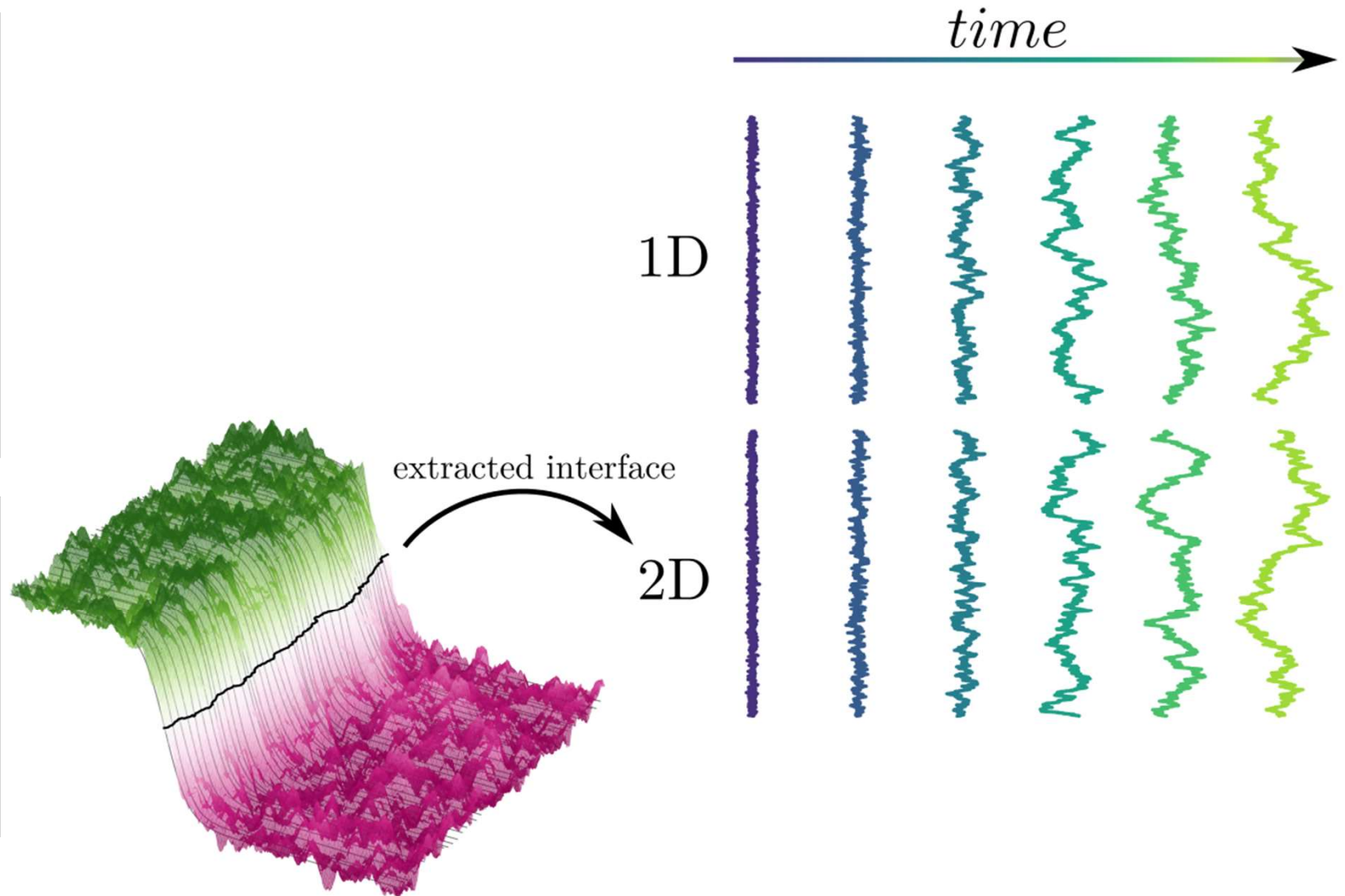
T

Ginzburg-Landau

One solves for $\varphi(x, y, t)$

With parameters

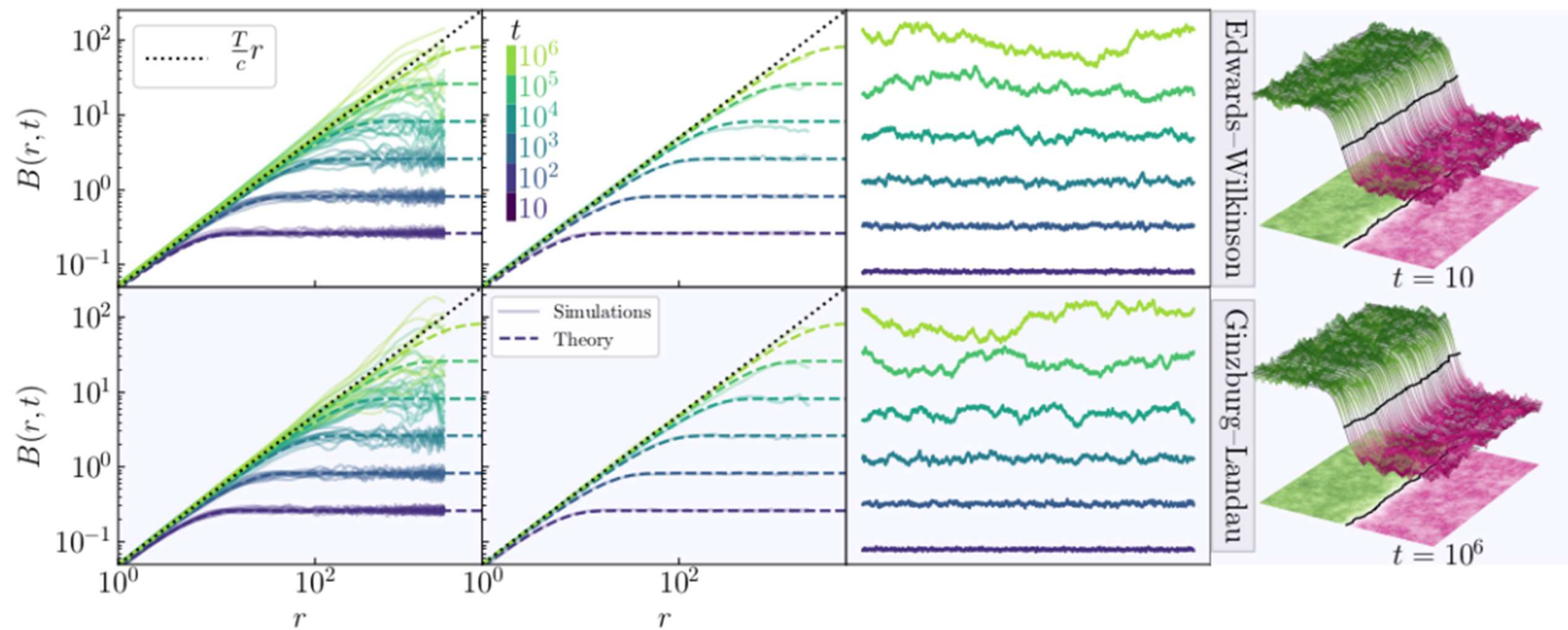
$$\eta, \alpha, \delta, \gamma, T, \varepsilon$$



Evolution from an initially flat configuration

Clean systems: Roughness at different evolution times

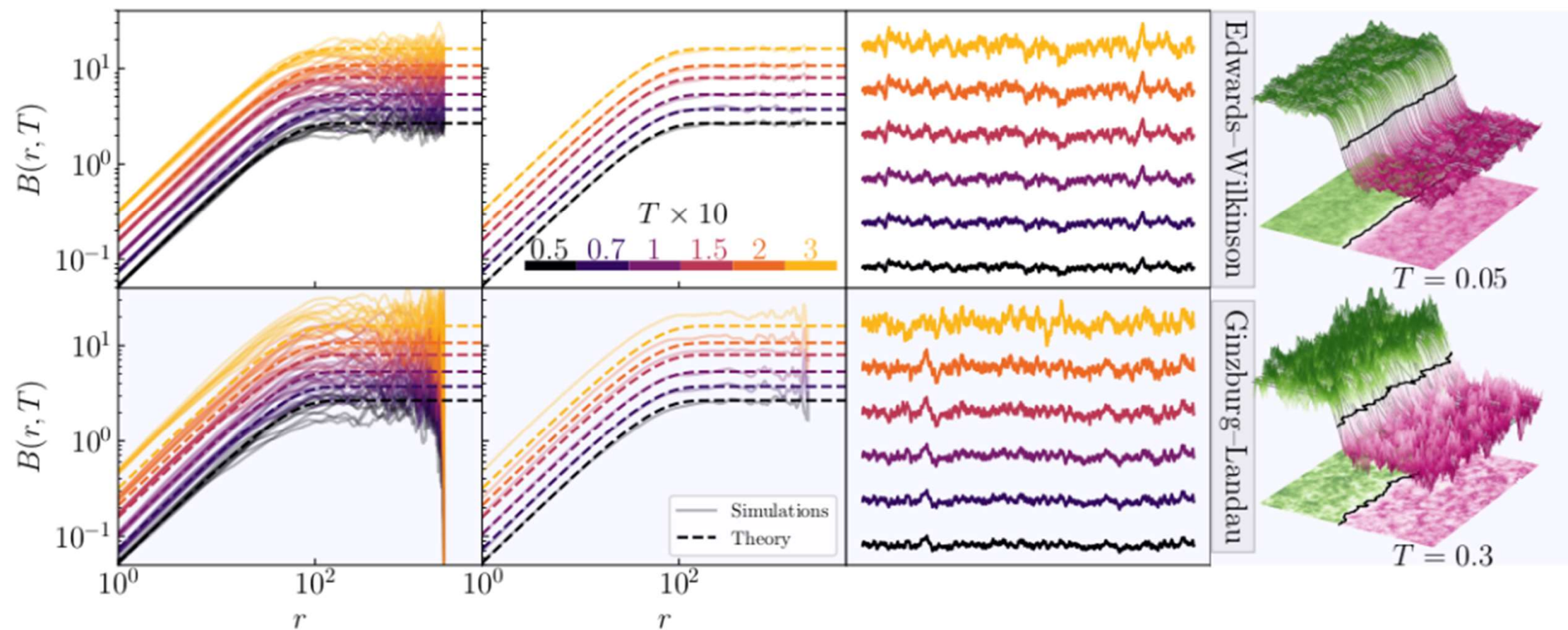
$$F = 0$$



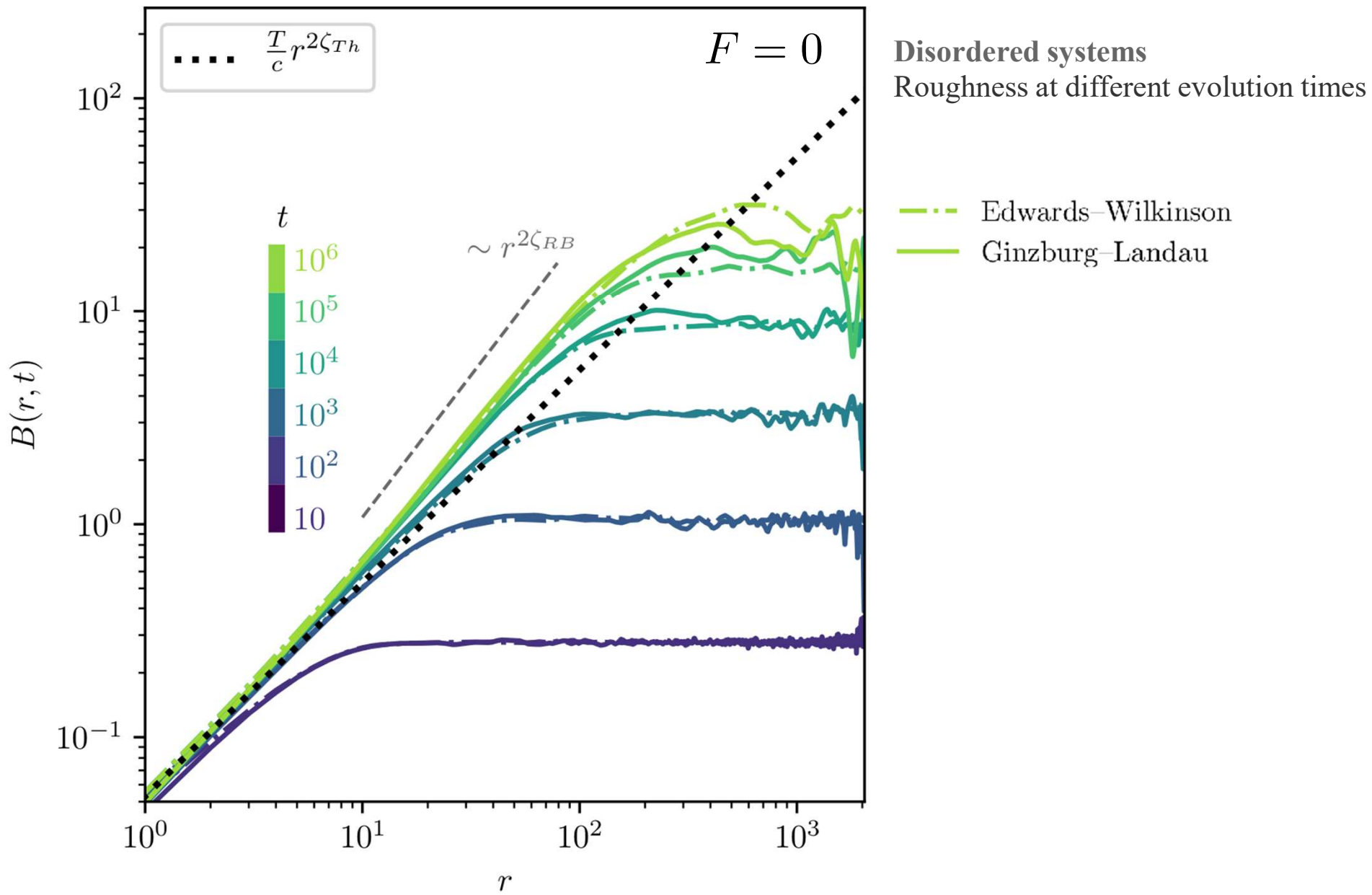
Evolution from an initially flat configuration

Clean systems: Roughness at different temperatures

$$F = 0$$

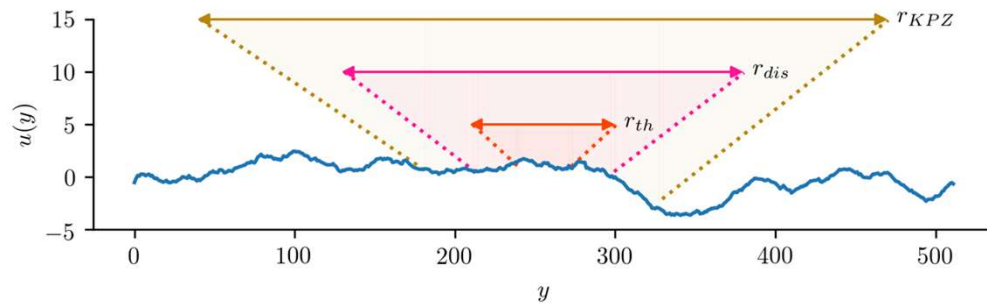


$$T \ll T^* = \frac{\alpha}{\delta} \gamma$$



Microscopic interplay of temperature and disorder in an interface

Interfaces' fluctuating shape reveal the systems' microscopic physics



Roughness

$$B(r) = \overline{[u(y+r) - u(y)]^2}$$

Microscopic interplay of temperature and disorder in an interface

Quenched Edwards-Wilkinson equation

$$\eta \partial_t u(y, t) = c \partial_y^2 u(y, t) + \xi(y, t) + F_p(y, u(y, t))$$

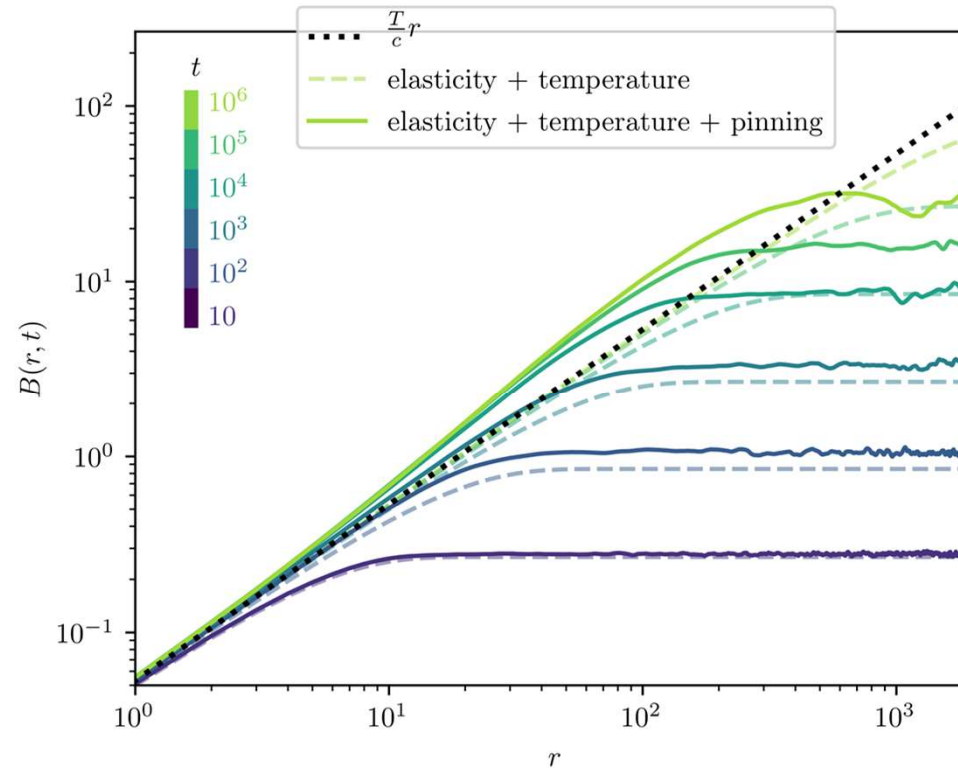
Thermal fluctuations

$$\langle \xi(y_1, t_1) \xi(y_2, t_2) \rangle = 2\eta T \delta(y_2 - y_1) \delta(t_2 - t_1)$$

Pinning force

with short-length correlations

$$\overline{F_p(y_1, u_1) F_p(y_2, u_2)} = \Delta_\xi(u_2 - u_1) \delta(y_2 - y_1)$$



