

**Dislocation Avalanches
from Strain Rate Controlled Loading:
A Discrete Dislocation Dynamics Study**

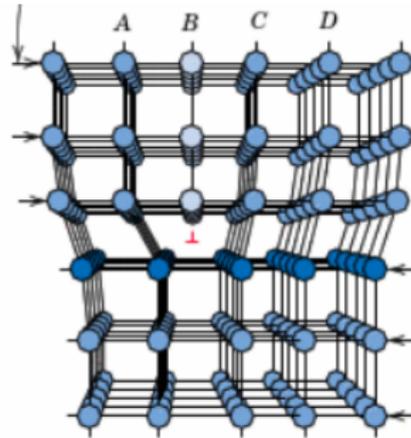
David Kurunczi-Papp and Lasse Laurson
david.kurunczi-papp@tuni.fi

Avalanche 2022, Debrecen, Hungary
31.08.2022

Motivation

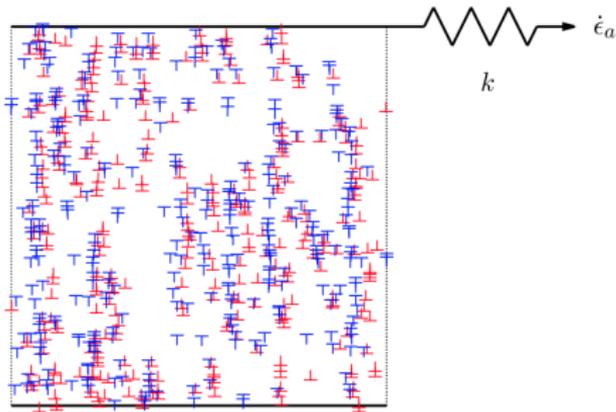


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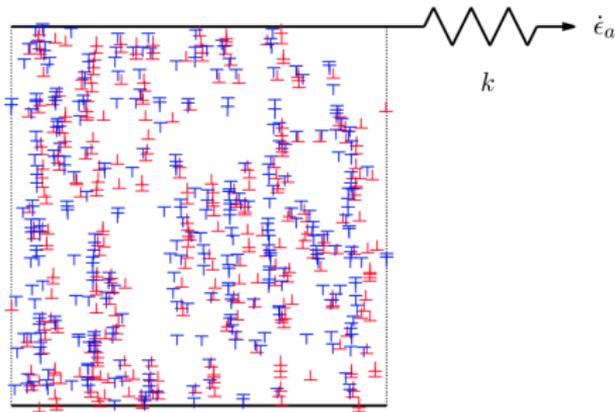


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Engineering

2D Discrete Dislocation Dynamics



2D Discrete Dislocation Dynamics

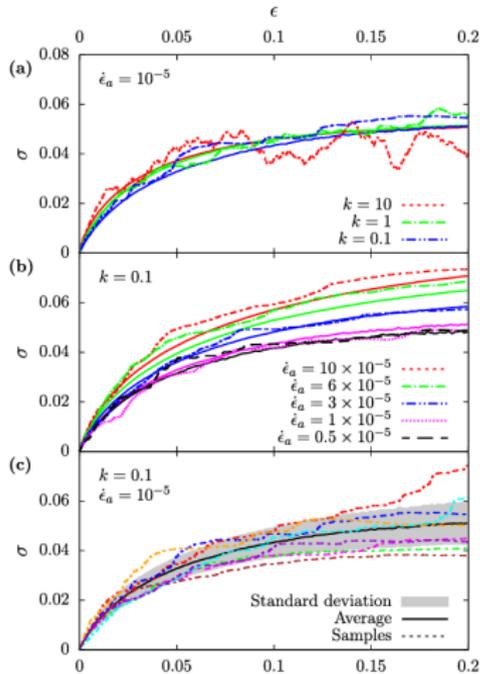


$$\frac{\dot{x}_i}{Mb} = s_i b \left[\sum_{j \neq i} s_j \sigma_d(\mathbf{r}_i - \mathbf{r}_j) + \sigma \right],$$