Microscopic interplay of temperature and disorder in an interface

Quenched Edwards-Wilkinson equation

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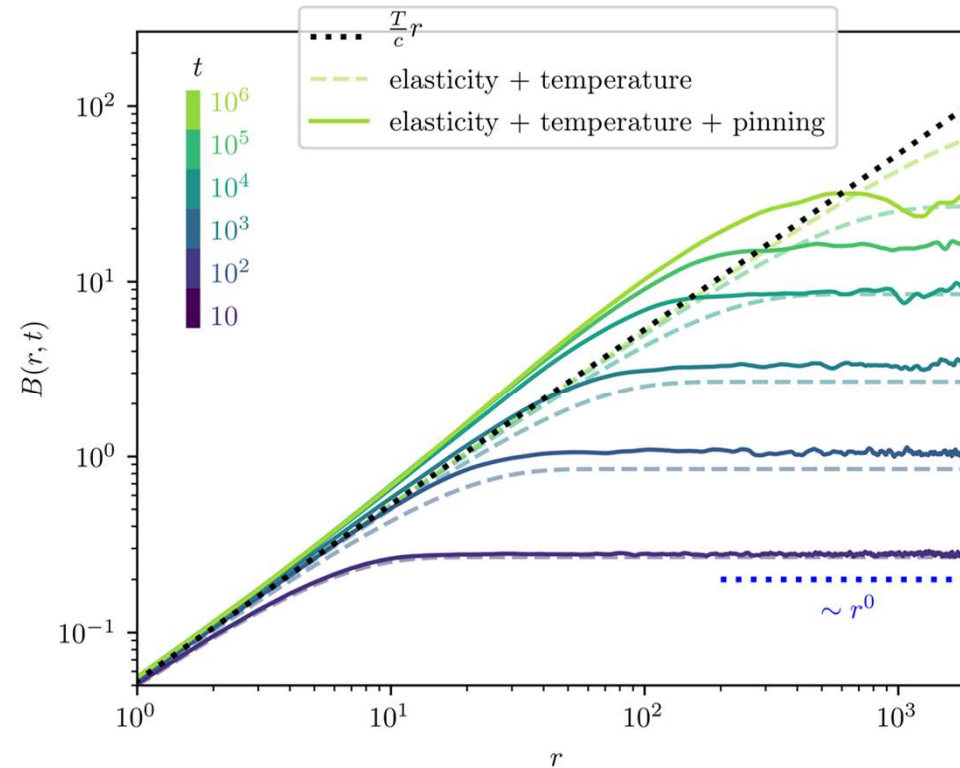
Thermal fluctuations

$$\langle \xi(y_1, t_1) \xi(y_2, t_2) \rangle = 2\eta T \delta(y_2 - y_1) \delta(t_2 - t_1)$$

Pinning force

with short-length correlations

$$\overline{F_p(y_1, u_1) F_p(y_2, u_2)} = \Delta_\xi(u_2 - u_1) \delta(y_2 - y_1)$$



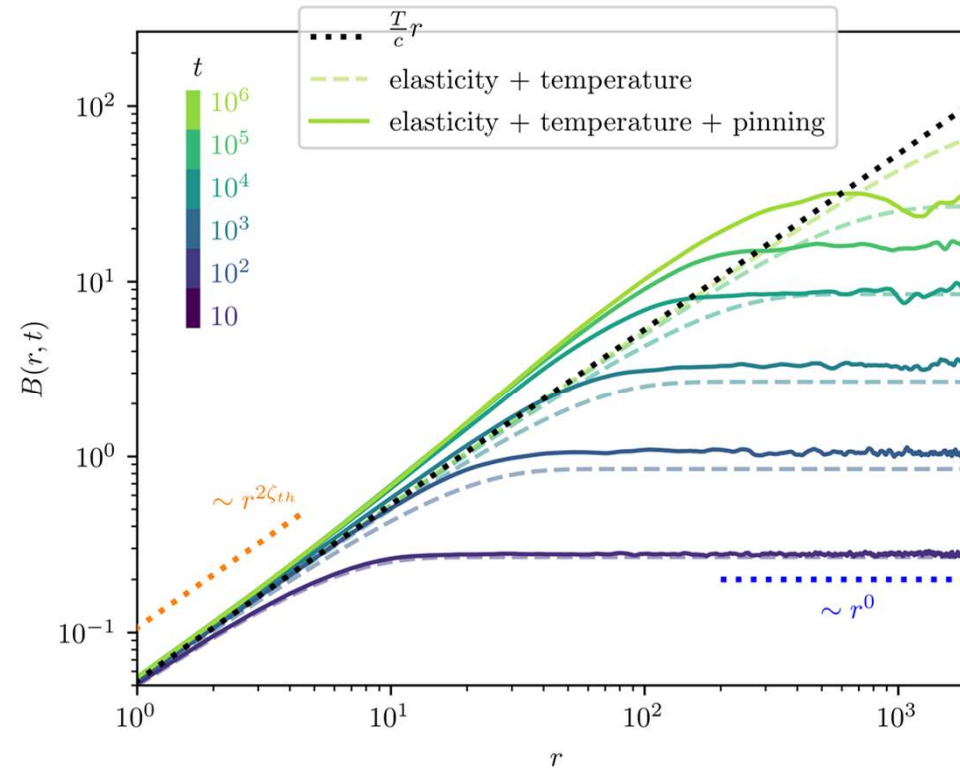
Microscopic interplay of temperature and disorder in an interface

Quenched Edwards-Wilkinson equation

$$\eta \partial_t u(y, t) = c \partial_y^2 u(y, t) + \xi(y, t) + F_p(y, u(y, t))$$

temperature

$$\zeta_{th} = \frac{1}{2}$$



Microscopic interplay of temperature and disorder in an interface

Quenched Edwards-Wilkinson equation

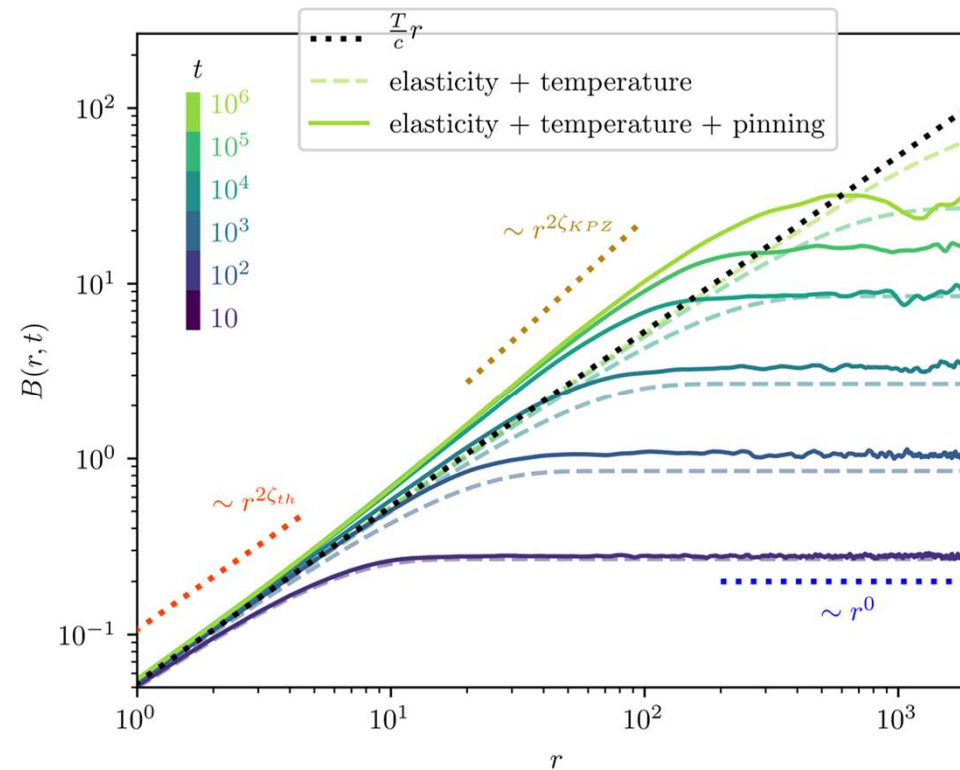
$$\eta \partial_t u(y, t) = c \partial_y^2 u(y, t) + \xi(y, t) + F_p(y, u(y, t))$$

temperature

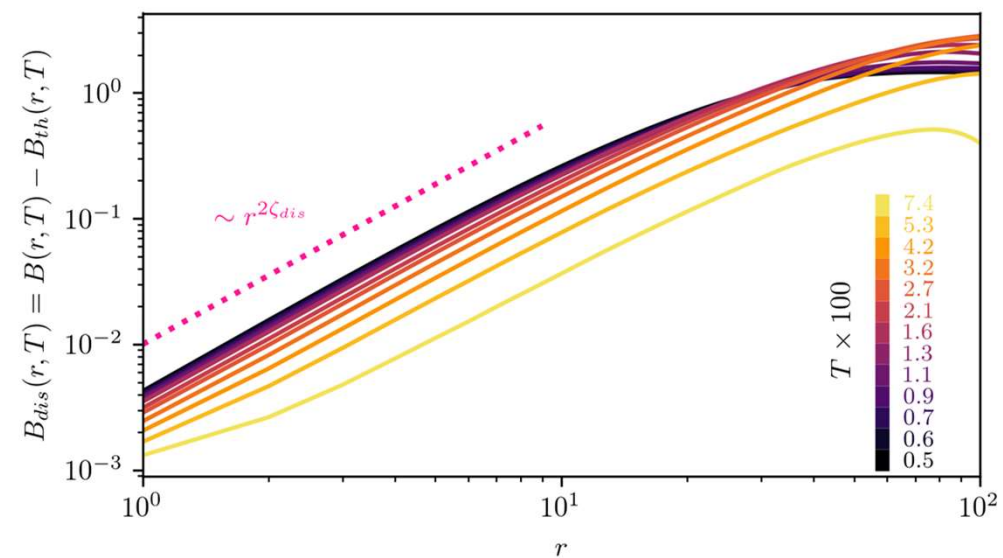
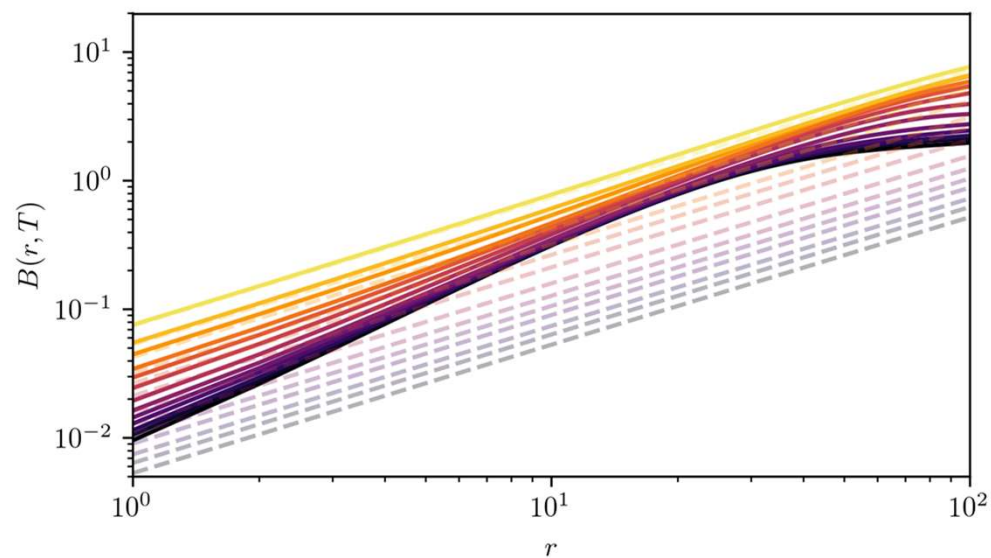
$$\zeta_{th} = \frac{1}{2}$$

disorder

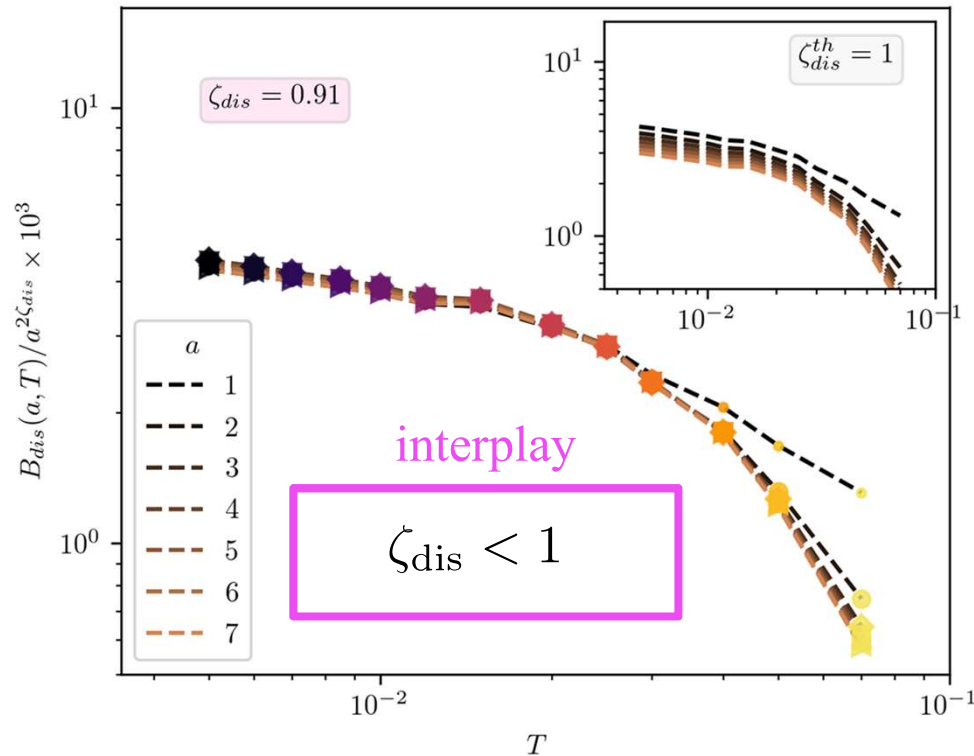
$$\zeta_{KPZ} = \frac{2}{3}$$



Microscopic interplay of temperature and disorder in an interface



Microscopic interplay of temperature and disorder in an interface



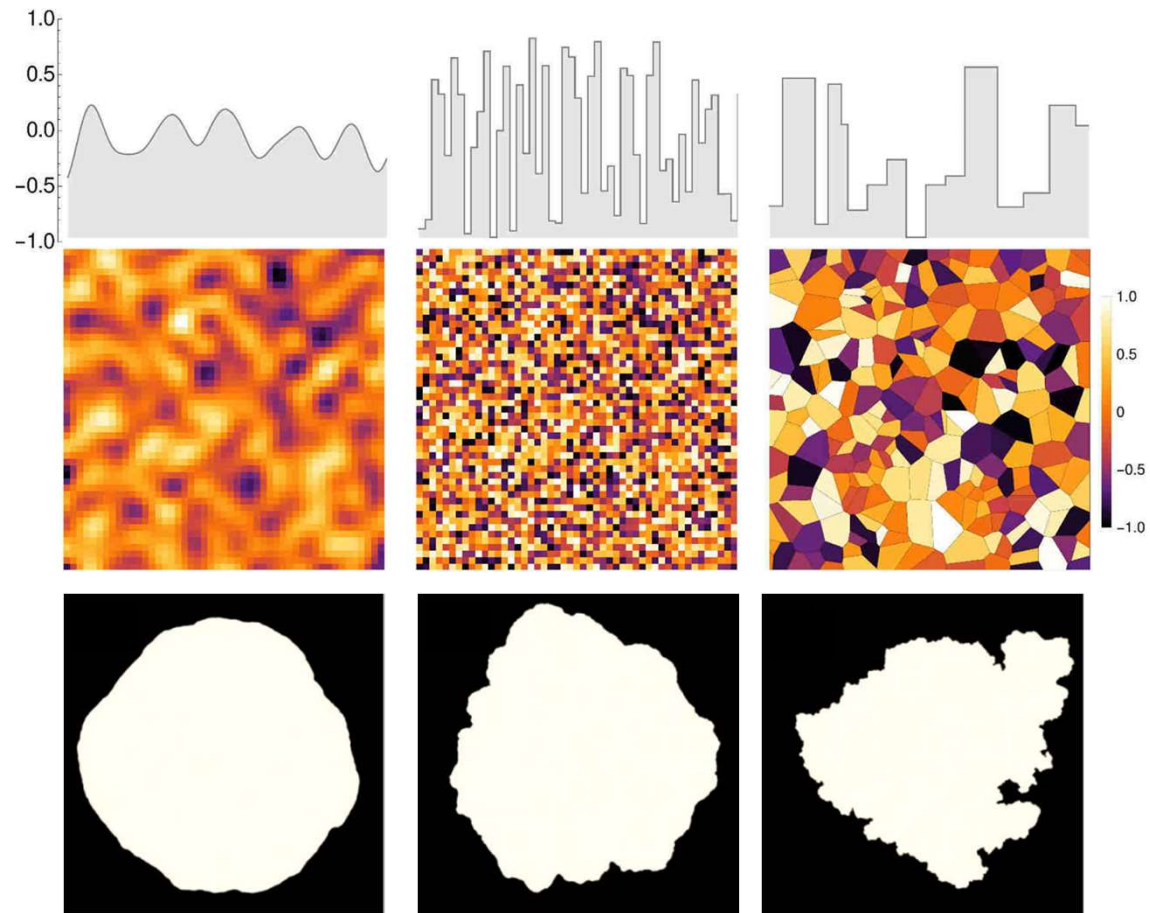
Rescaling arguments:

$$A_{dis}(T) = \frac{B_{dis}(r \leq r_0)}{r^{2\zeta_{dis}}} \propto \frac{\xi^2 T_c^2}{(c\xi^2)^{2\zeta_{dis}}} \left(\frac{f}{T}\right)^{2(1-\zeta_{dis})}$$

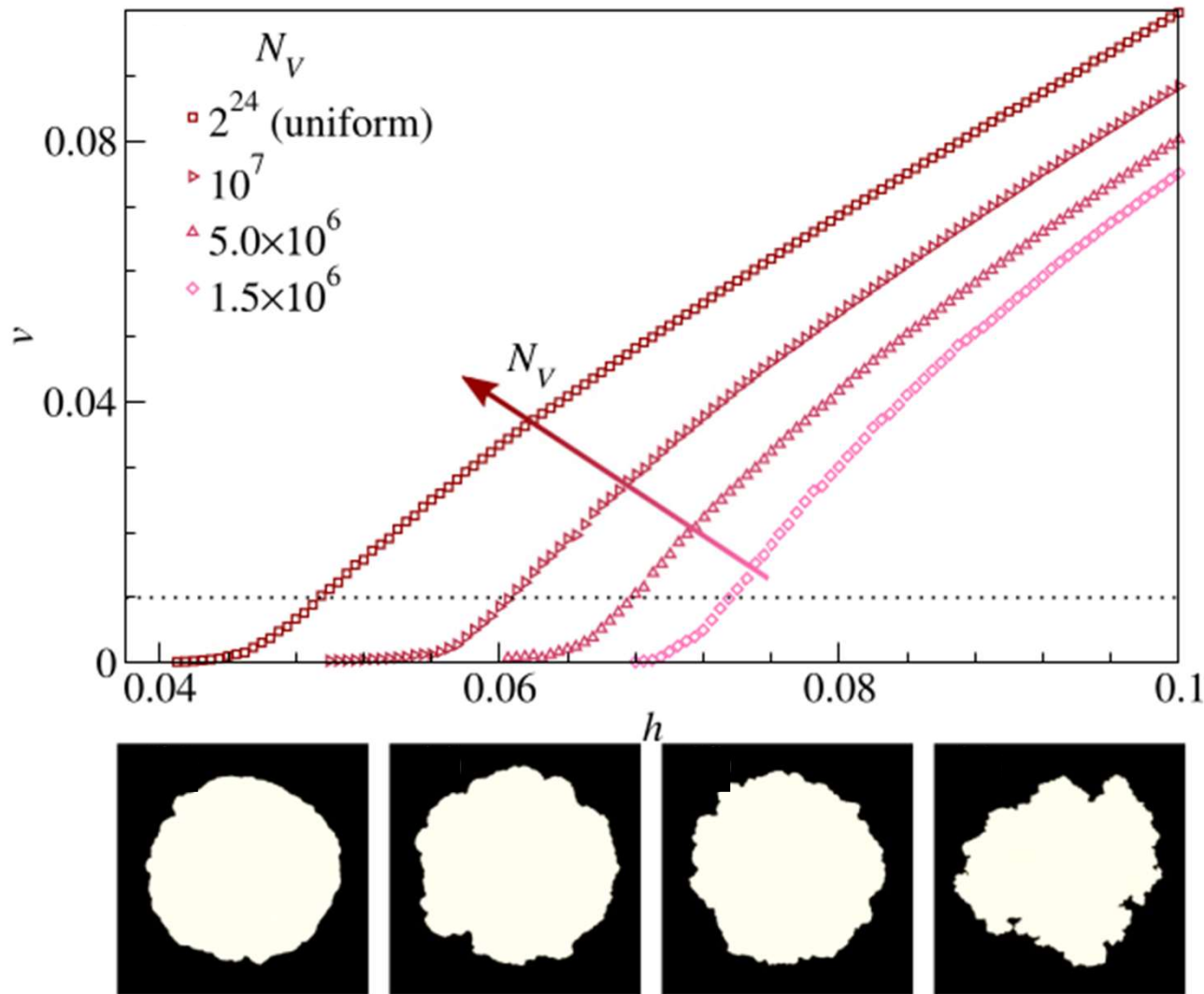
$\zeta_{dis} = 1$ would yield a temperature-independent

We have shown a numerical confirmation of this regime

Versatility of a Ginzburg-Landau approach



Versatility of a Ginzburg-Landau approach



Allows us to emulate typical experimental I

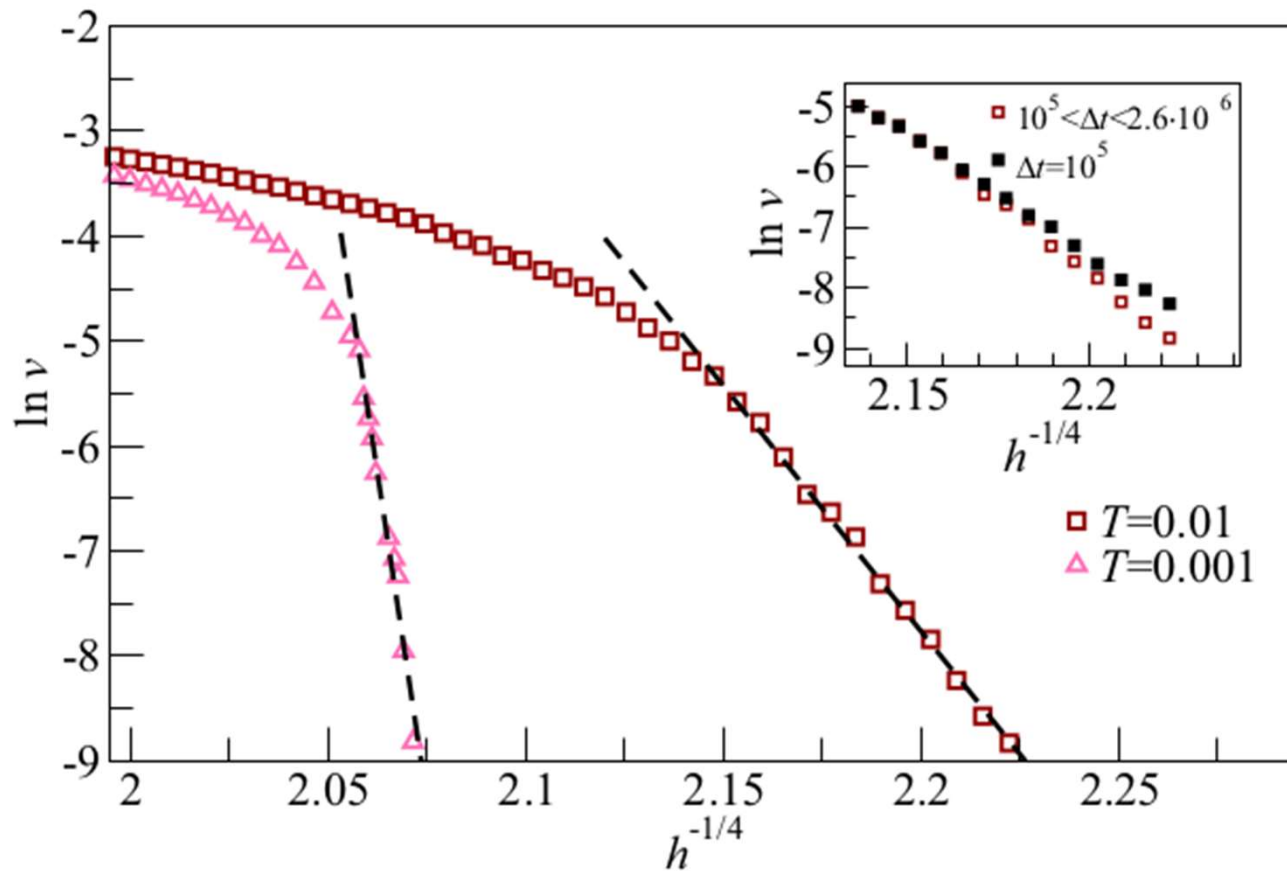
$$\eta \frac{\partial \varphi}{\partial t} = \gamma \nabla^2 \varphi + (D \alpha \varphi + H)(1 - \varphi^2) + \xi$$

$$D = D(\varepsilon, \vec{r}) = (1 + \varepsilon \chi(\vec{r}))$$

$$\langle \chi(\vec{r}_i) \chi(\vec{r}_j) \rangle = \delta^2(\vec{r}_i - \vec{r}_j)$$

Versatility of a Ginzburg-Landau approach

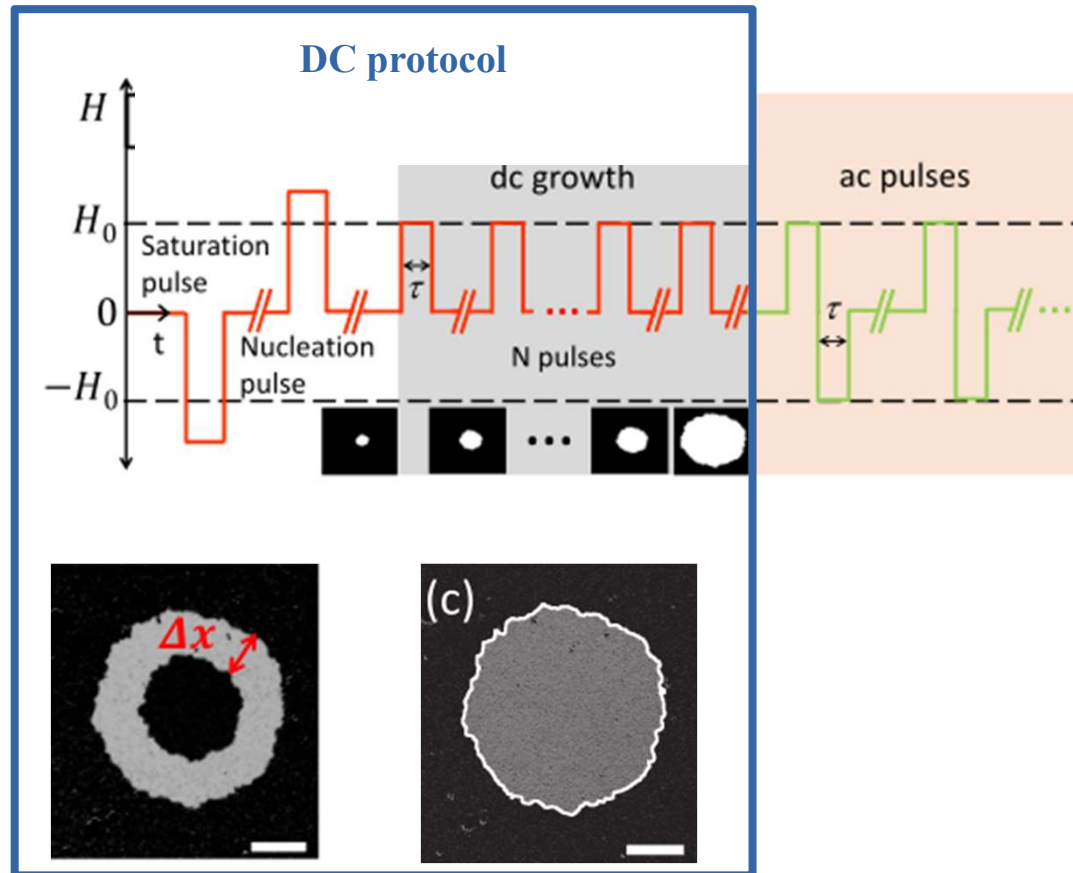
Observation of the creep regime



Applications

Recent experiments revealed complex interface behaviours

Typical PMOKE protocol to estimate domain wall velocities

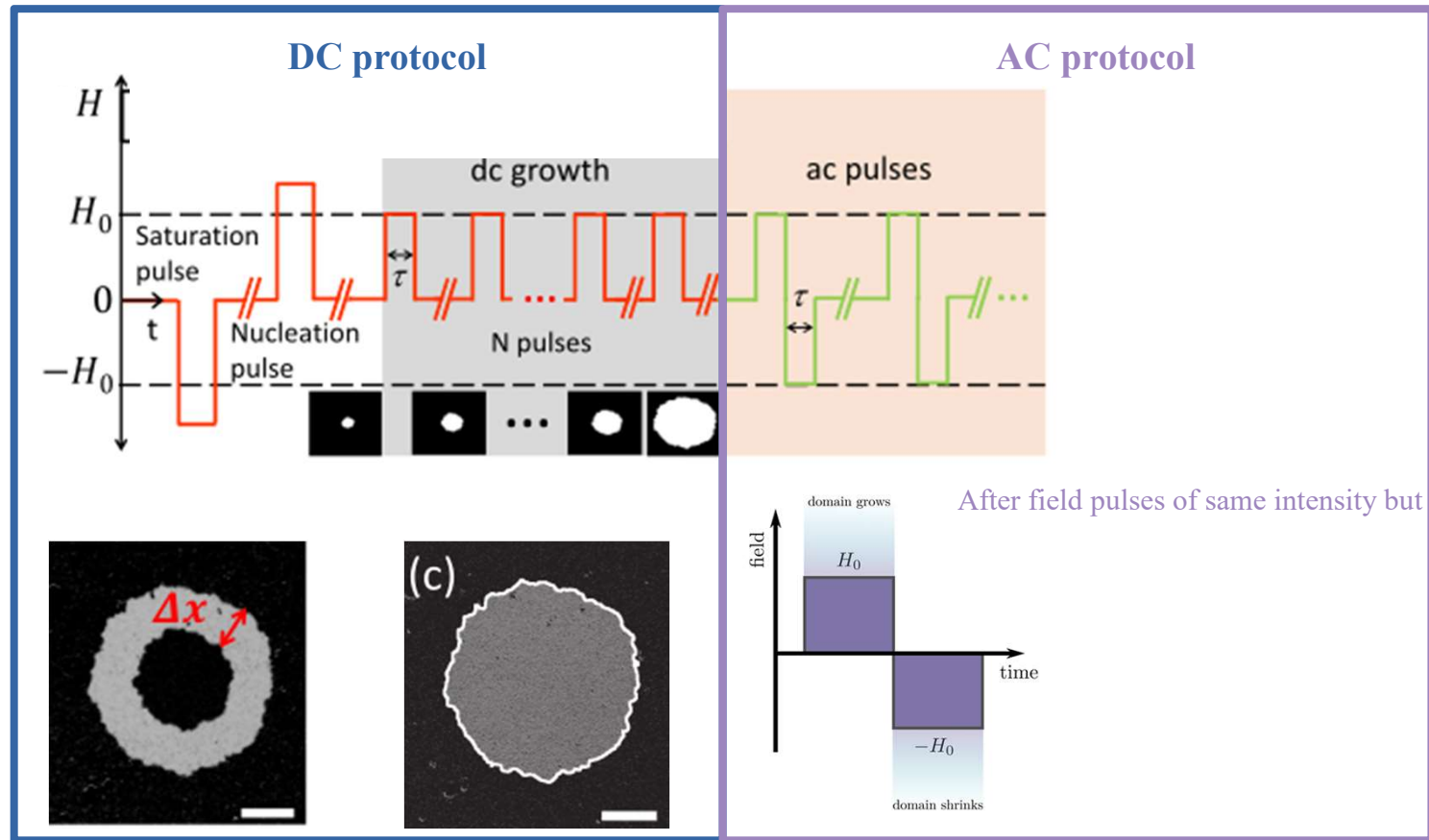


P. Domenichini, et al. *Transient magnetic-domain-wall ac dynamics by means of magneto-optic Kerr effect microscopy*. Highlighted in PRB, 2019.

Applications

Recent experiments revealed complex interface behaviours

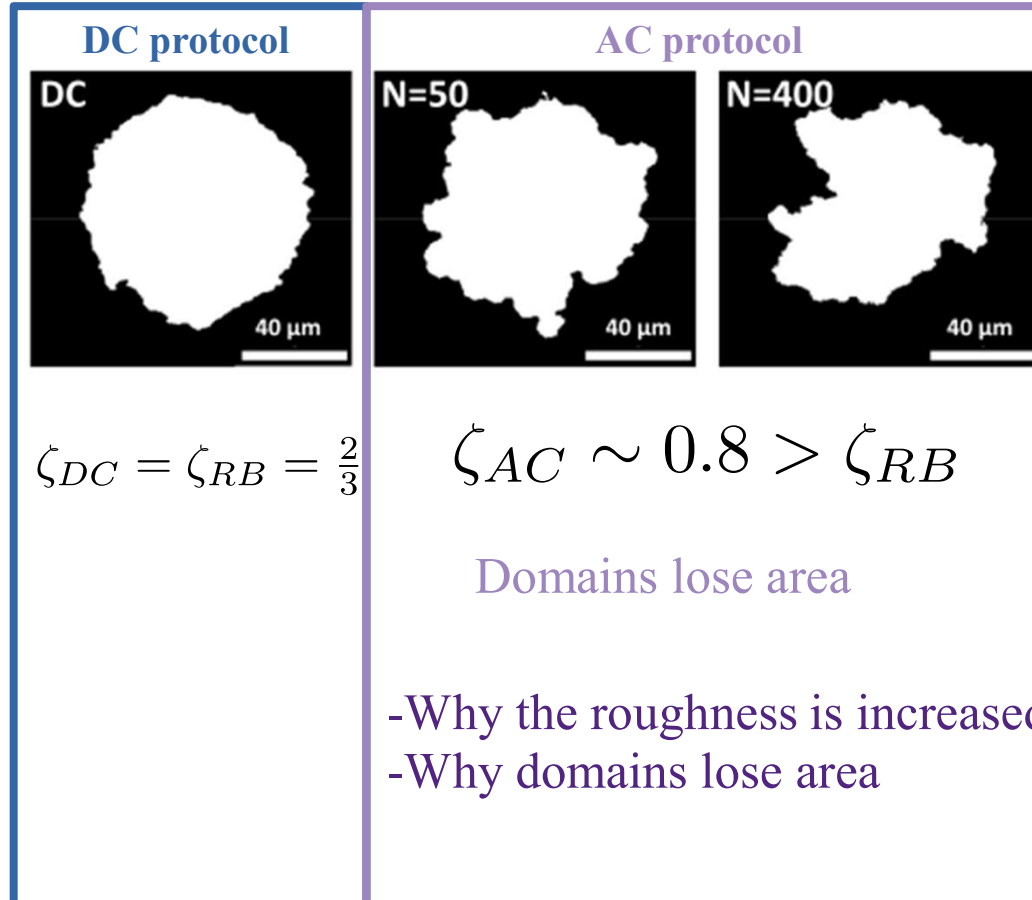
Typical PMOKE protocol to estimate domain wall velocities