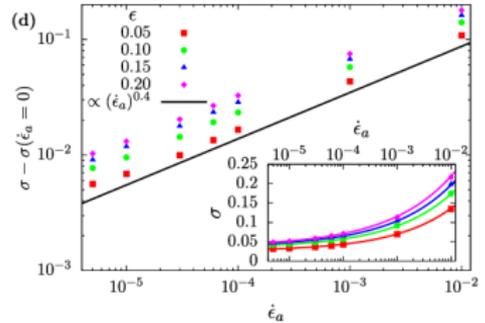
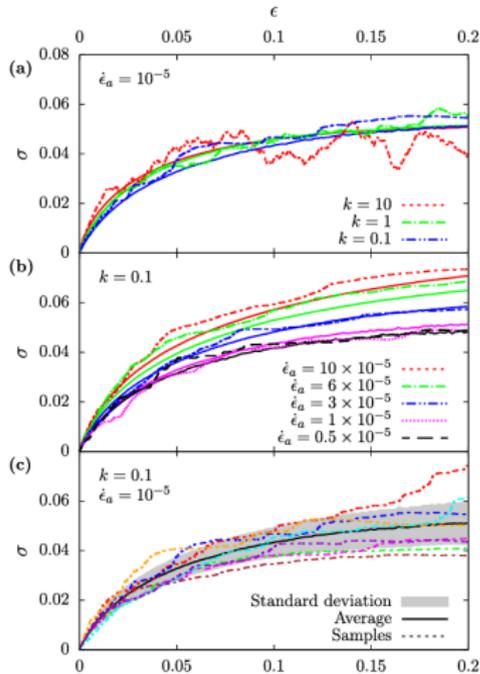
$$\sigma_d(\mathbf{r}) = Db \frac{x(x^2 - y^2)}{(x^2 + y^2)^2}$$

$$\sigma(t) = k [\dot{\epsilon}_a t - \epsilon(t)]$$

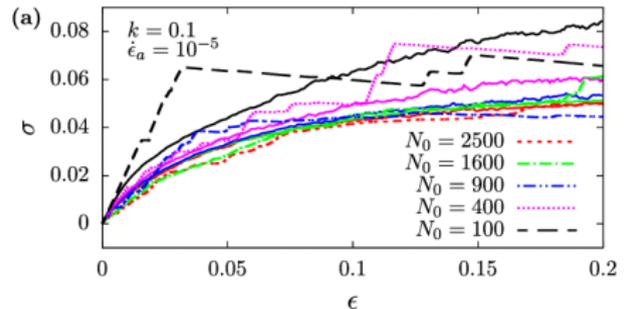
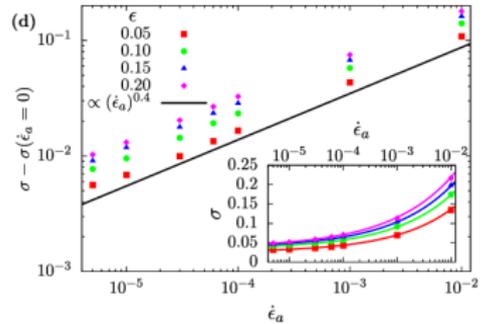
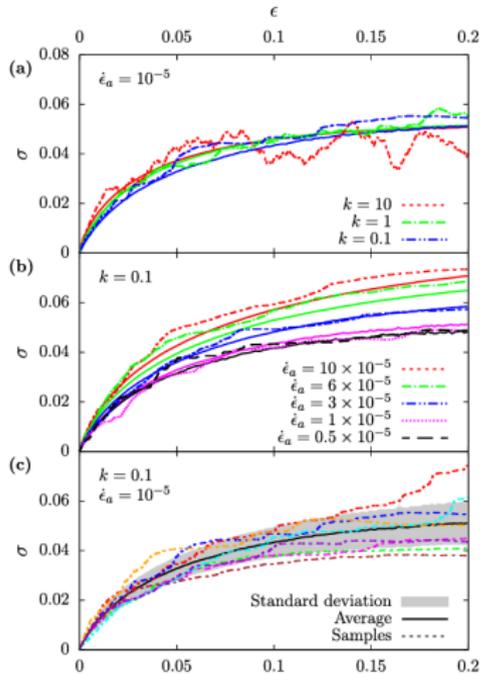
Stress-strain curves