After field pulses of same intensity but opposite polarity

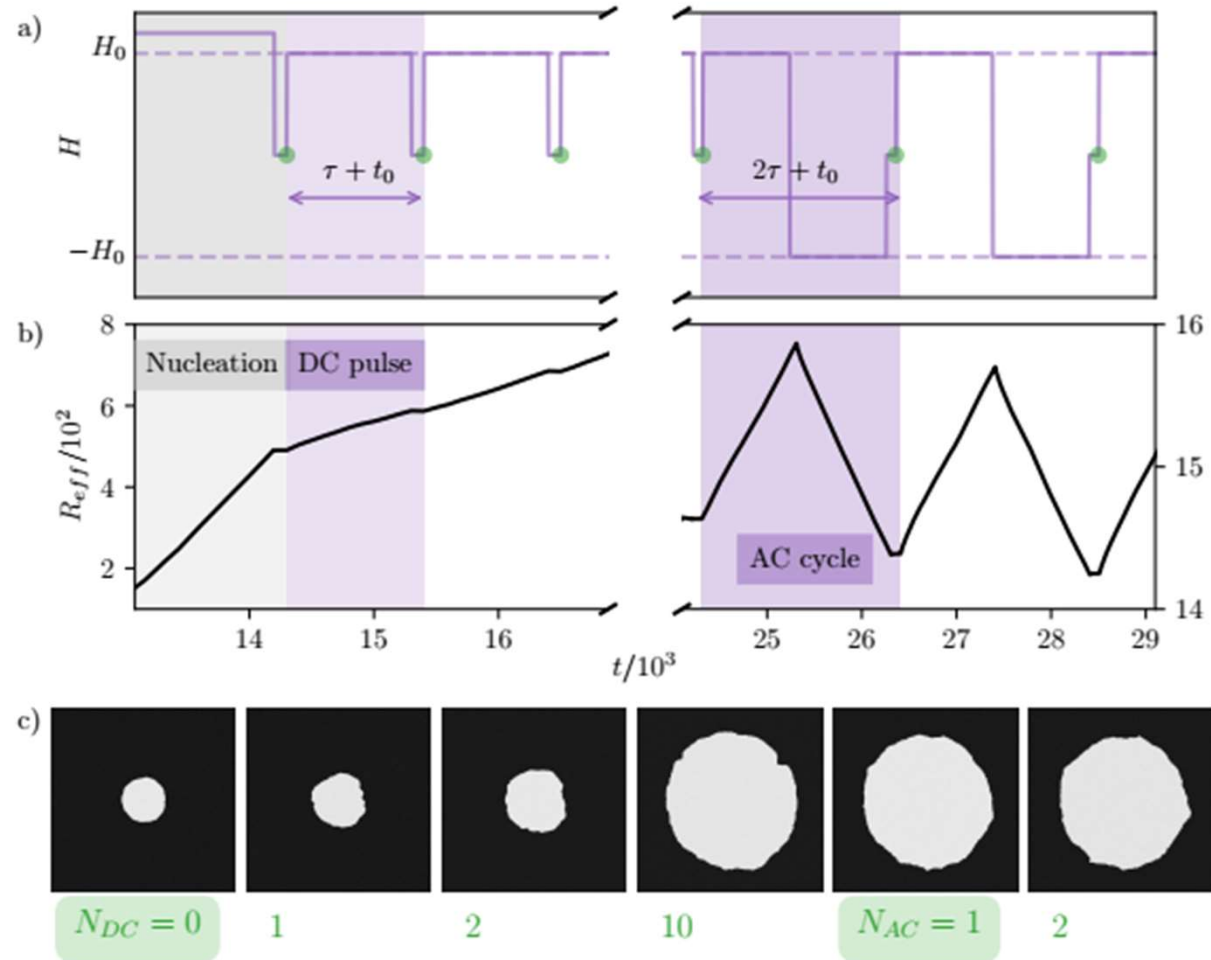
Applications

Recent experiments revealed complex interface behaviours



Experimental protocol emulation

Ginzburg-Landau simulations

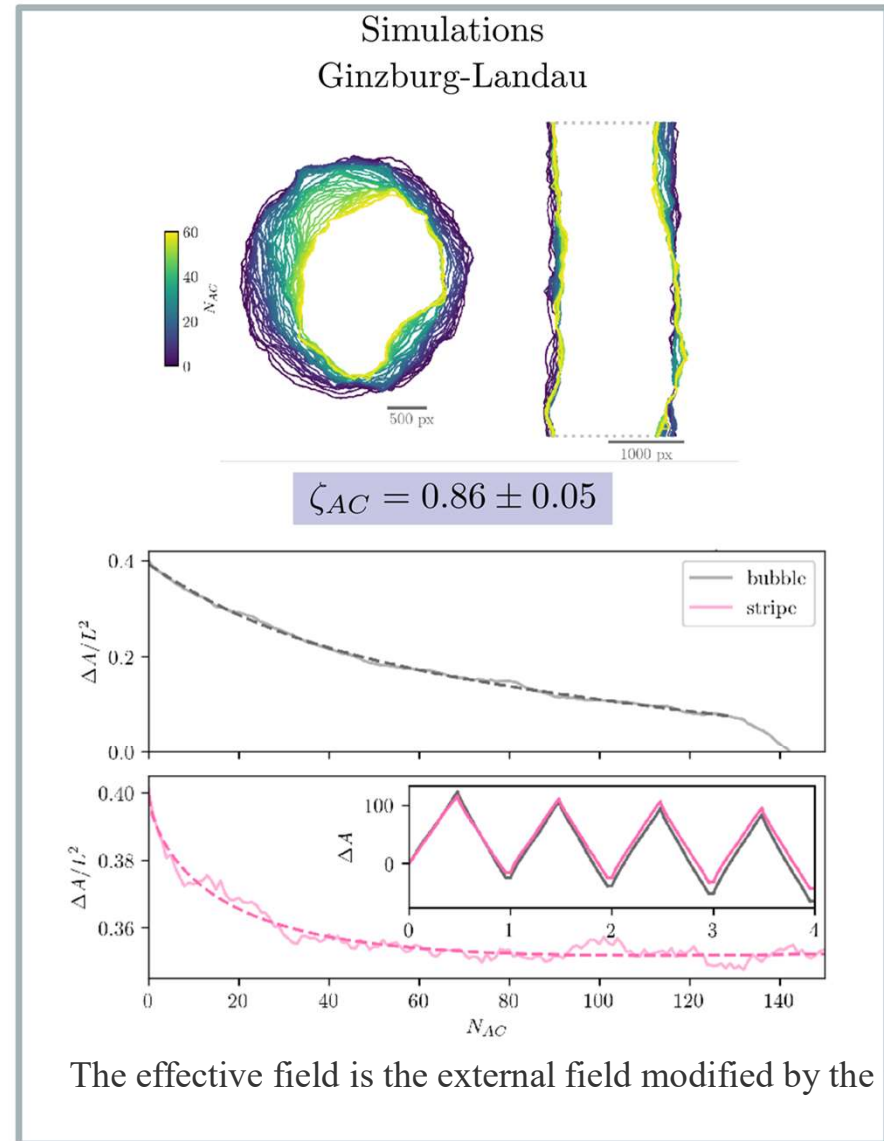
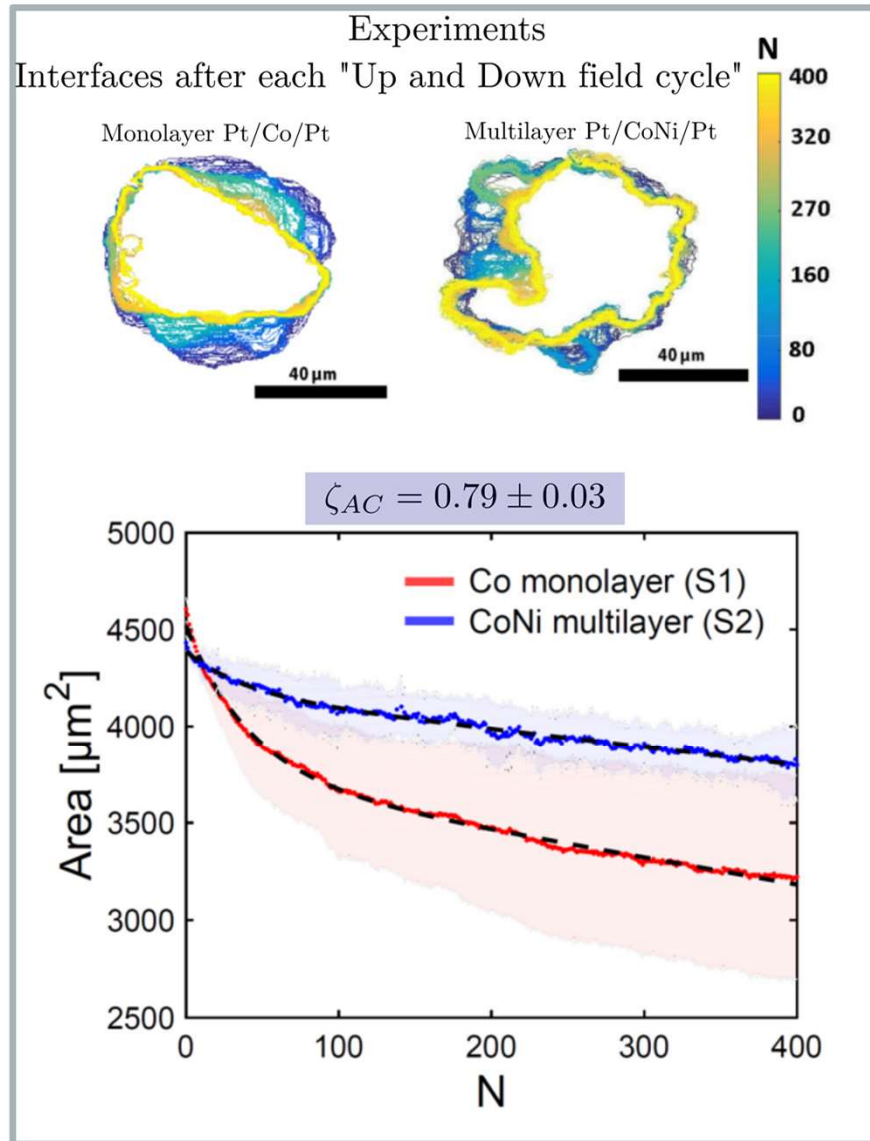


2



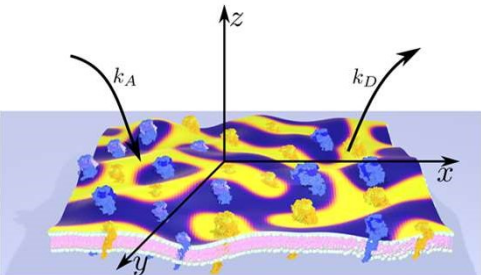
1000 px

Experiments and simulations have the same scaling behavior



Conclusions and perspectives

- Ginzburg-Landau type models allow us to emulate typical experimental protocols to study velocity-field responses
- We show how a Ginzburg-Landau model can be reduced to an elastic line description
- We are now developing new observables to characterise interfaces



Other applications: NC, Kruse, Giamarchi. *Phase separation in surfaces due to matter exchange*. Arxiv: 2205.03306

– **University of Geneva**

Thierry Giamarchi
Patrycja Paruch
Karsten Kruse
Jean-Pierre Eckmann
Bastien Chopard
Iaroslav Gaponenko

– **University of Zurich**

Steven A. Brown

– **EPFL, Laussane**

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Ezequiel Ferrero – CNEA, Bariloche
Javier Curiale – CNEA, Bariloche



**UNIVERSITÉ
DE GENÈVE**

DOMP Department of
Quantum
Matter
Physics

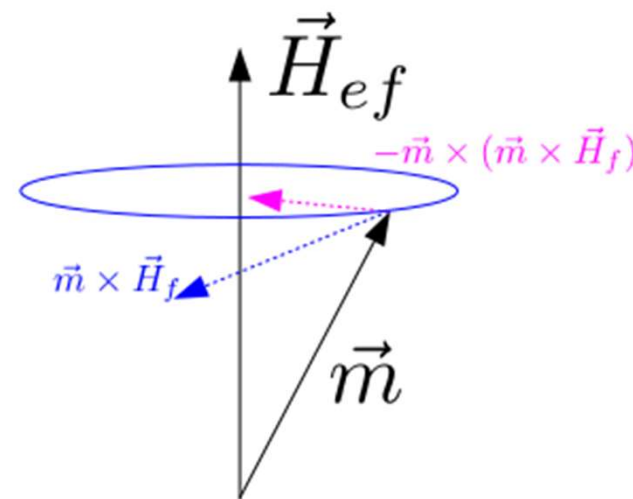


Stochastic Landau-Lifshitz-Gilbert equation

sLLG
$$d_t \vec{M} = \frac{-\gamma_0}{1 + \eta_0^2} \vec{M} \times \left[(\vec{H}_{eff} + \vec{H}_t) + \frac{\eta_0}{M_S} \vec{M} \times (\vec{H}_{eff} + \vec{H}_t) \right]$$

Stochastic field
$$\vec{H}_t = (f_x, f_y, f_z)$$

$$\langle f_i \rangle = 0 \quad \langle f_i(t_1) f_j(t_2) \rangle = 2D \delta_{ij} \delta(t_2 - t_1) \quad D = \frac{\eta_0 k_B T}{\gamma_0 V M_S}$$



Effective field Zeeman + Exchange + Perpendicular magnetic anisotropy (z-direction)

$$\vec{H}_{eff} = -\frac{1}{M_S} \frac{\delta E}{\delta \vec{m}}$$

$$H_{eff}^{x,y} = \frac{2A}{M_S} \nabla^2 m_{x,y} + H_{x,y}$$

$$H_{eff}^z = \frac{2A}{M_S} \nabla^2 m_z + \frac{2K_u}{M_S} m_z + H_z$$

$$\begin{aligned}
\frac{\partial m_z}{\partial t} = & \frac{-\gamma_0}{1 + \eta_0^2} \left\{ \frac{2A}{M_S} (m_x \nabla^2 m_y - m_y \nabla^2 m_x) \right. \\
& + m_x f_y + m_y f_x \\
& + \eta_0 \left[\frac{2A}{M_S} (-m_z) ((\nabla m_x)^2 + (\nabla m_y)^2 + (\nabla m_z)^2) \right. \\
& \left. \left. + m_x m_z f_x - m_y m_z f_y + \right. \right.
\end{aligned}$$

sLLG

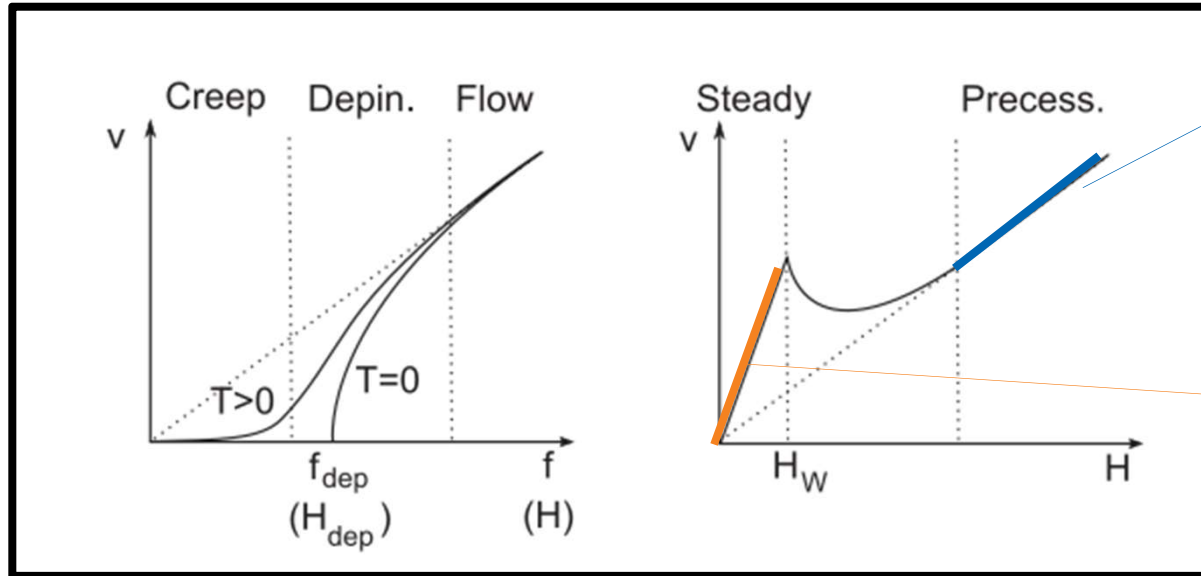
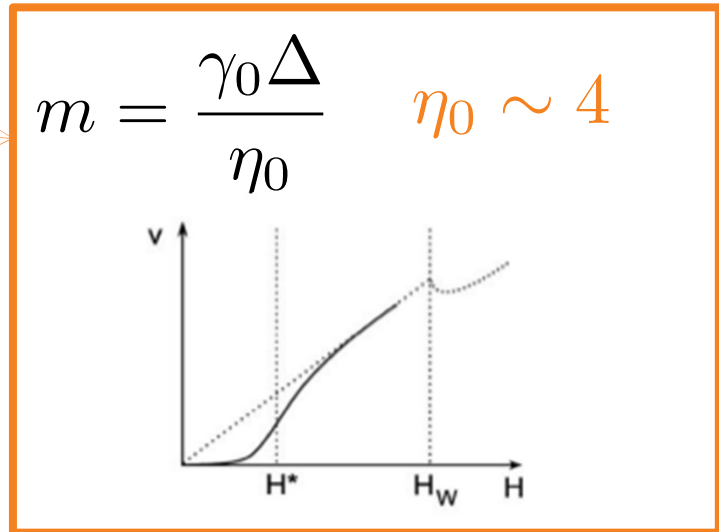
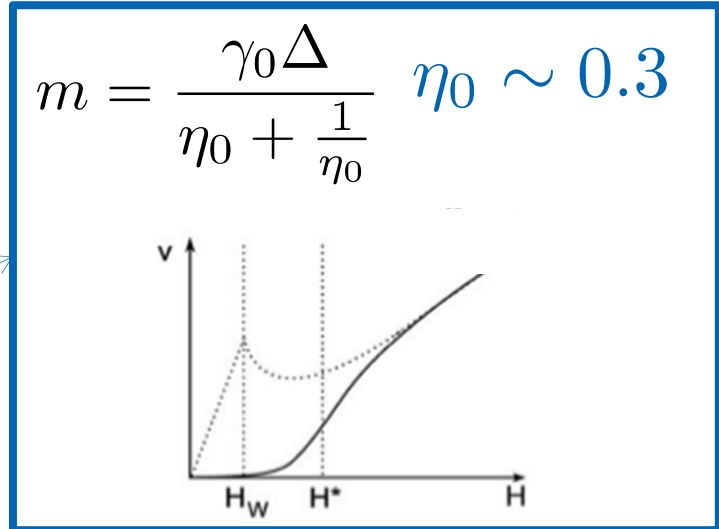
$$\frac{\eta_0 \gamma_0}{1 + \eta_0^2} (1 - m_z^2) \left(\frac{2K_u}{M_S} m_z + H_z + f_z \right) - \frac{2A}{M_S} \nabla^2 m_z$$

Ginzburg-Landau

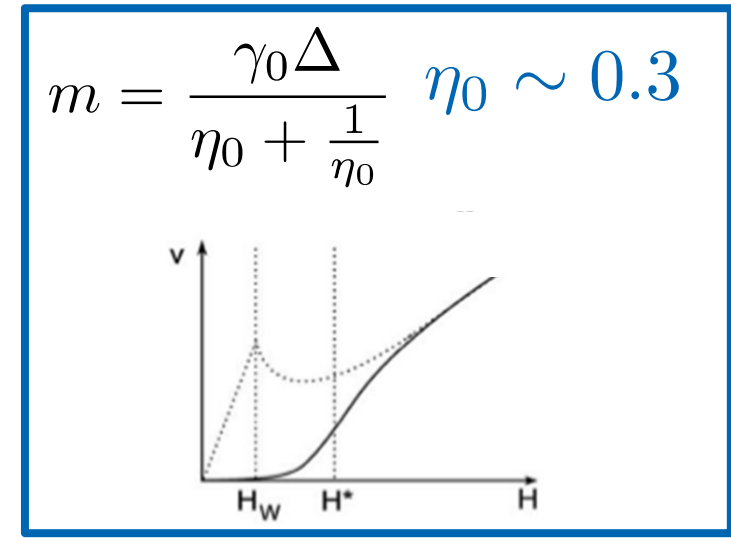
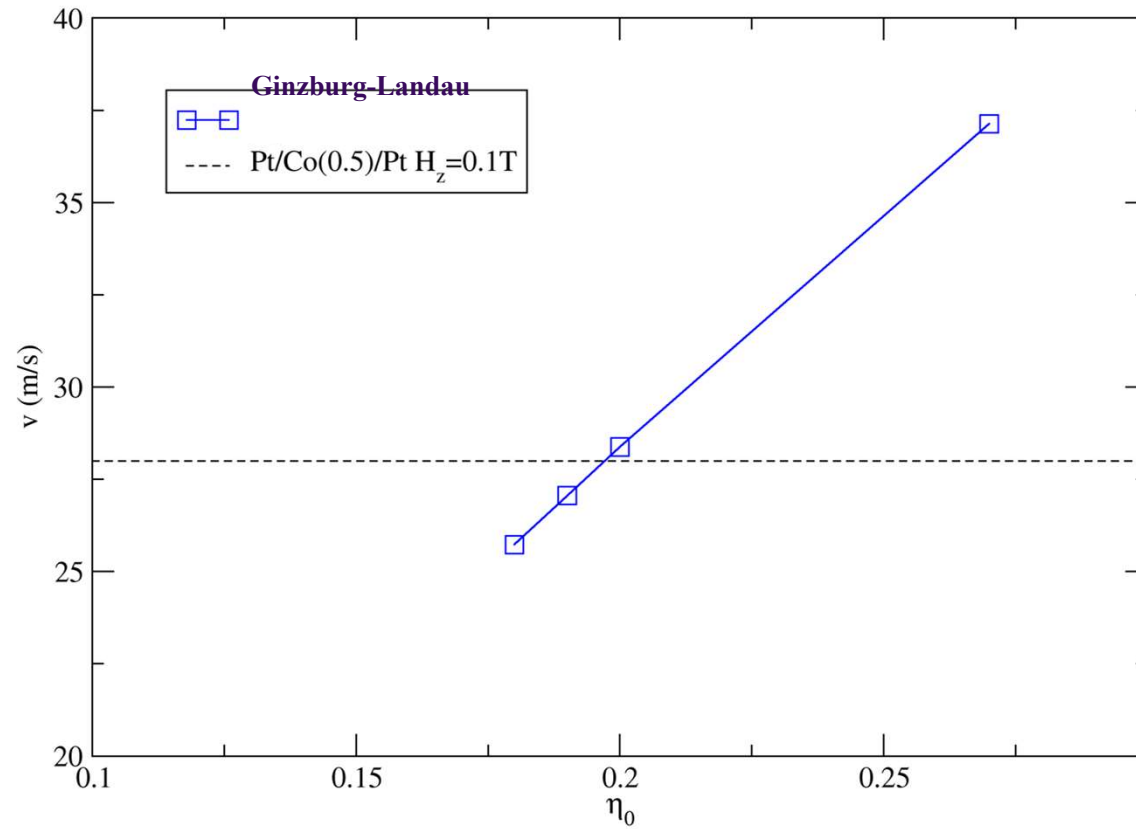
$$\frac{\partial \phi}{\partial t} = \Gamma (1 - \phi^2) (\alpha \phi + h_0) + \Gamma \gamma \nabla^2 \phi + \xi$$

Flow regime

$$v_{flow} = mH_z$$

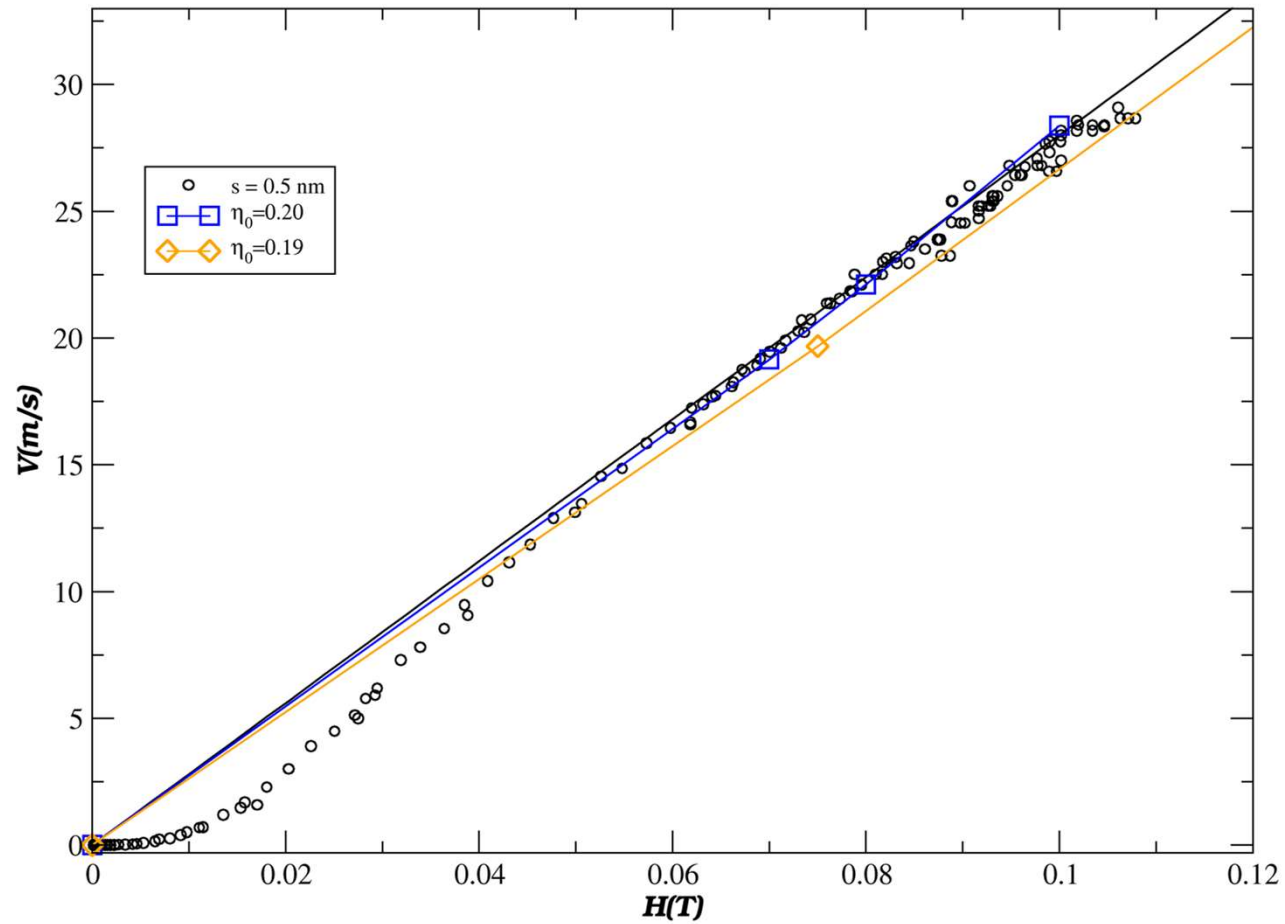


$$v_{flow} = mH_z$$

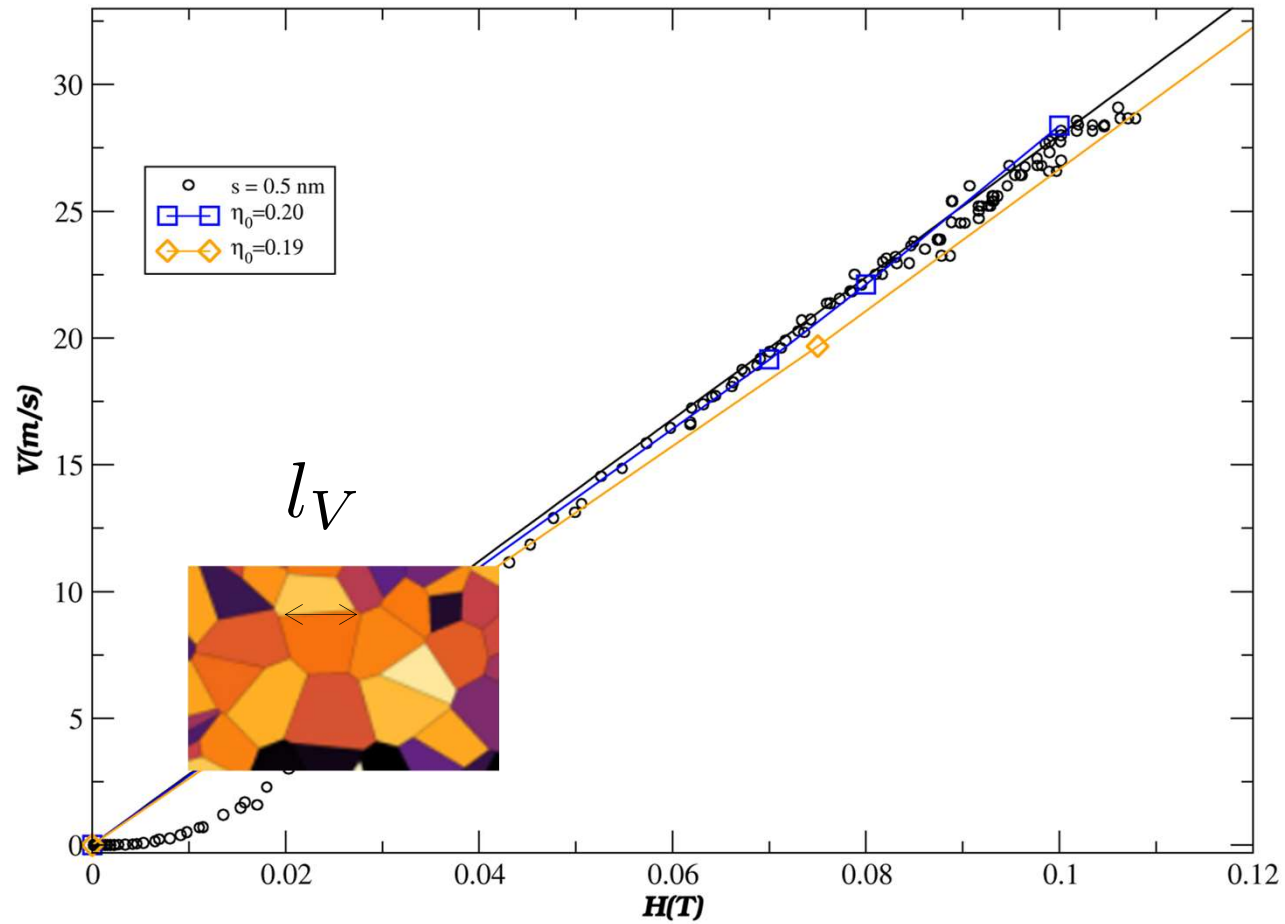


Precessional regime

Flow regime: Ginzburg-Landau simulations and Pt/Co/Pt experiments

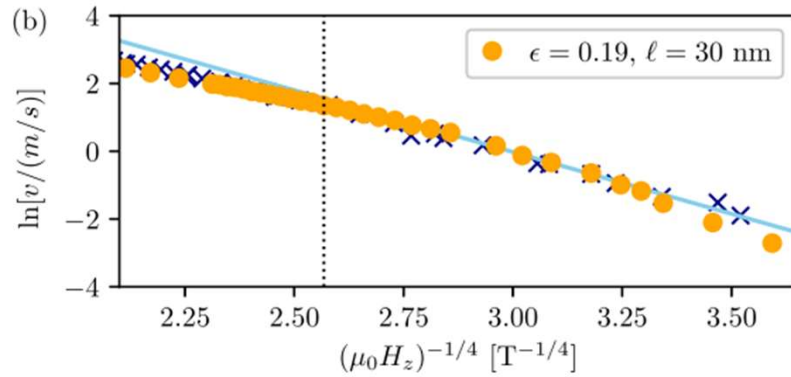
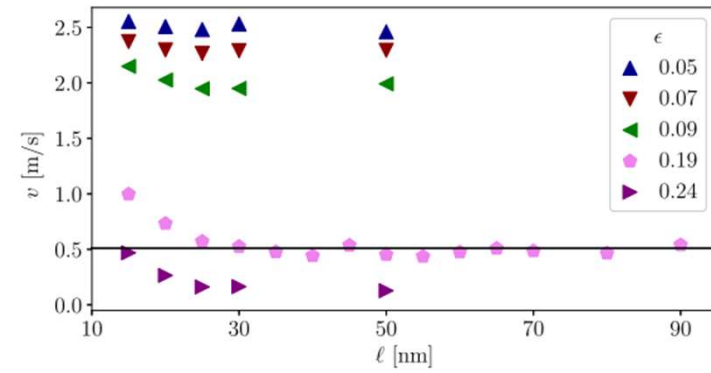
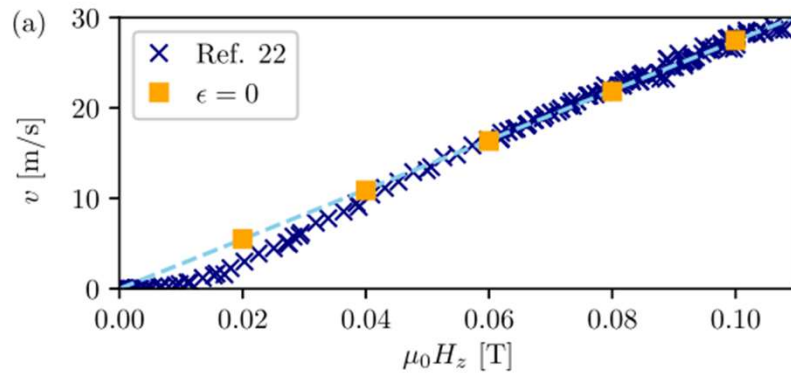


Flow regime: Ginzburg-Landau simulations and Pt/Co/Pt experiments



P.J. Metaxas, J. P. Jamet, A. Mougin, M. Cormier, J. Ferre, V. Baltz, B. Rodmacq, B. Dieny, and R. L. Stamps. PRL 2007
P. Guruciaga, NC, V. Jeudy, J. Curiale, and S. Bustingorry. JSTAT 2021

$$\mathbf{m}_{xy} = \sqrt{1 - m_z^2} \left[\cos \theta \frac{\nabla m_z}{|\nabla m_z|} + \sin \theta \frac{\nabla \times (m_z \hat{\mathbf{e}}_z)}{|\nabla \times (m_z \hat{\mathbf{e}}_z)|} \right]$$



Elastic approximation

The energy required to create an interface may be written as

$$E_{el} = \varepsilon_0 \ell.$$

where ε_0 is the energy cost of the interface per unit length.

We can approximate

$$d\ell = \sqrt{dy^2 + du^2} = dz \sqrt{1 + \left(\frac{du}{dy}\right)^2}.$$

So, $E_{el} = \varepsilon_0 \int_0^L d\ell = \varepsilon_0 \int_0^L dy \sqrt{1 + \left(\frac{du}{dy}\right)^2}.$

If u varies smoothly with y , then $\frac{du}{dy}$ is small, and

$$E_{el} \simeq \frac{\varepsilon_0}{2} \int_0^L dy (\nabla u(y))^2.$$

Assuming an Ansatz:

$$\varphi(x, y, t) = \varphi^*(x - u(y, t)),$$

its derivatives are given by

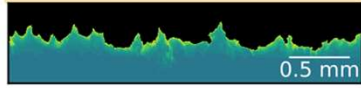
$$\partial_t \varphi^* = -\varphi^{*'} \partial_t u$$

$$\partial_x \varphi^* = \varphi^{*'}; \quad \partial_x^2 \varphi^* = \varphi^{*''}$$

$$\partial_y \varphi^* = -\varphi^{*'} \partial_y u; \quad \partial_y^2 \varphi^* = \varphi^{*''} (\partial_y u)^2 - \varphi^{*'} \partial_y^2 u.$$

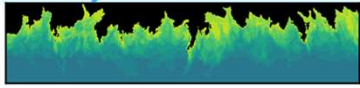
binds to tubulin: inhibits microtubule polymerization
targets cell division rates

Colchicine



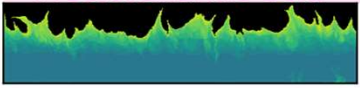
disrupts the polymerisation and network build-up of actin filaments
inhibits cell motility and transmission of mechanical forces

Cytochalasin B



inhibits gap junctions communication
disrupts this pathway of electrochemical signal transmission (up to 10 neighboring cells)

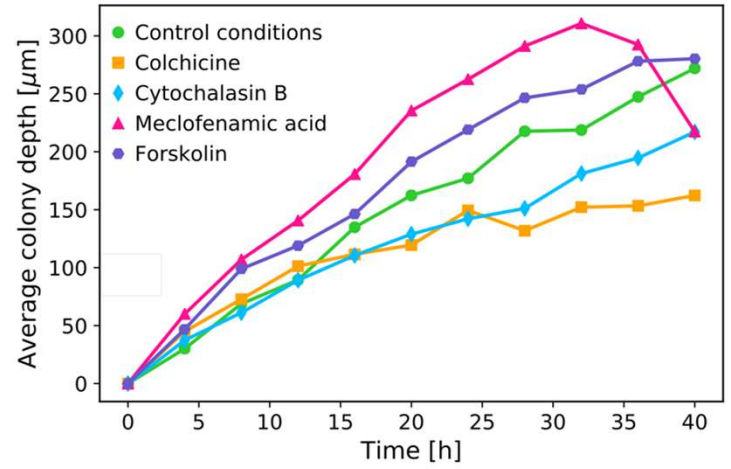
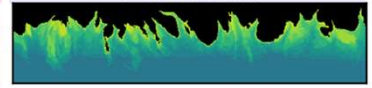
Meclofenamic acid



activates adenylyl cyclase creating the signalling molecule c-AMP.

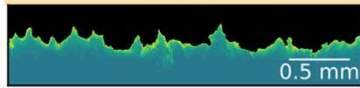
Globally affects cell metabolism

Forskolin



binds to tubulin: inhibits microtubule polymerization
targets cell division rates

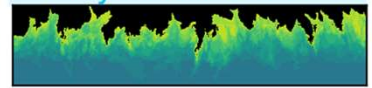
Colchicine



0.5 mm

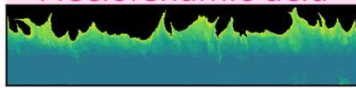
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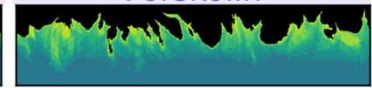
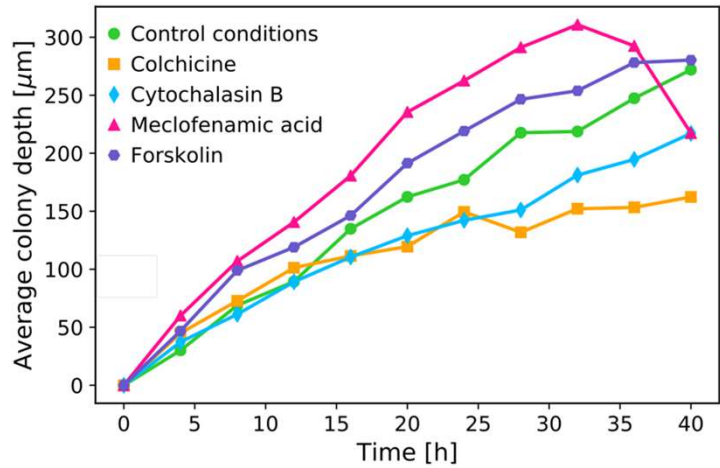
inhibits gap junctions communication
disrupts this pathway of electrochemical signal transmission
 (up to 10 neighboring cells)

Meclofenamic acid



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Globally affects cell metabolism

Forskolin

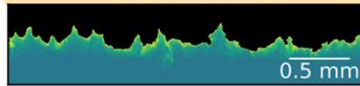



Cytochalasin B
 Colchicine

decrease front velocity

binds to tubulin: inhibits microtubule polymerization
targets cell division rates

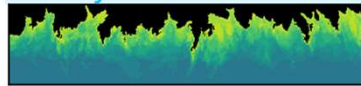
Colchicine



0.5 mm

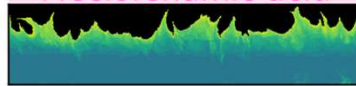
disrupts the polymerisation and network build-up of actin filaments
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Cytochalasin B



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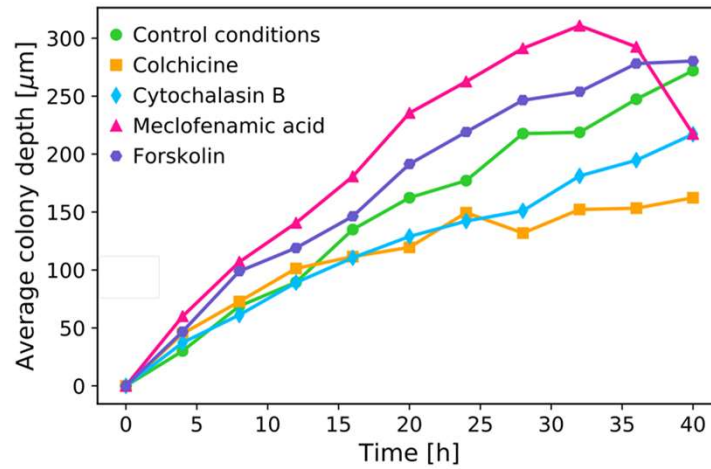
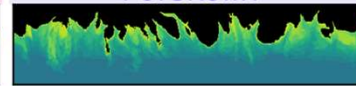
Meclofenamic acid



activates adenylyl cyclase creating the signalling molecule c-AMP.