Stress-strain curves

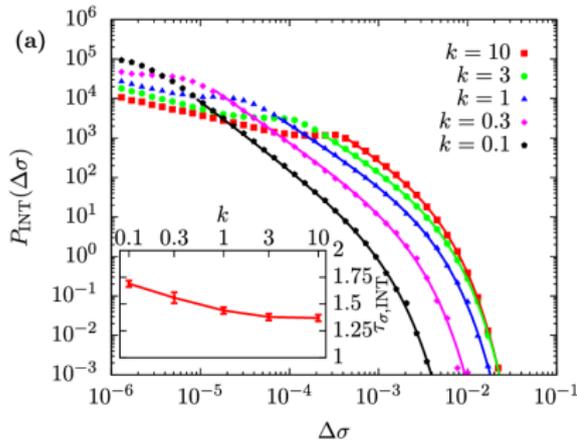


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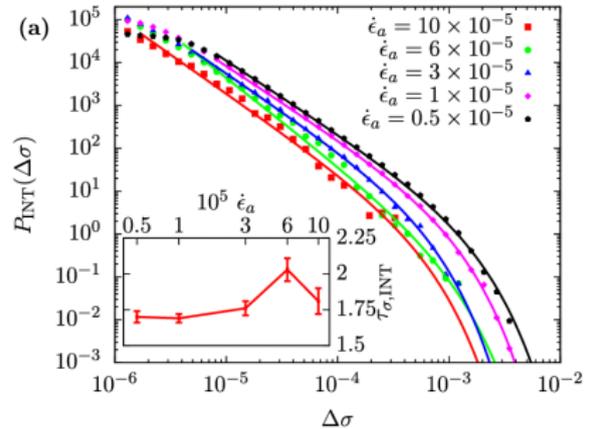
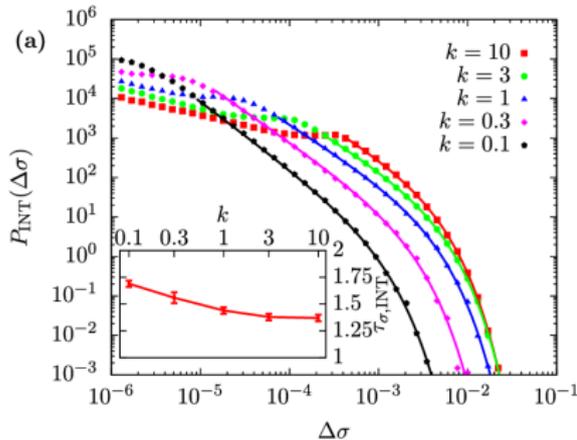
Stress drop magnitude distributions

$$P_{\text{INT}}(\Delta\sigma) \propto (\Delta\sigma)^{-\tau_\sigma} \exp\left(-\frac{\Delta\sigma}{\Delta\sigma_0}\right)$$



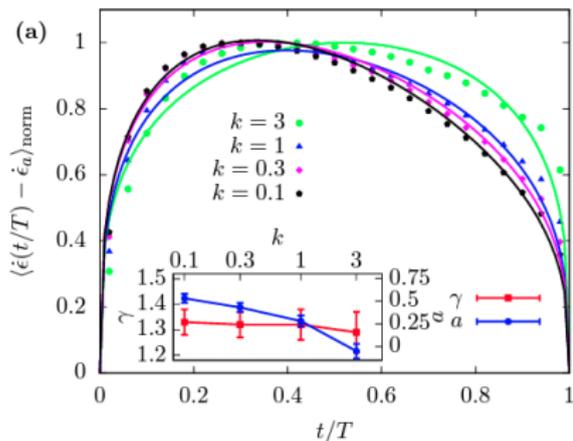
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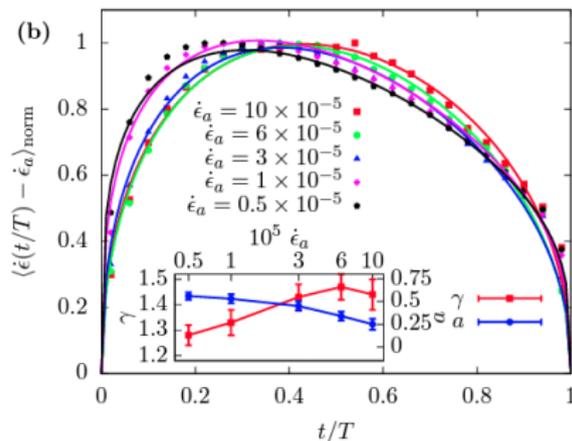
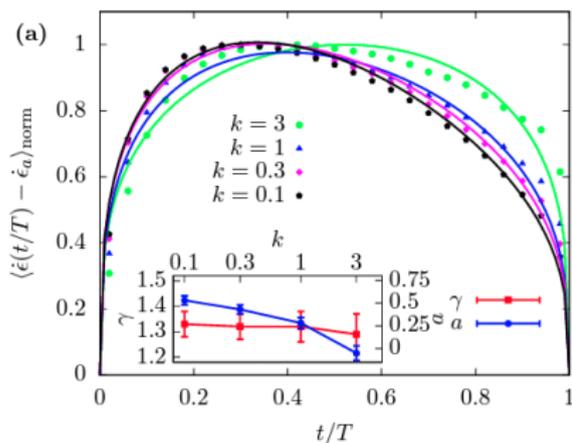
Average avalanche shapes

$$\langle \dot{\epsilon} \left(\frac{t}{T} \right) - \dot{\epsilon}_a \rangle \propto T^{\gamma-1} \left[\frac{t}{T} \left(1 - \frac{t}{T} \right) \right]^{\gamma-1} \left[1 - a \left(\frac{t}{T} - \frac{1}{2} \right) \right]$$