Globally affects cell metabolism

Forskolin

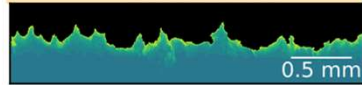


Meclofenamic acid
 Forskolin

increase front velocity

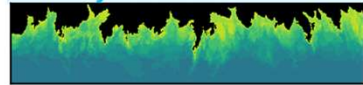
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Colchicine



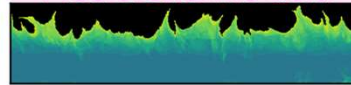
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Cytochalasin B



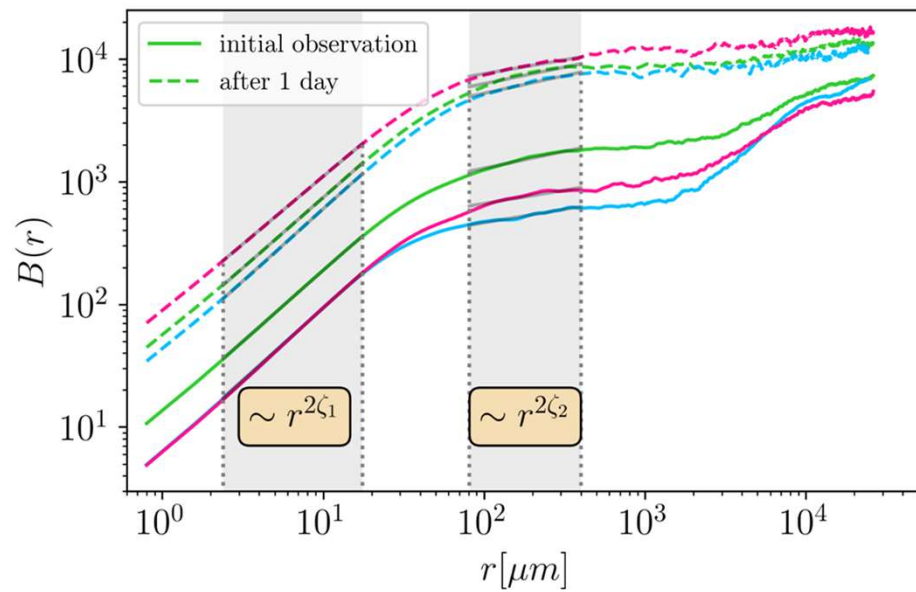
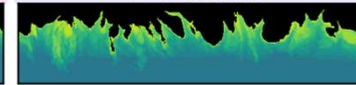
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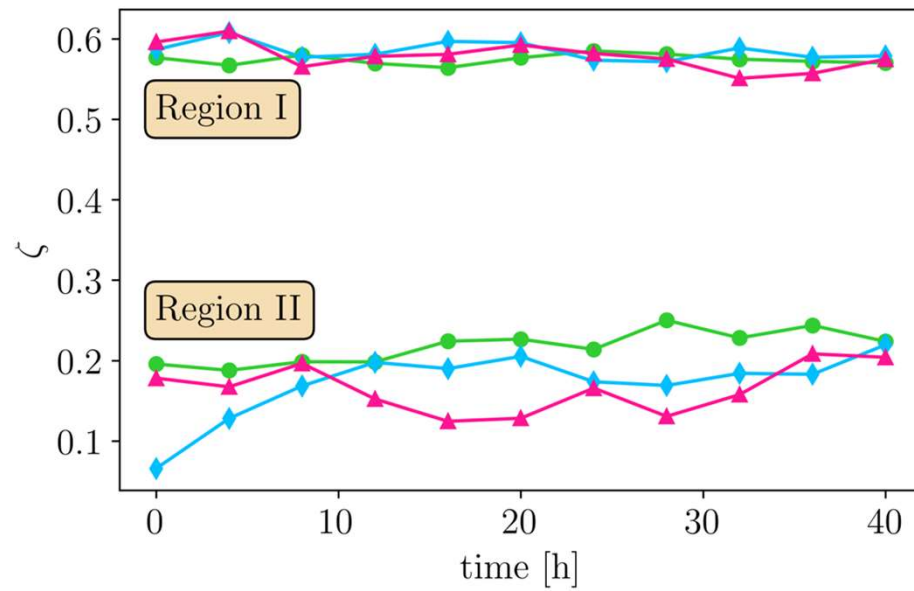
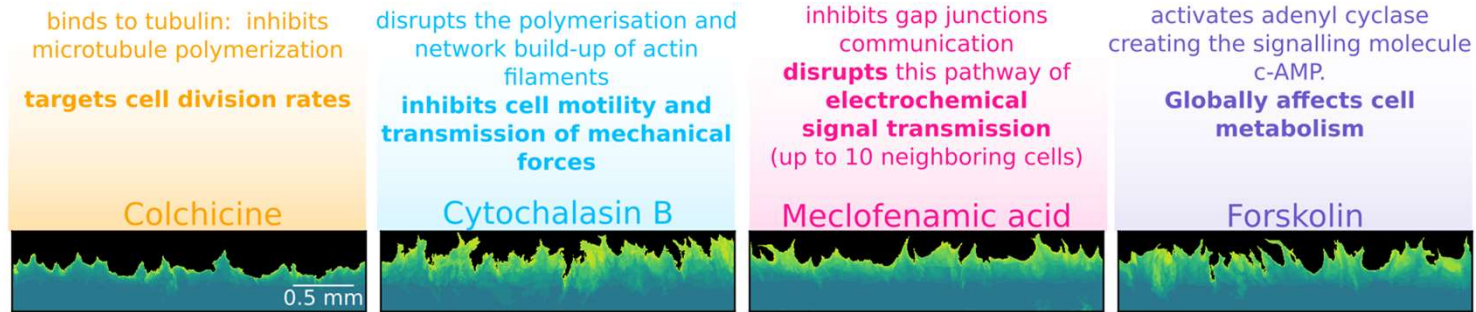
Meclofenamic acid



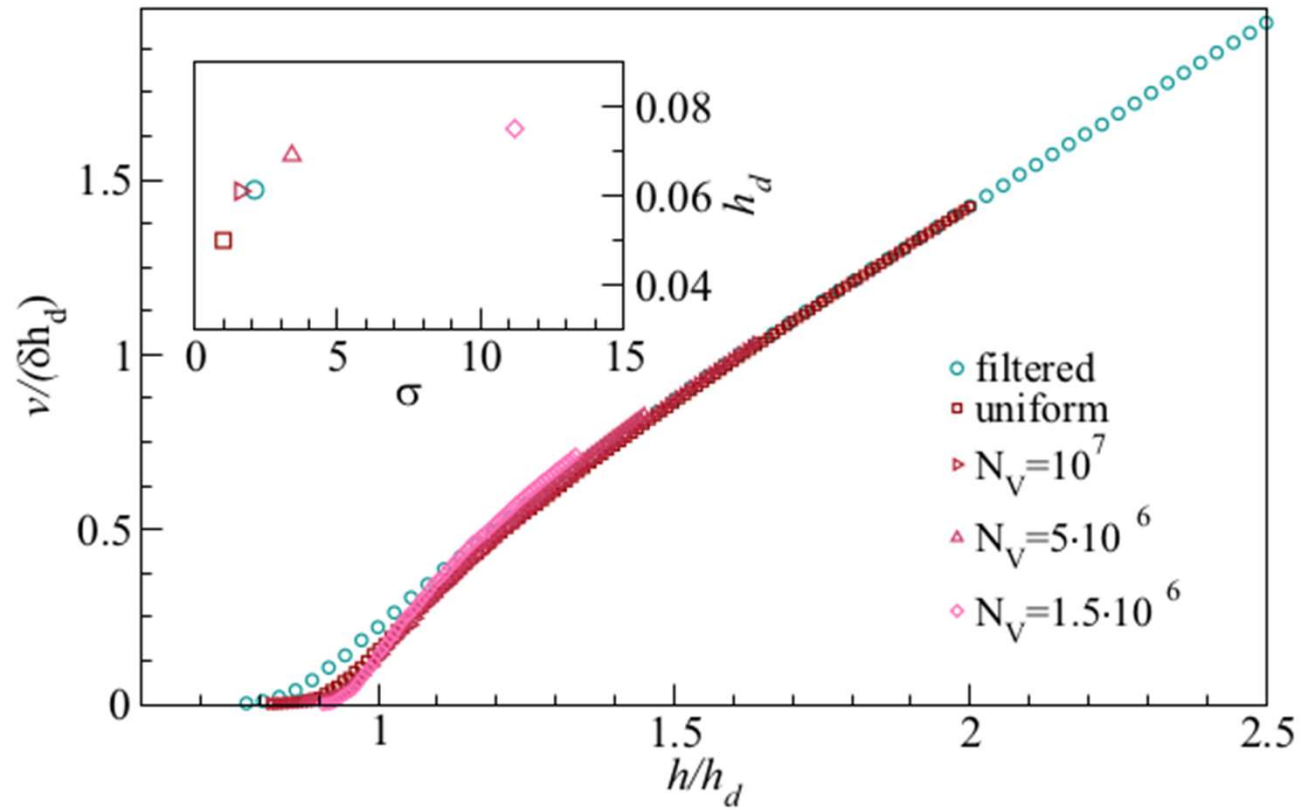
activates adenylyl cyclase creating the signalling molecule c-AMP.
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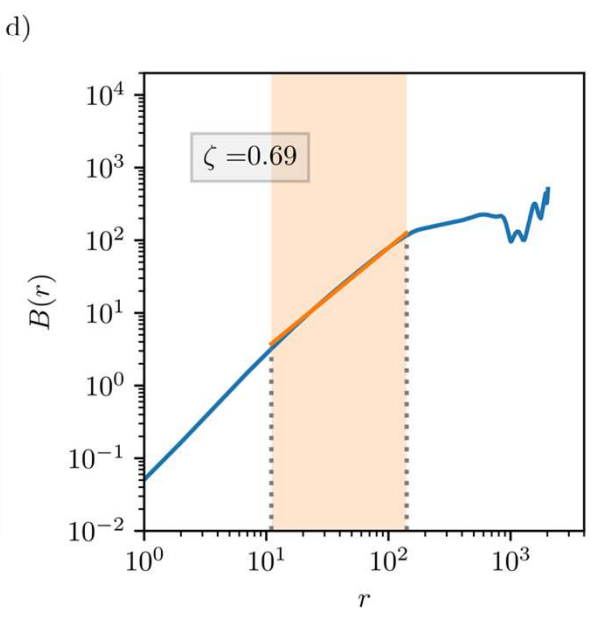
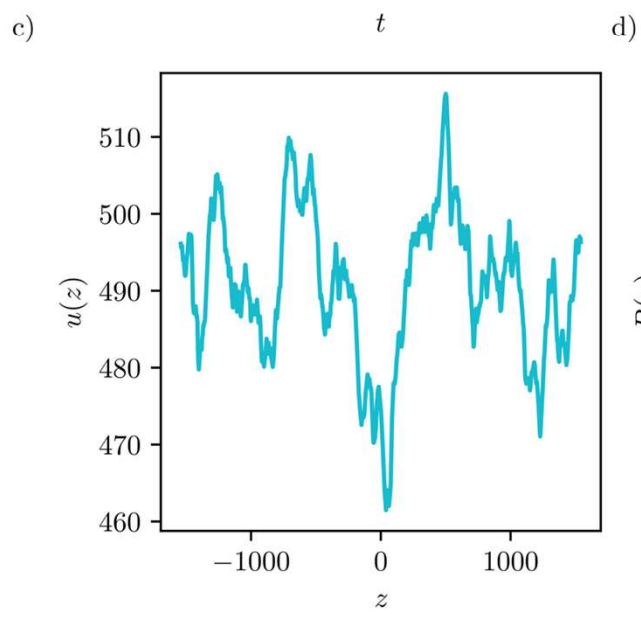
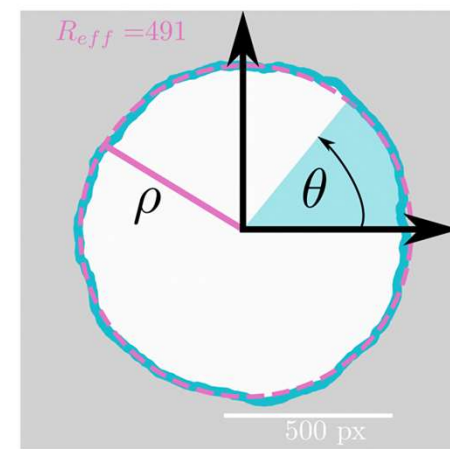
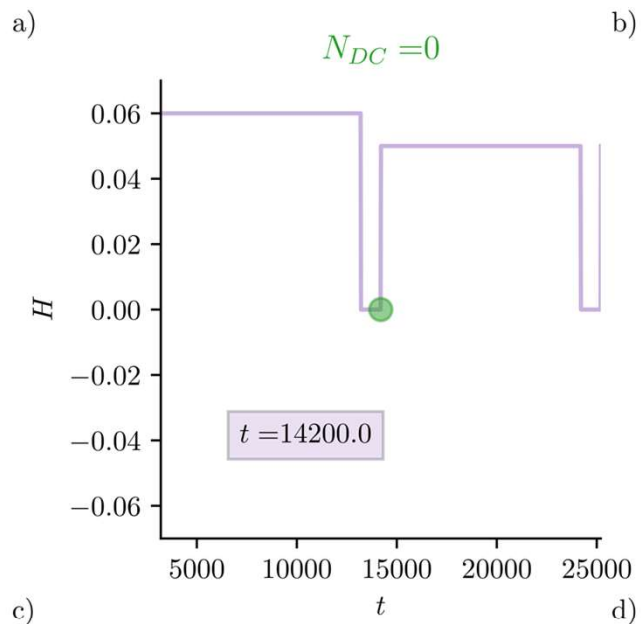
Forskolin





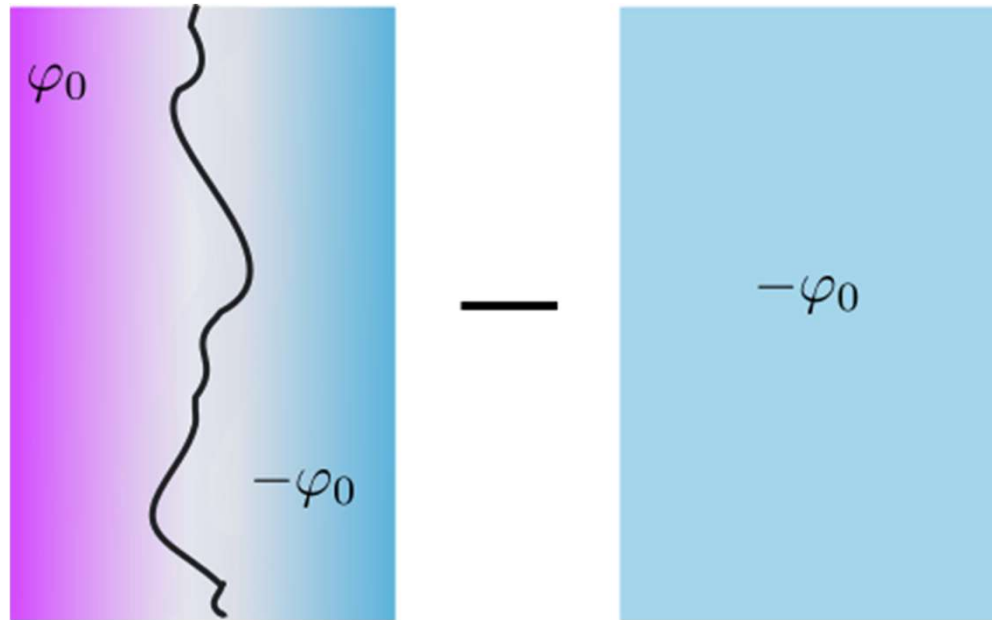
Ginzburg-Landau approach





With our method we find

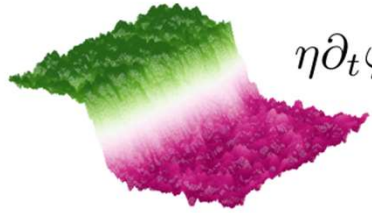
$$c = \frac{2\sqrt{2}}{3} \frac{\alpha}{\delta} \sqrt{\alpha\gamma}$$



Which is the same relation that one finds by computing the energy cost of creating a domain wall in the

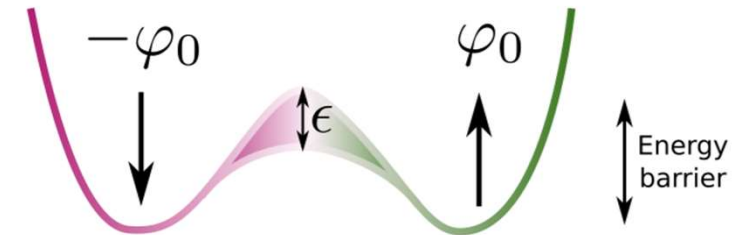
Ginzburg-Landau

State: φ



$$\eta \partial_t \varphi = \gamma \nabla^2 \varphi - (1 + \epsilon \zeta(\vec{r})) V'(\varphi) + h + \xi(\vec{r}, t)$$