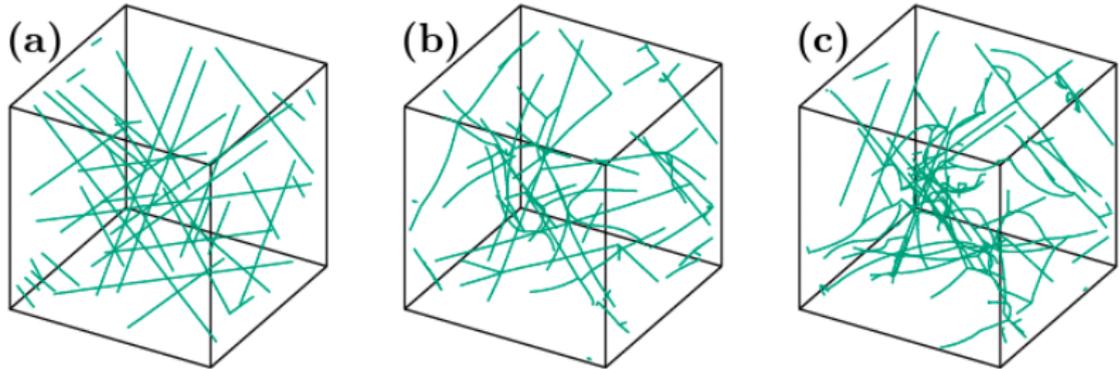


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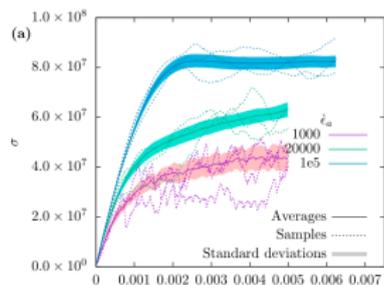
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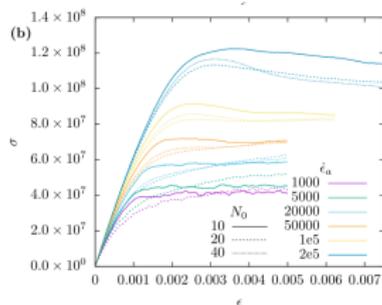
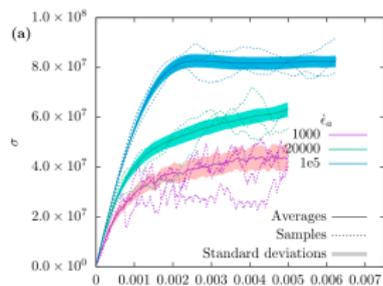
3D Discrete Dislocation Dynamics



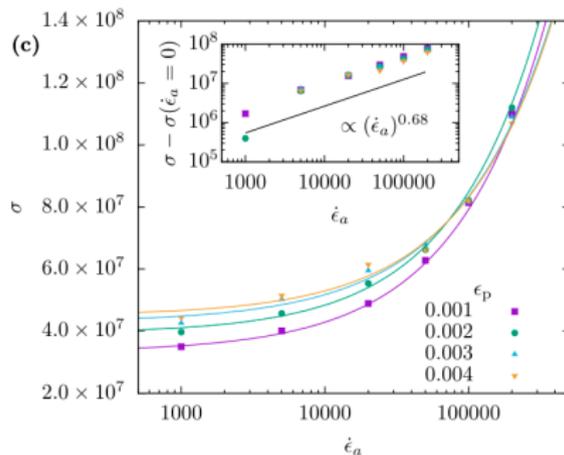
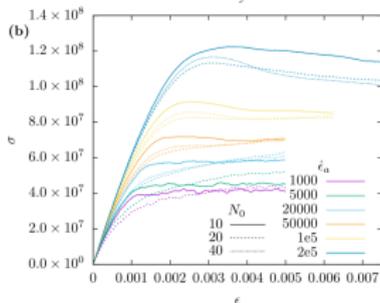
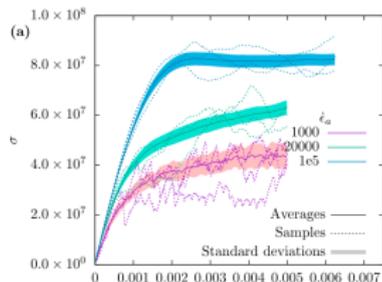
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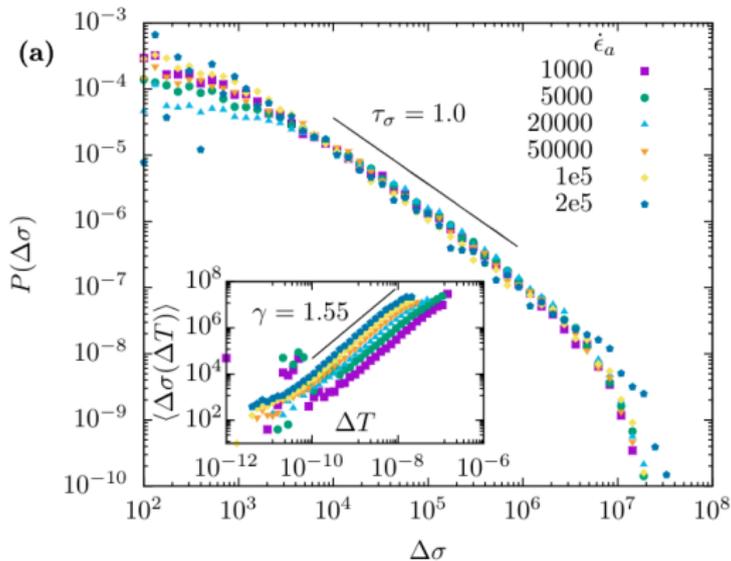


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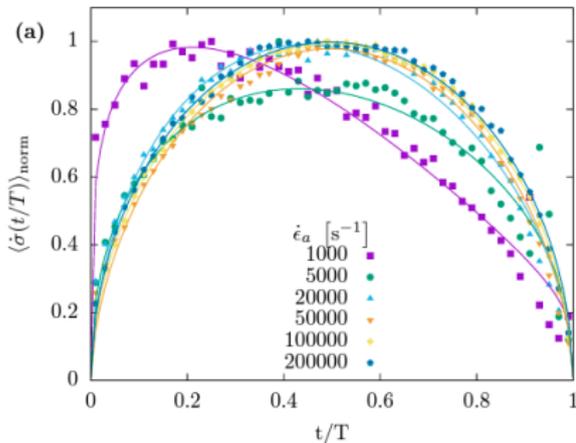
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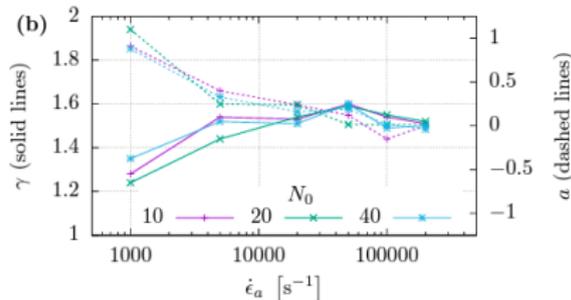
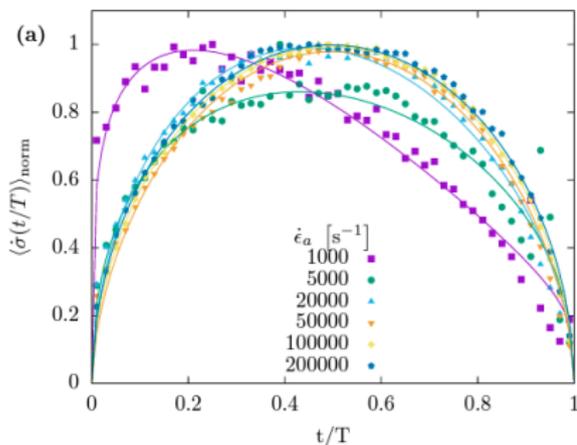
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Summary and conclusions

- ▶ Study the statistical properties of strain rate controlled loading of both 2D and 3D discrete dislocation simulations.
- ▶ Size- and rate dependence of the stress-strain curves
- ▶ In 2D the avalanche sizes are distributed by rate-dependent power laws, while in 3D the universal power law $\tau \approx 1.0$ is observed
- ▶ Rate dependent avalanche shapes with left asymmetries
- ▶ Several universality classes present in crystal plasticity

Thank you for Your attention!