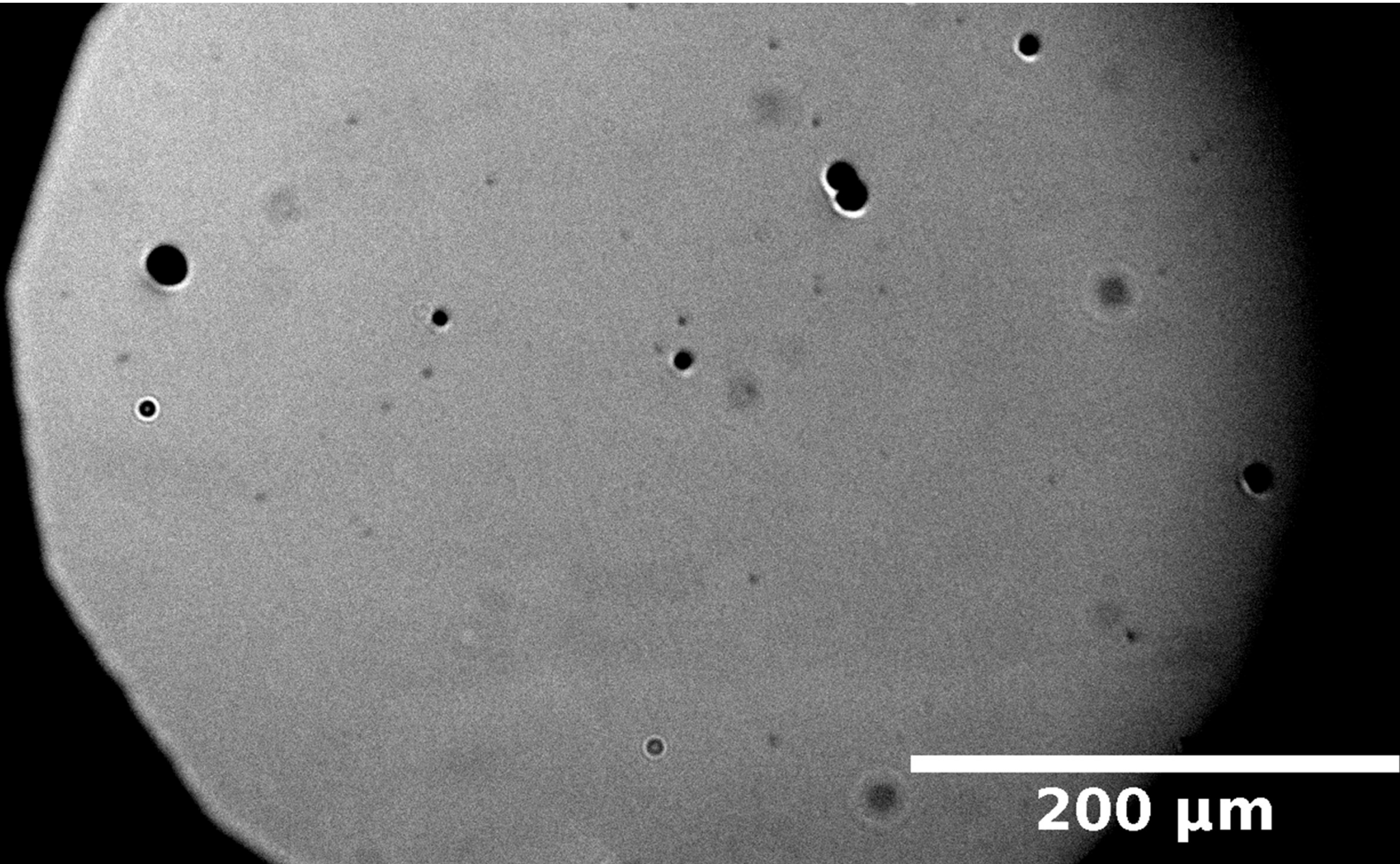
disorder



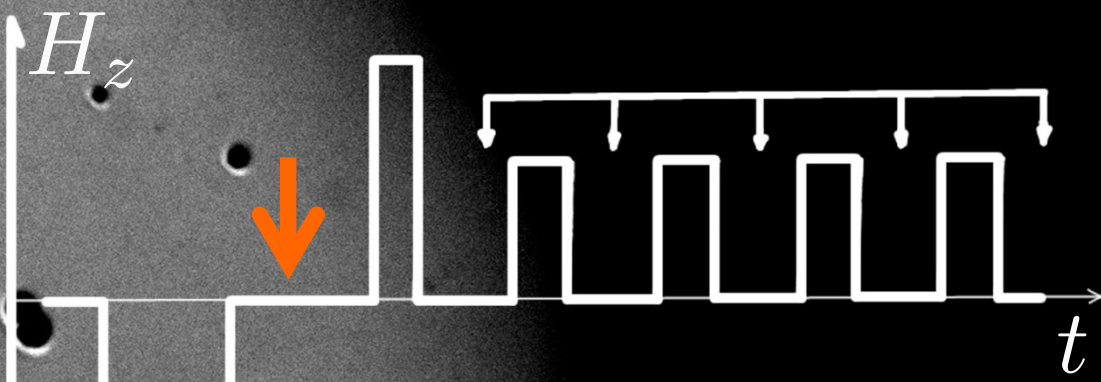
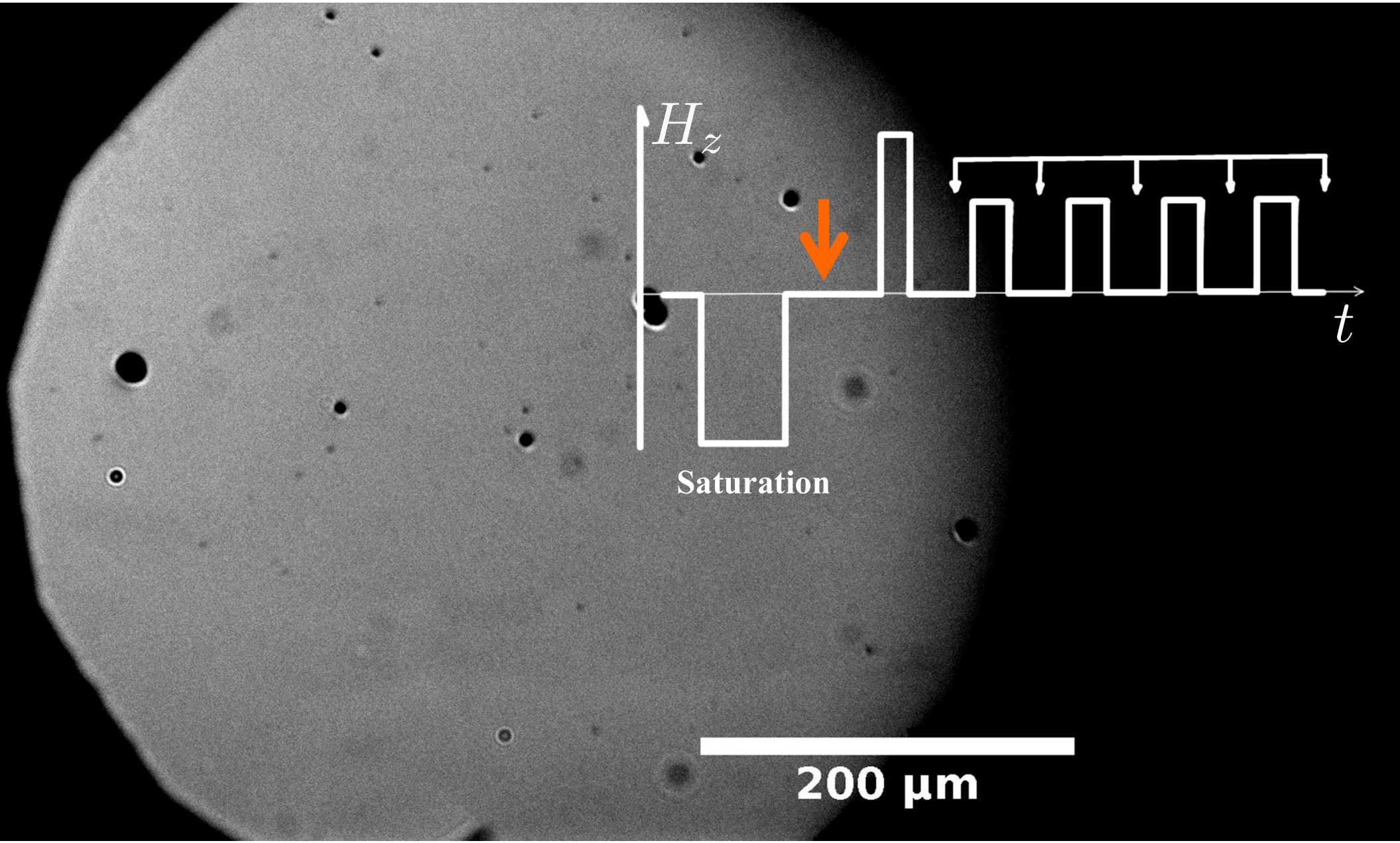
We use an ansatz

$$\varphi(x, y, t) = \varphi^*(x - u(y, t))$$

$$-\eta \varphi^{*'} \partial_t u = \gamma \left(\varphi^{*''} + \varphi^{*''} (\partial_y u)^2 - \varphi^{*'} \partial_y^2 u \right) - V'(\varphi^*) - \epsilon \zeta(x, y) V'(\varphi^*) + \xi(x, y, t)$$



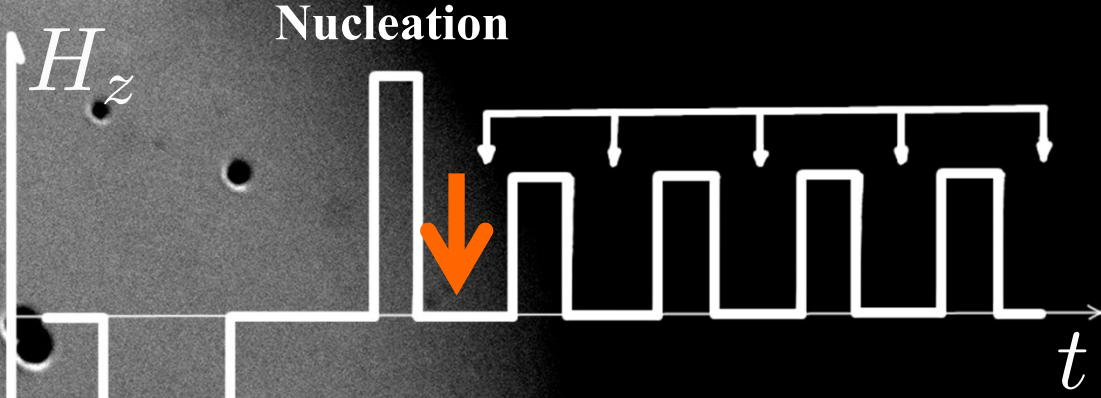
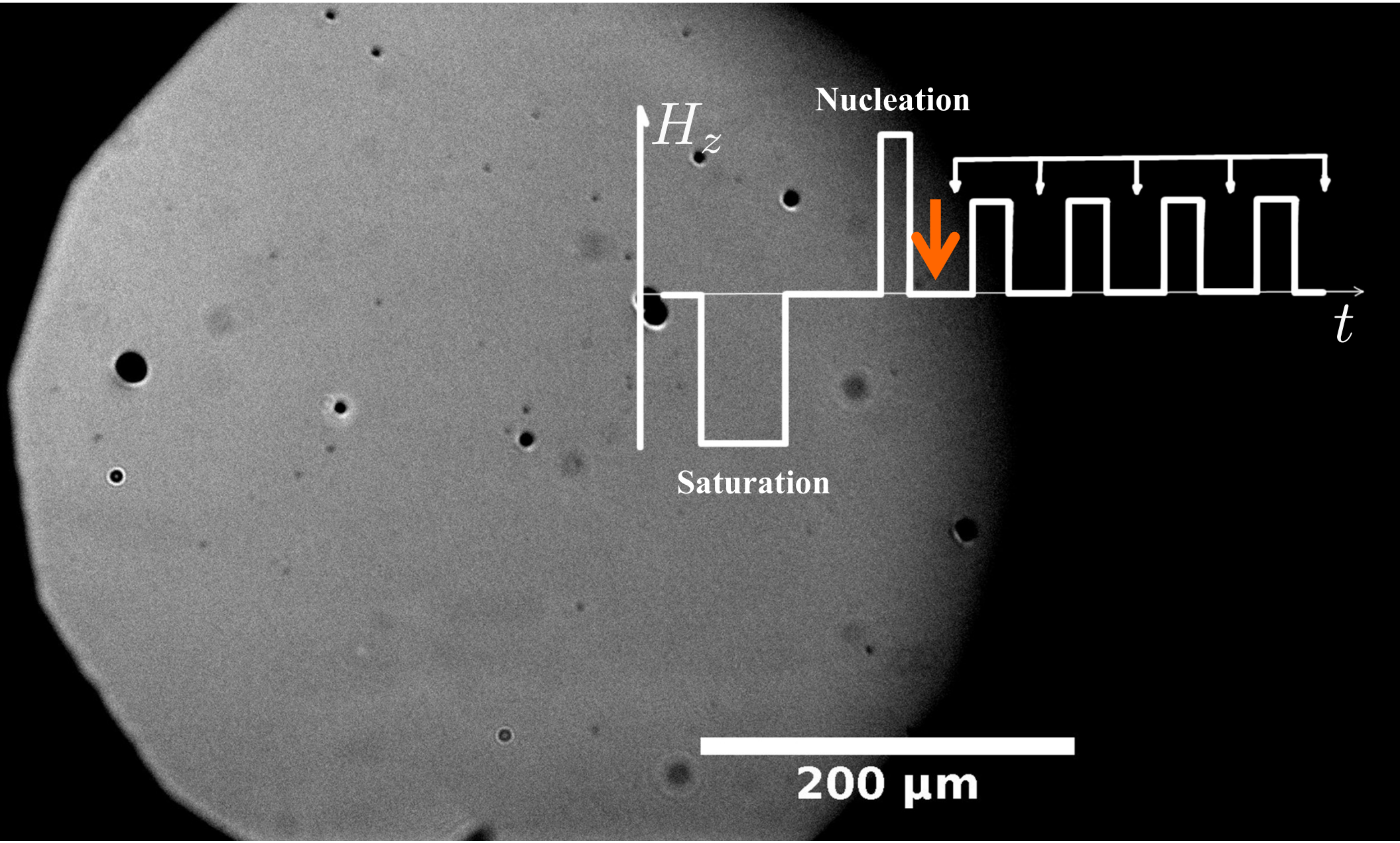
200 μm



Saturation

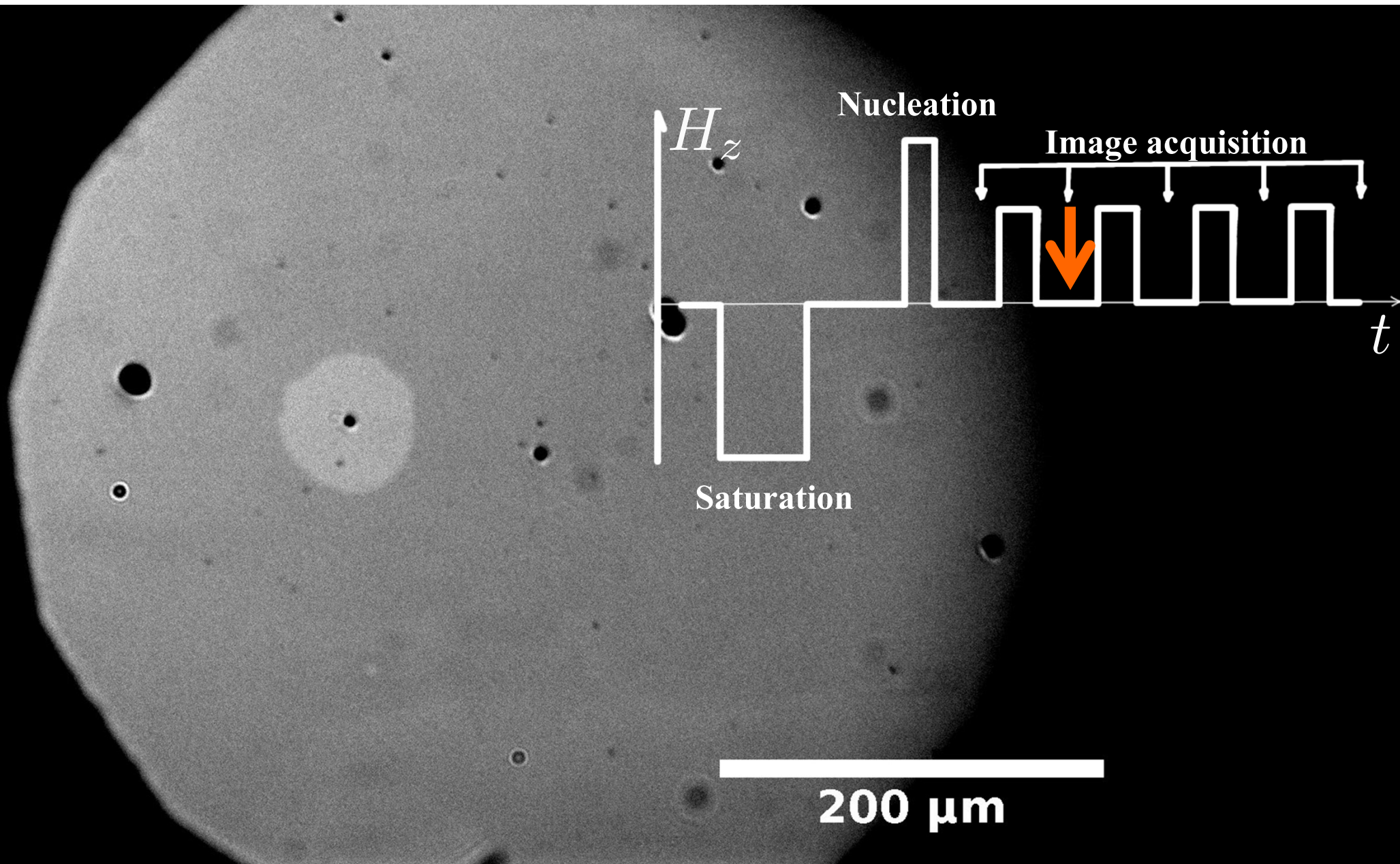


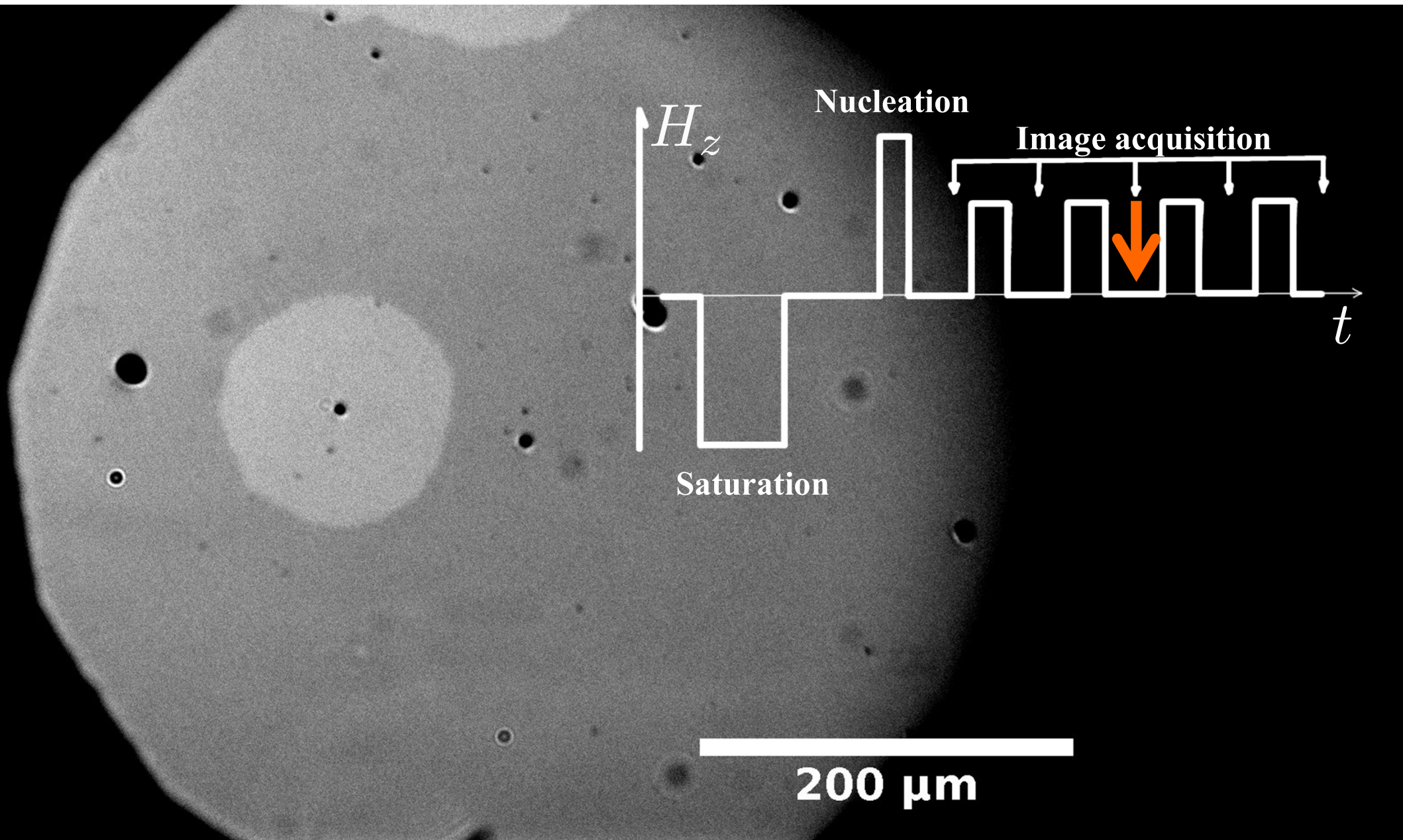
200 μm

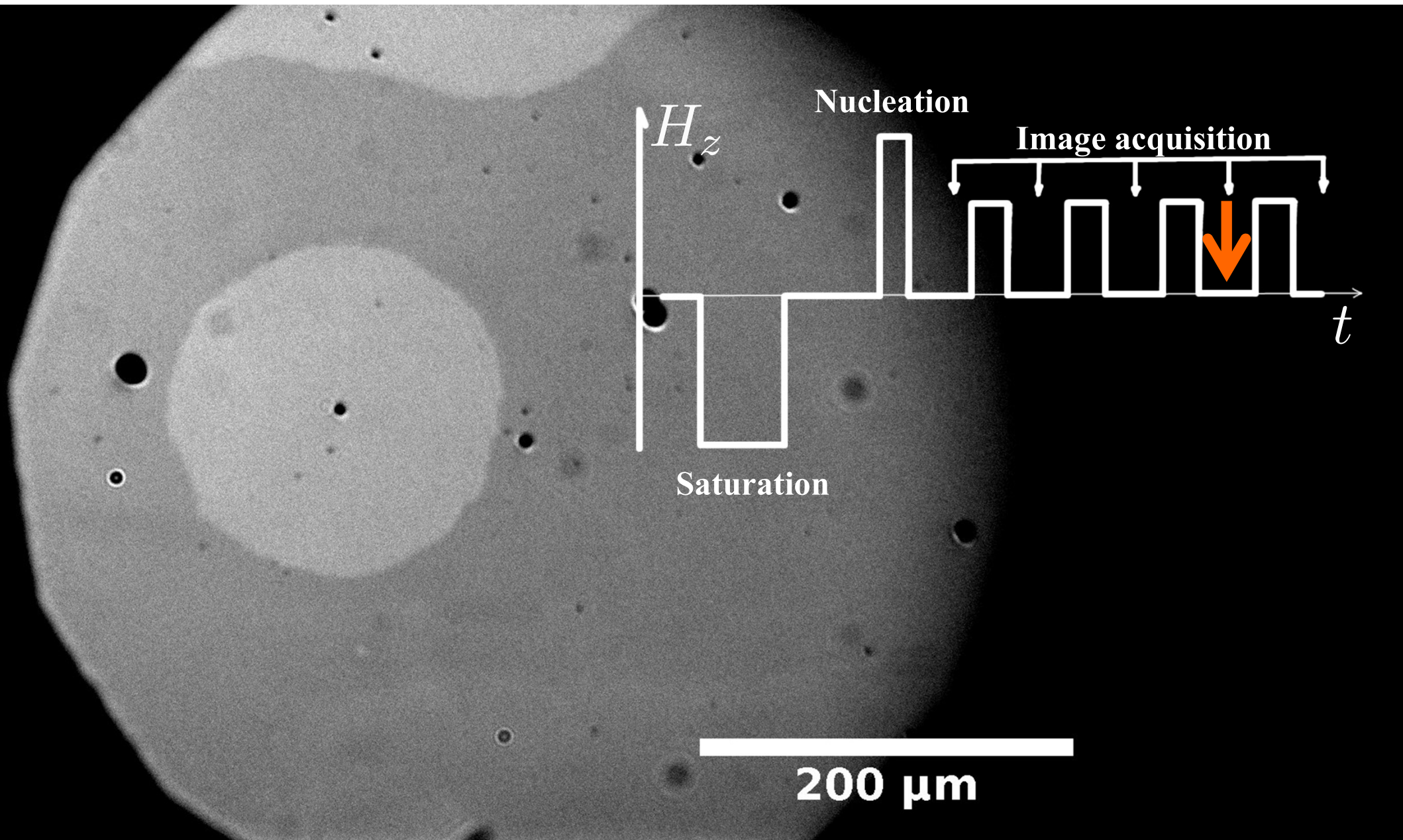


Saturation

200 μm





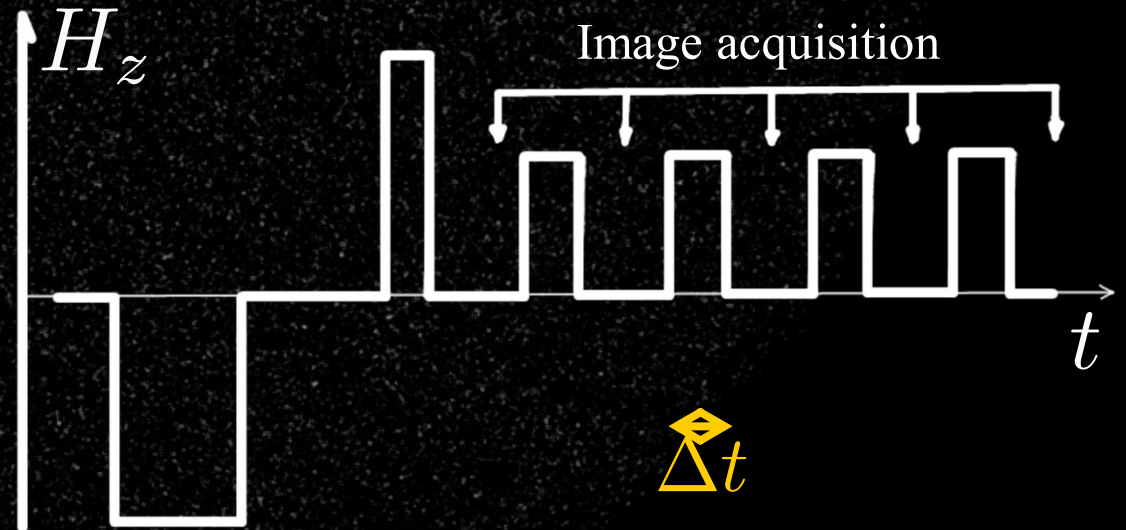


Typical PMOKE
protocol to estimate
domain wall velocities

$$v_{\text{DW}} = \frac{\Delta x}{\Delta t}$$

$\odot \vec{H}_z$

200 μm



temperature

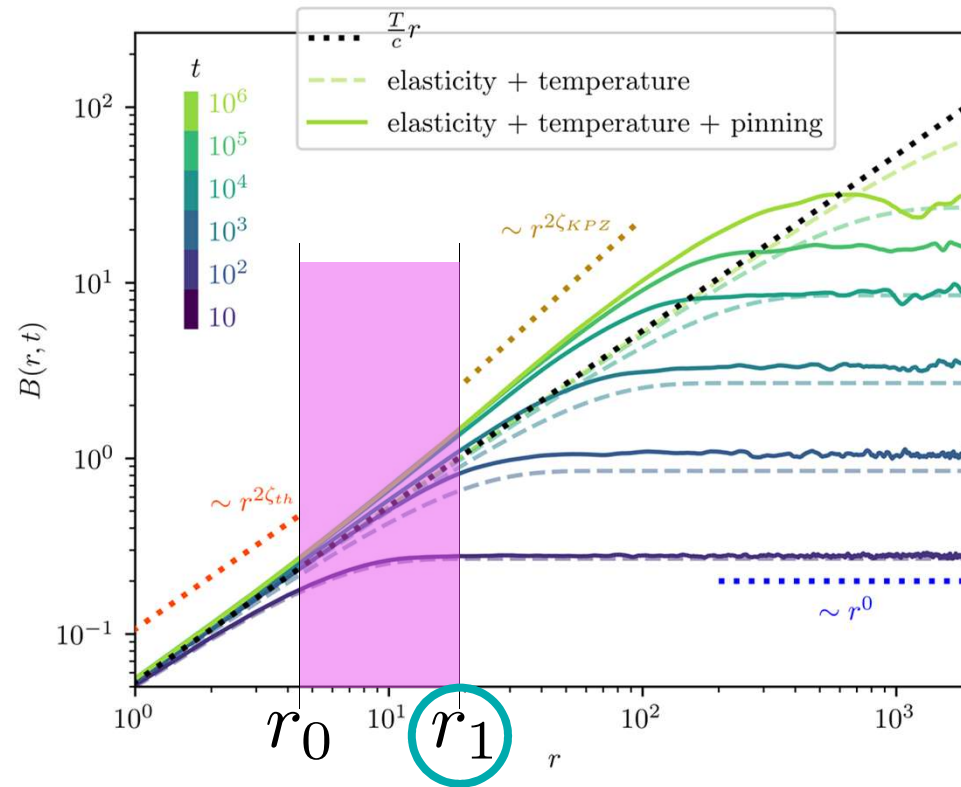
$$\zeta_{th} = \frac{1}{2}$$

disorder

$$\zeta_{RB} = \frac{2}{3}$$

interplay

$$\zeta_{dis} \sim 0.9$$



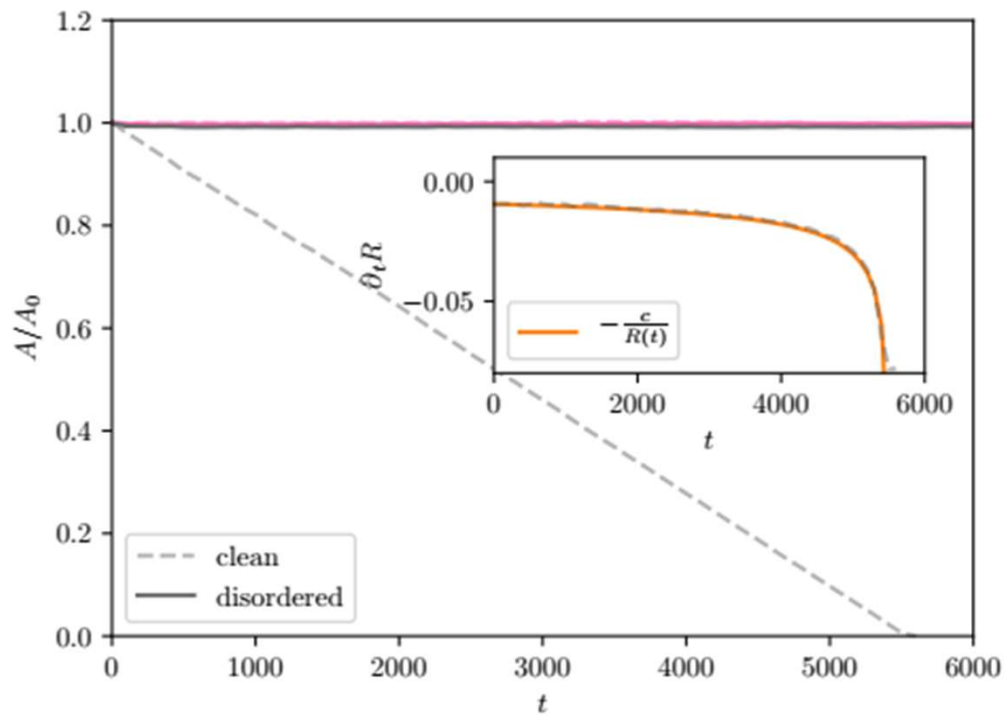
depends on the disorder correlation

With AC cycles the disorder

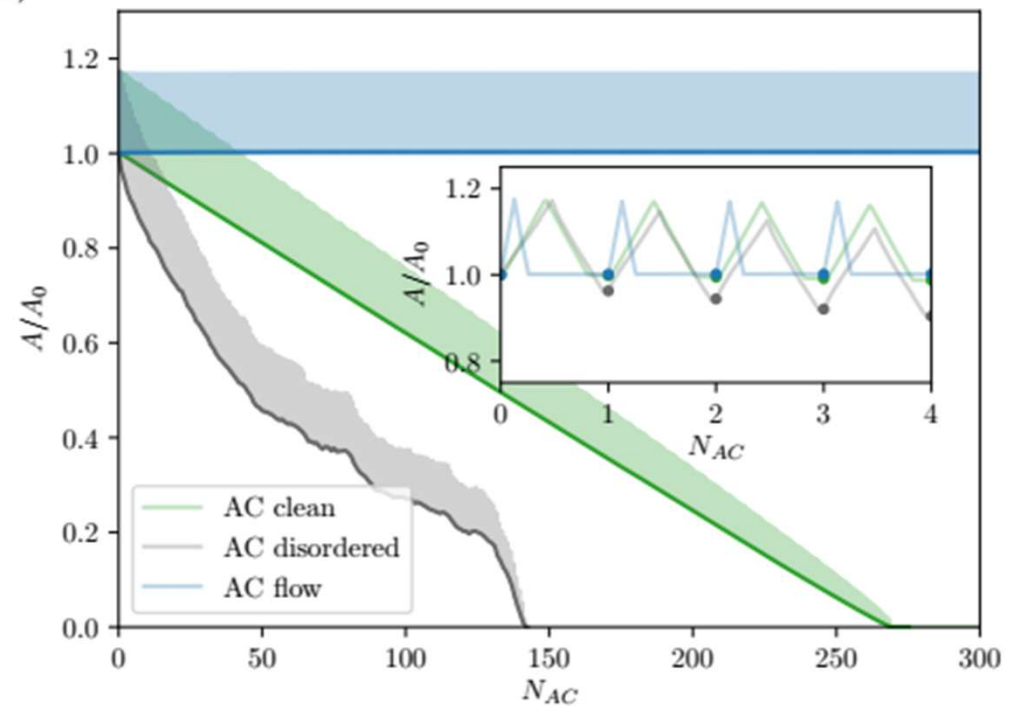
The area is lost due to local curvatures that induce a force:
the effective field felt by the interface is

$$\sim H_0 - \frac{c}{R(t)}$$

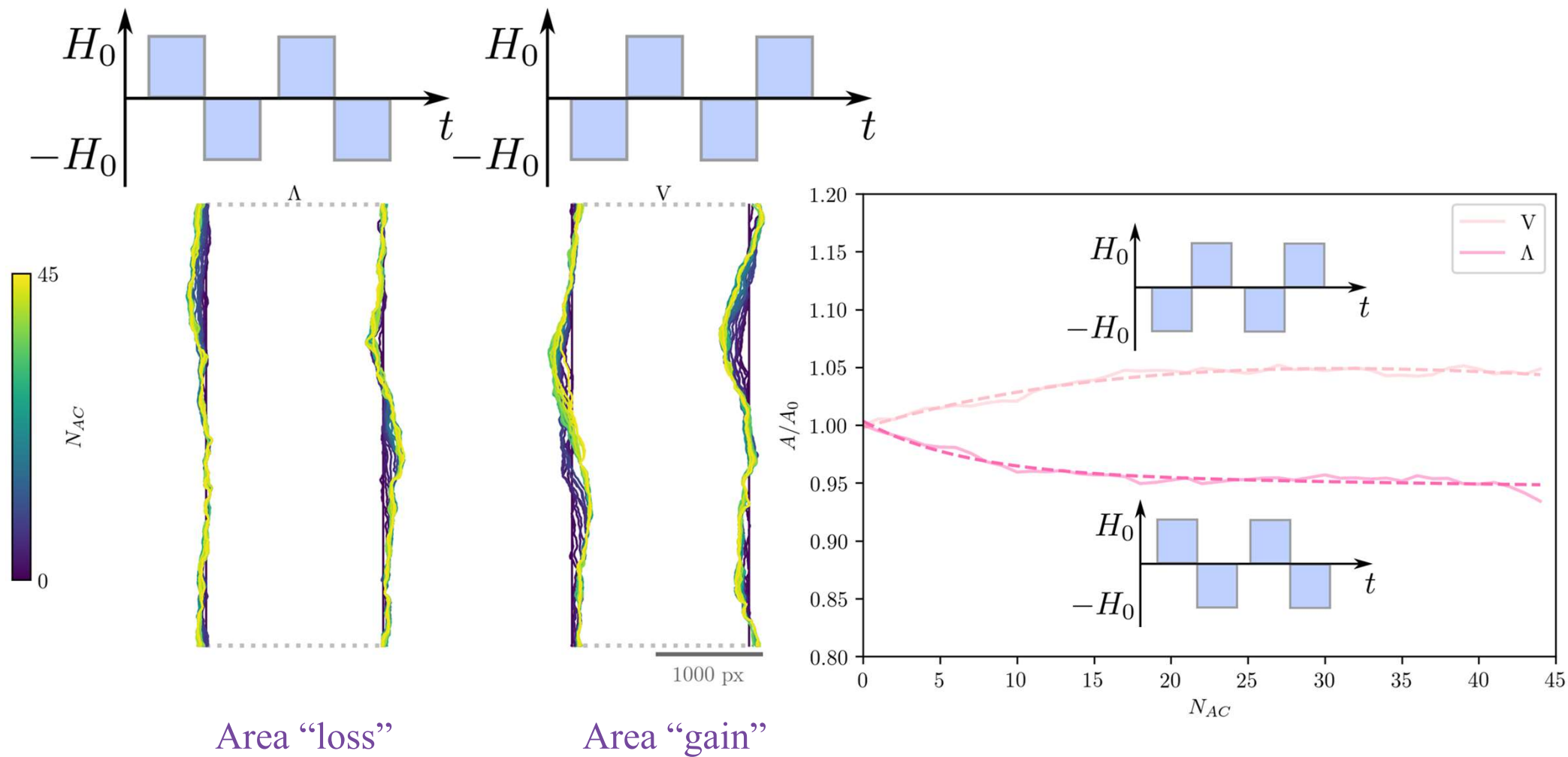
a)

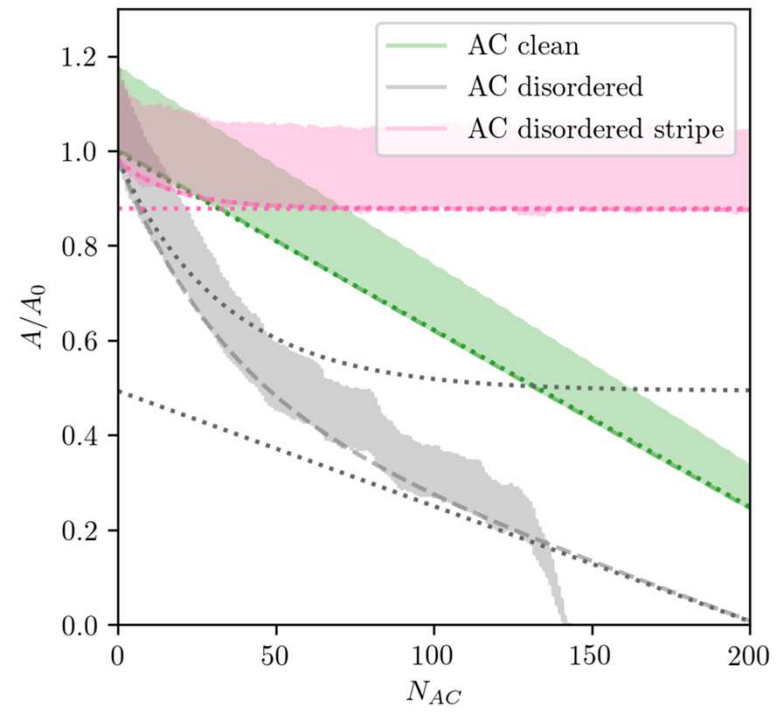


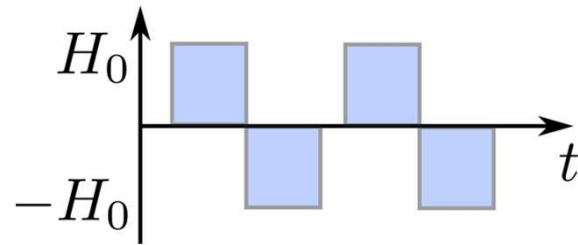
b)



But that is not all...







When domains are subjected to AC dynamics:
the disorder correlation length is changed (compared to the DC case)

This explains:

- the change in the observed exponent

$$\zeta_{DC} \rightarrow \zeta_{AC}$$

- the non linear part of the area loss